

Mass and velocity anisotropy profiles of GOGREEN clusters

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& GOGREENers (most notably: van den Burg & Balogh)



Credits: "The incredible Hulk", (partly) shot on location in Toronto

Motivation:

1) $M(r)$: Cluster mass profile shape predicted to change with time

inner slope affected by adiabatic contraction (Blumenthal+86, Gnedin+04), accretion of subclusters (Laporte+12, Schaller+15), dynamical friction (El-Zant+01, +04), AGN feedback (Navarro+96, Ragone-Figueroa+12, Peirani+17)

outer slope affected by mass accretion (Diemer+Kratsov 14)

2) $\beta(r)$, velocity anisotropy profile \Leftrightarrow orbits of galaxies in clusters

Galaxy evolution (might) depend on the environment, that changes with time as the galaxy orbits the cluster

- ram pressure strength depends on a galaxy orbit (Tonnesen 19)
- galaxy morphology evolution depends on pericentric radius and number of pericentric passages (Joshi+20)



How to do this:

- ◆ Identify spectroscopic members
- ◆ Build stack cluster (*need samples of ≥ 200 galaxies*)
- ◆ Use MAMPOSSt to determine mass profile $M(r)$
- ◆ Use Jeans inversion to determine velocity anisotropy profile $\beta(r)$

Data-set:

GOGREEN + GCLASS

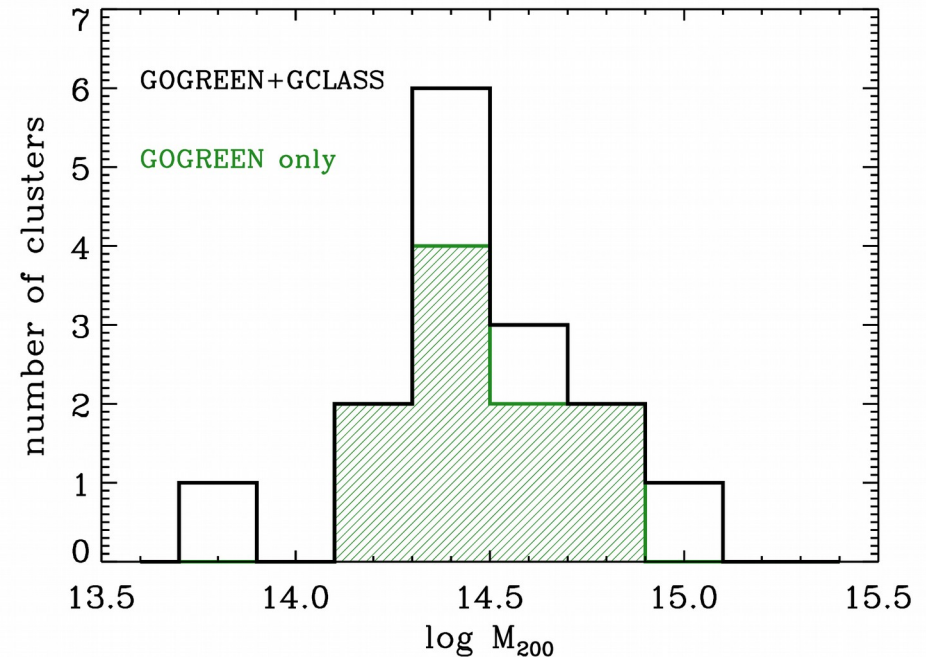
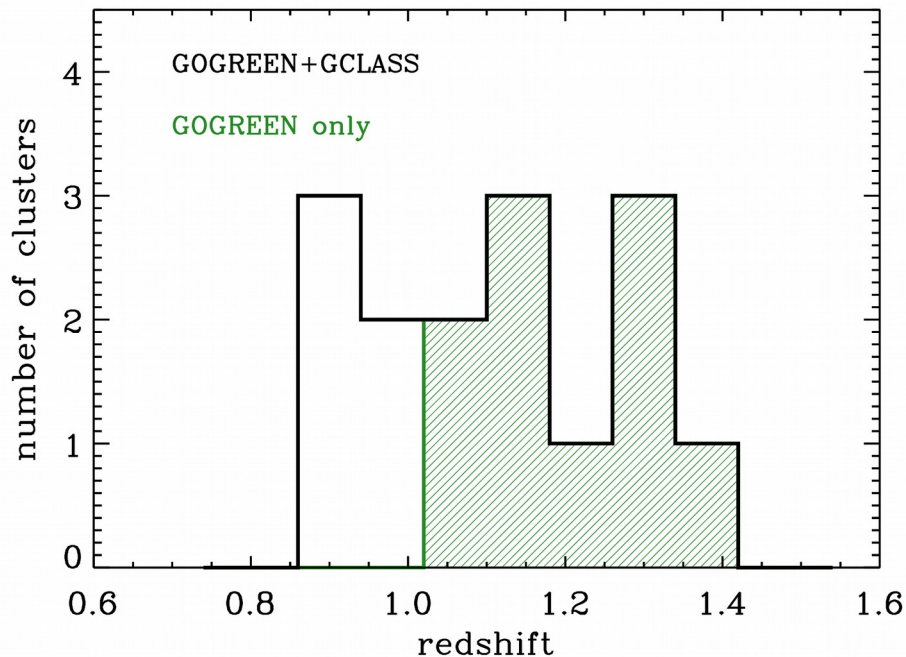
+ literature (Stalder+13, Sifón+16, Nantais priv.comm.)



Data-set:

GOGREEN: SPT 205, 546, 2106; SpARCS 35, 219, 335, 1051, 1616, 1634, 1638

GCLASS: SpARCS 34, 36, 215, 1047, 1613



Masses M_{200} based on velocity dispersion
(more on this in following slides)

Membership:

Must define cluster center

In velocity space:

use peak of velocity distribution,
then iterate using biweight mean velocity

In coordinate space, 2 choices (so far):

- 1) BCG positions (van den Burg + Chan)
- 2) luminosity-weighted centers (*analysis to be completed*)



Membership:

Use KMM to identify main peak in z space,
then refine the identification by two methods:

CLEAN (Mamon, AB, Boué 13) & CLUMPS (Munari, priv. comm.)

The 2 methods are conceptually very different although both based on
the location of a galaxy in its cluster projected phase space
(= line-of-sight rest-frame velocity vs. cluster-centric projected distance)

Assign weights: 1 = CLEAN and CLUMPS member
1/2 = CLEAN xor CLUMPS member
0 = neither CLEAN nor CLUMPS member

677 cluster members (sum of membership weights = 613.5)
in 15 clusters (3 SPT + 12 SpARCS) with $0.87 \leq z \leq 1.37$



Stacking:

Limited statistics per cluster \Rightarrow
need to stack clusters to determine $\langle M(r) \rangle$ and/or $\langle \beta(r) \rangle$

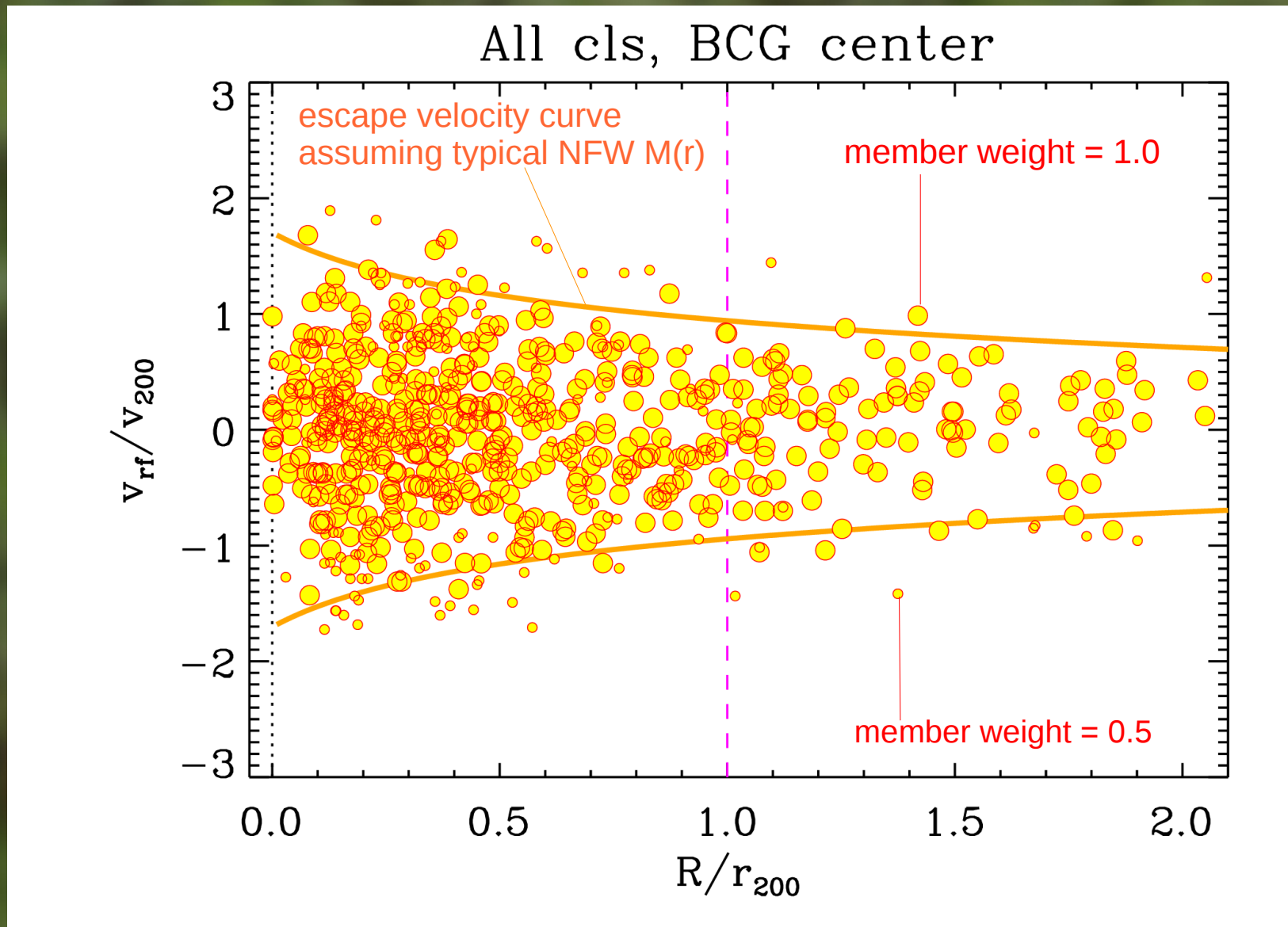
Normalize galaxy cluster-centric projected distances (“radii” R)
by r_{200} , and galaxy line-of-sight rest-frame velocities (v_{rf}) by v_{200}

Determine r_{200} (hence also v_{200} and M_{200} given cluster $\langle z \rangle$ and cosmology)
from velocity dispersion using **3 different prescriptions to check for systematics** (no difference found among the 3 resulting stacked cluster projected phase-space distributions)

Assume spherical symmetry – this is not a bad assumption for a stack cluster (van der Marel+00) as long as there is no selection bias for clusters elongated along the line-of-sight



Stacked projected phase-space



weighted average of clusters r_{200} (using number of members as weights): **0.98 Mpc**

The Jeans equation

$$M(< r) = -\frac{r\sigma_r^2}{G} \left(\frac{d \ln \nu}{d \ln r} + \frac{d \ln \sigma_r^2}{d \ln r} + 2\beta \right)$$

Mass profile

3D number density profile

Velocity dispersion profile along the radial direction, r

Velocity anisotropy profile

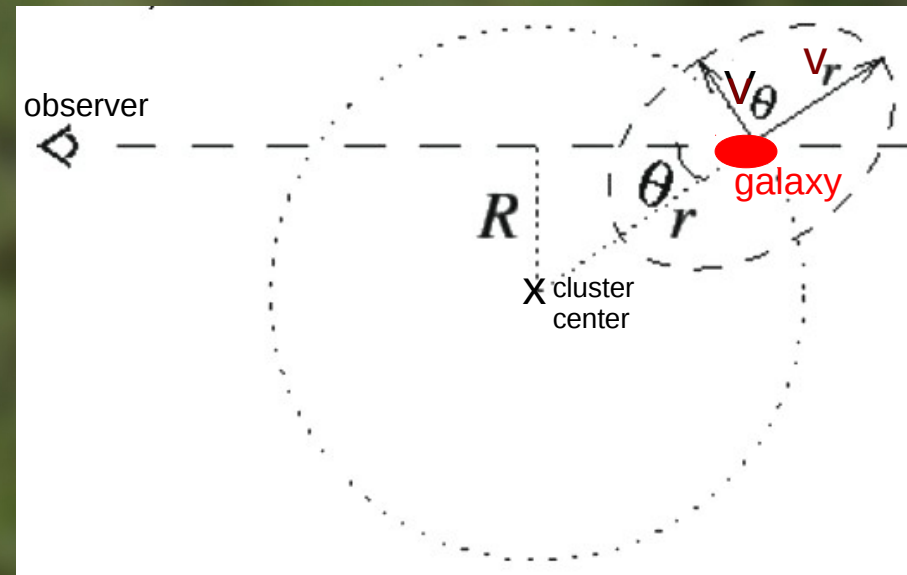
$$\beta(r) = 1 - \frac{\sigma_\theta^2(r)}{\sigma_r^2(r)}$$

Velocity dispersion profile along the tangential direction



The solution for the mass profile $M(<r)$ is degenerate with the solution for the velocity anisotropy profile $\beta(r)$:

Mass-Anisotropy Degeneracy
(aka Jeans' MADness)



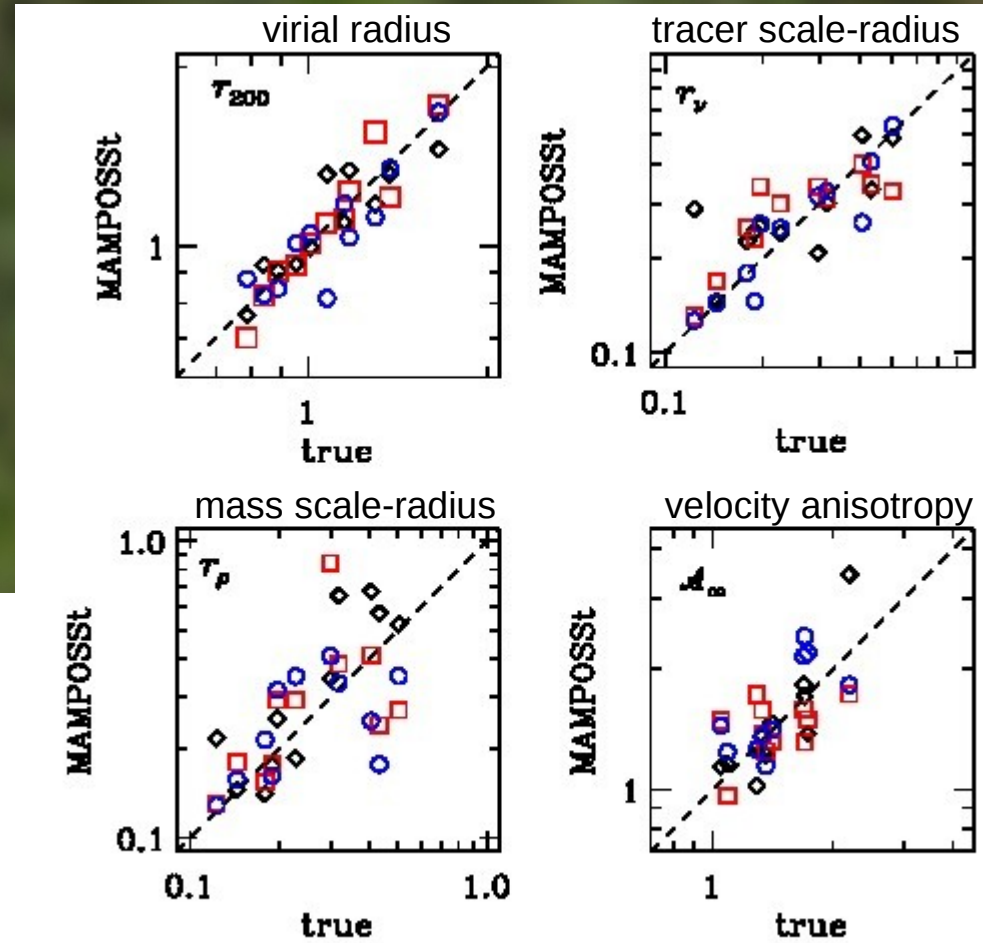
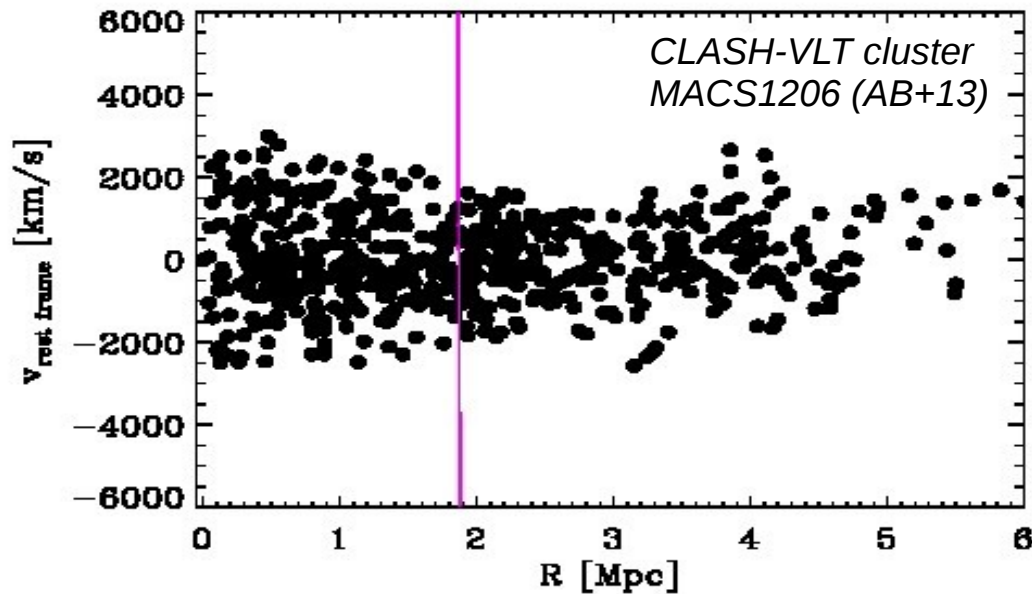
(courtesy of G. Mamon)

Solving the Jeans equation with observables:

MAMPOSSt (Mamon, AB, Boué 13)

Performs a maximum likelihood fit of model $M(r)$ and model $\beta(r)$ to the projected phase-space distribution of cluster galaxies

Modelling
Anisotropy and
Mass
Profiles of
Observed
Spherical
Systems



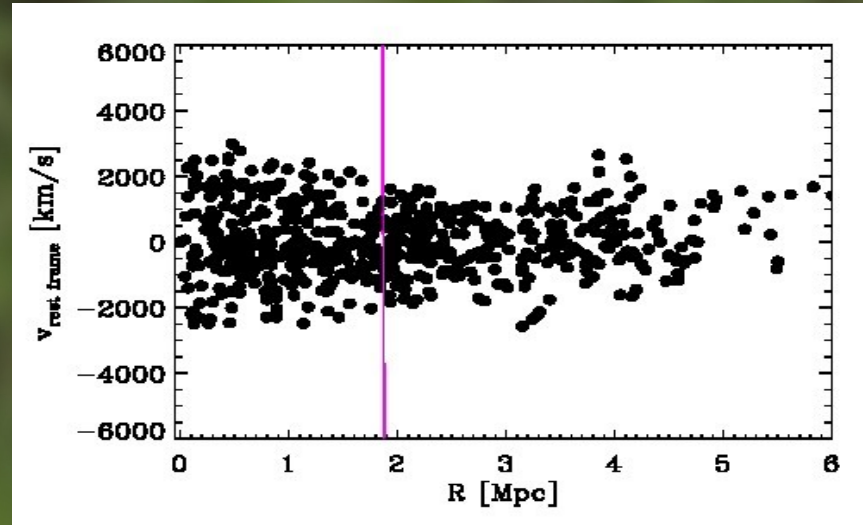
Cluster-size halos from numerical simulations

Using the full information available in projected phase-space...

**MAMPOSSt cures
Jeans' MADness!**



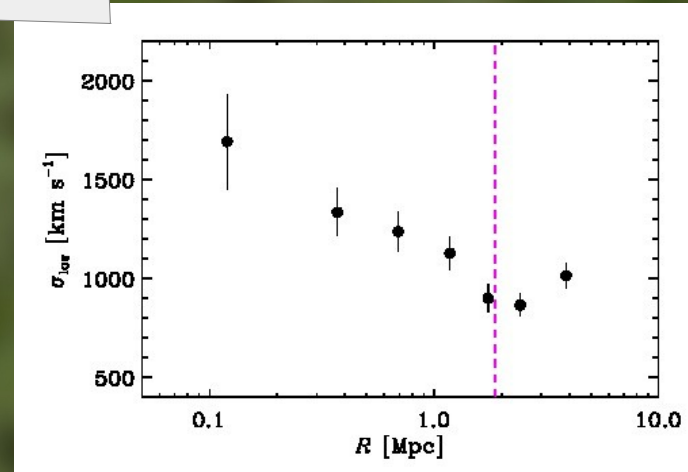
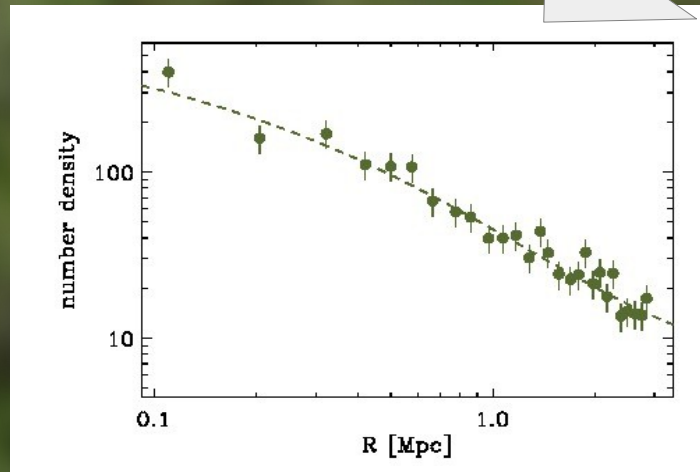
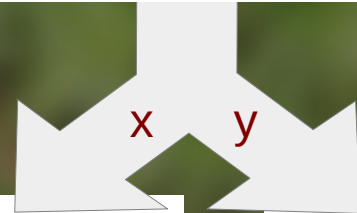
Solving the Jeans equation with observables:



Projected phase-space distribution of cluster member galaxies

projected number density profile $N(R)$

line-of-sight velocity dispersion profile $\sigma_{\text{los}}(R)$



$M(r)$ +

If known, e.g. from lensing or MAMPOSSt

+

→ $\beta(r)$

Inversion of the Jeans equation

(Binney & Mamon 82, see also Solanes & Salvador-Solé 90)



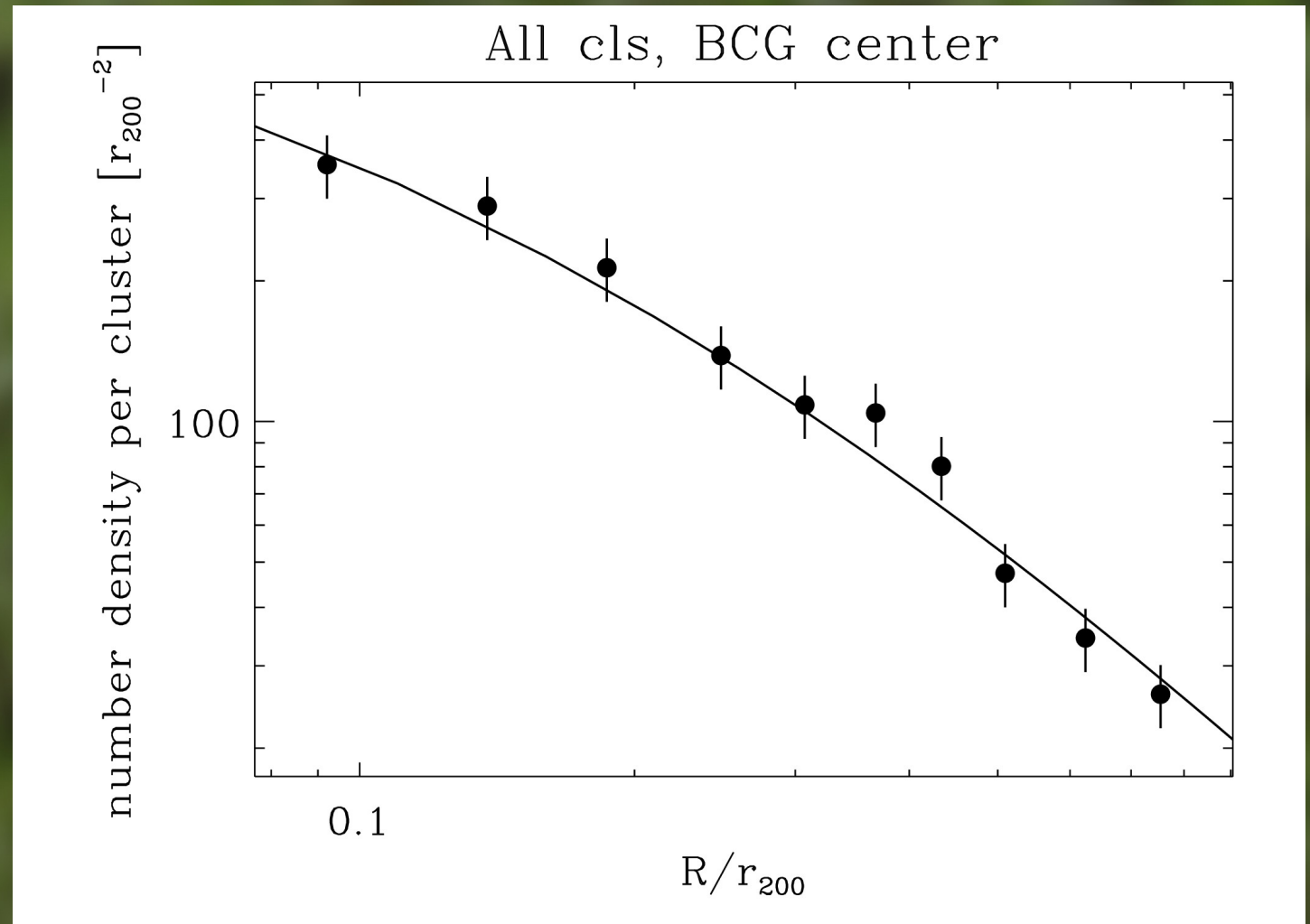
The number density profile

Use the photometric sample to correct for the spectroscopic sample incompleteness (van den Burg)

Best-fit with
projected
NFW profile:

$$r_v = 0.24 r_{200}$$

$$c_v = 4.1$$



Running MAMPOSSt

Mass models considered (γ , γ_{out} is the logarithmic inner/outer slope)

gNFW: $\gamma = 0.0, 0.5, 1.0$ (NFW), 1.5; $\gamma_{out} = 3$

Burkert: $\gamma = 0.0$; $\gamma_{out} = 3$

Hernquist: $\gamma = 1.0$; $\gamma_{out} = 4$

Einasto: γ approaching 0.0 asymptotically; $\gamma_{out} = 3$

Velocity anisotropy models considered:

Constant with radius

Rising from isotropy to radial orbits with radius (3 different models)

Rising from tangential to radial orbits (or viceversa)

Use membership weights in the analysis

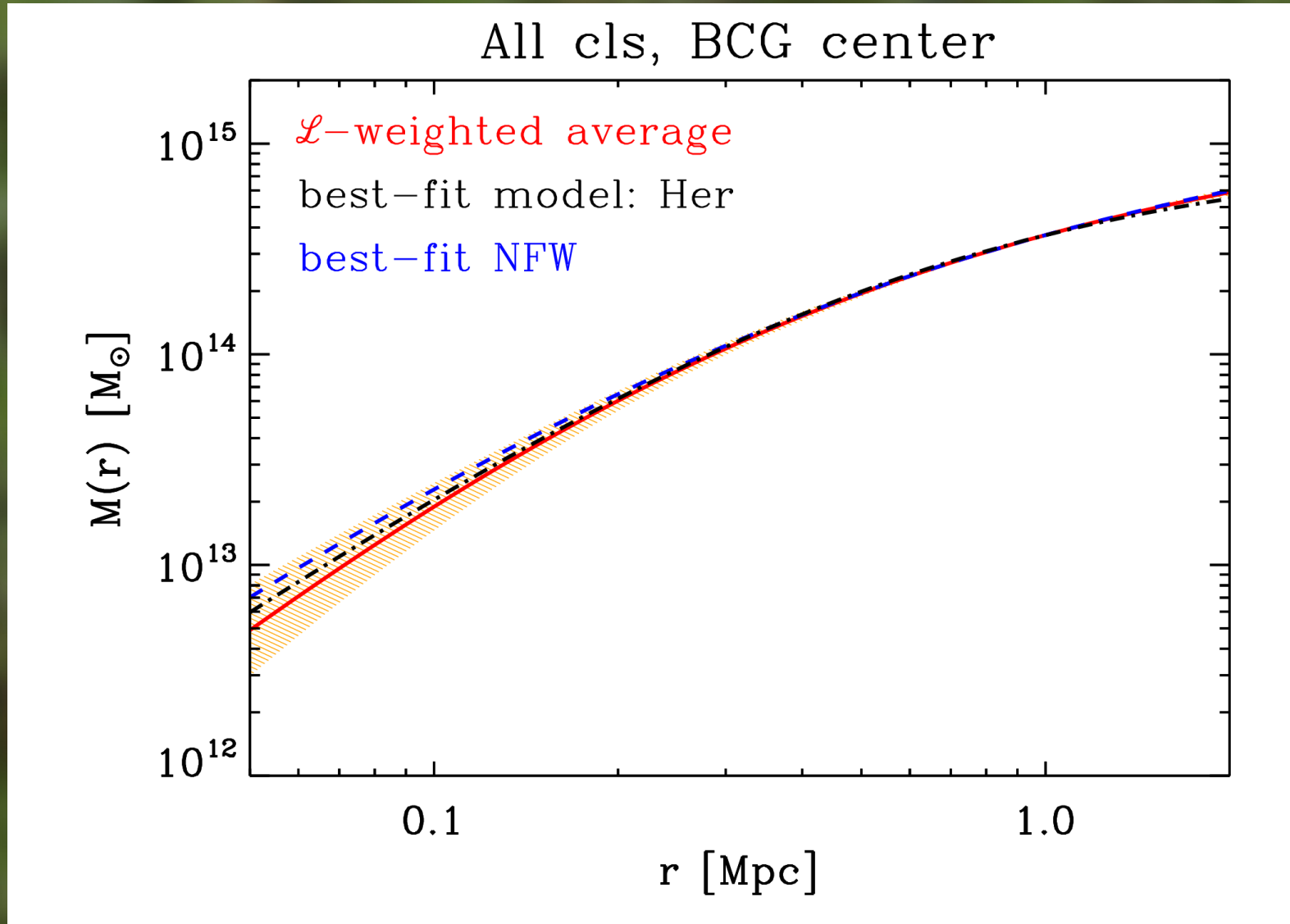


Mass profiles, $M(r)$

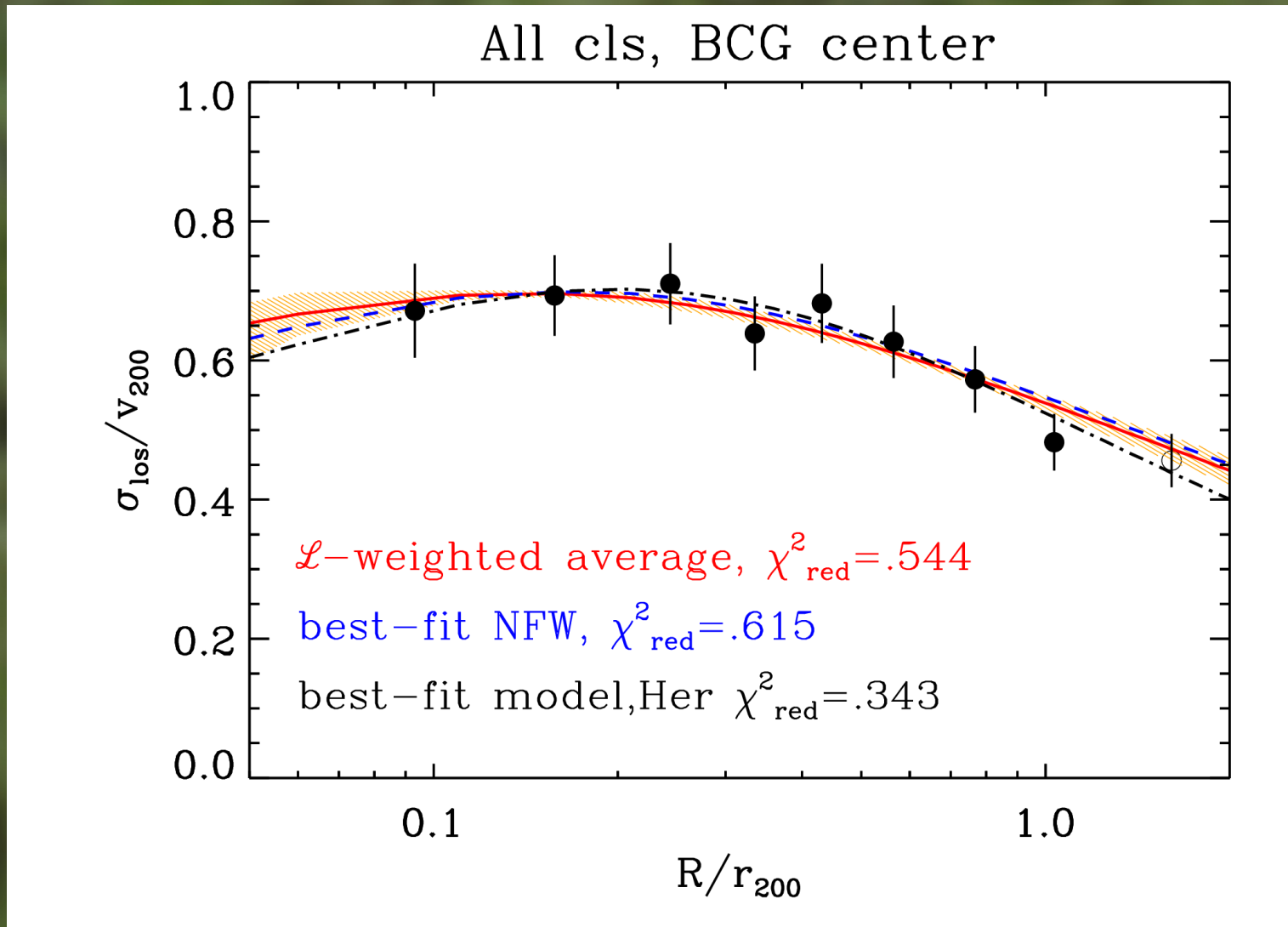


MAMPOSSt: results

All models are acceptable in terms of relative likelihoods

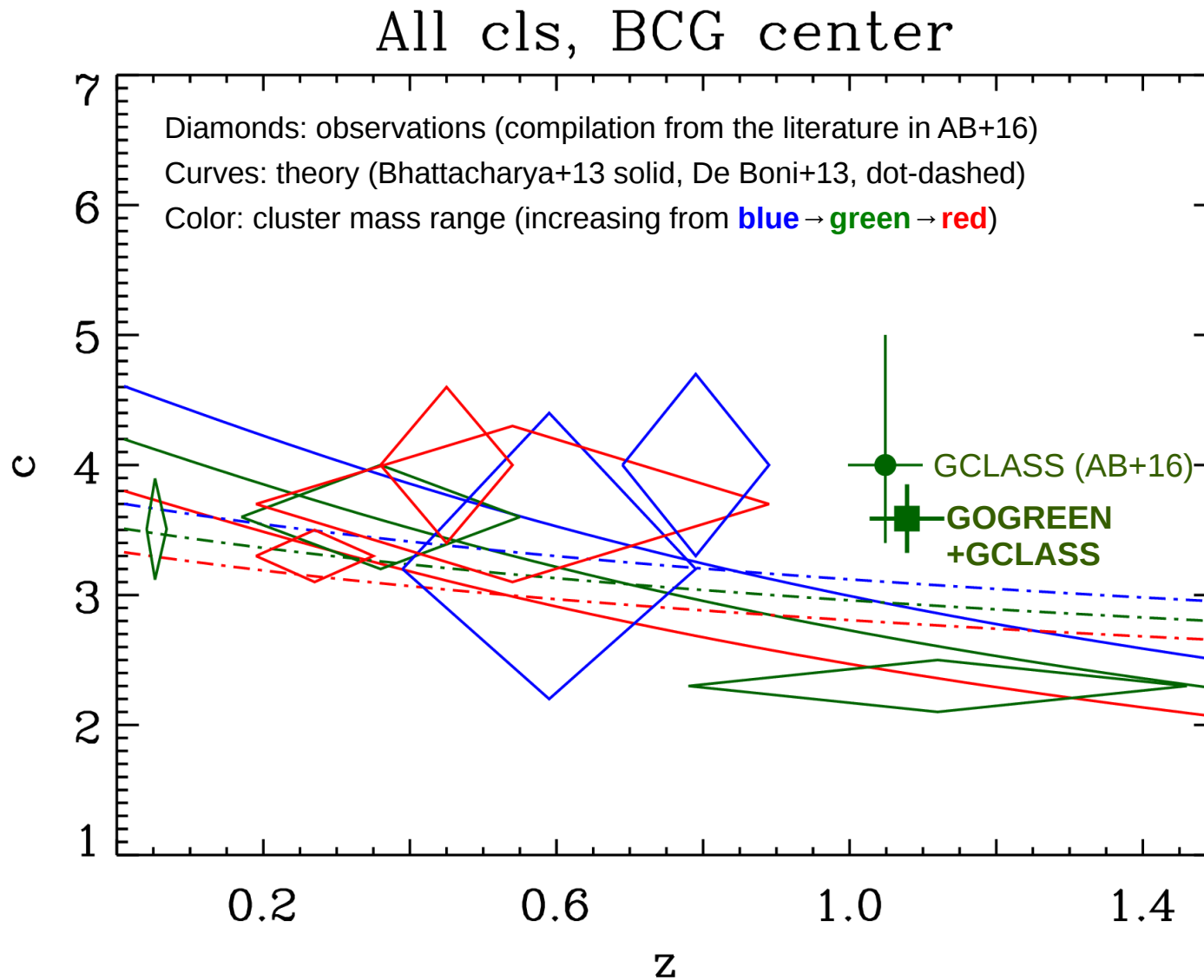


MAMPOSSt: predicted velocity dispersion profile



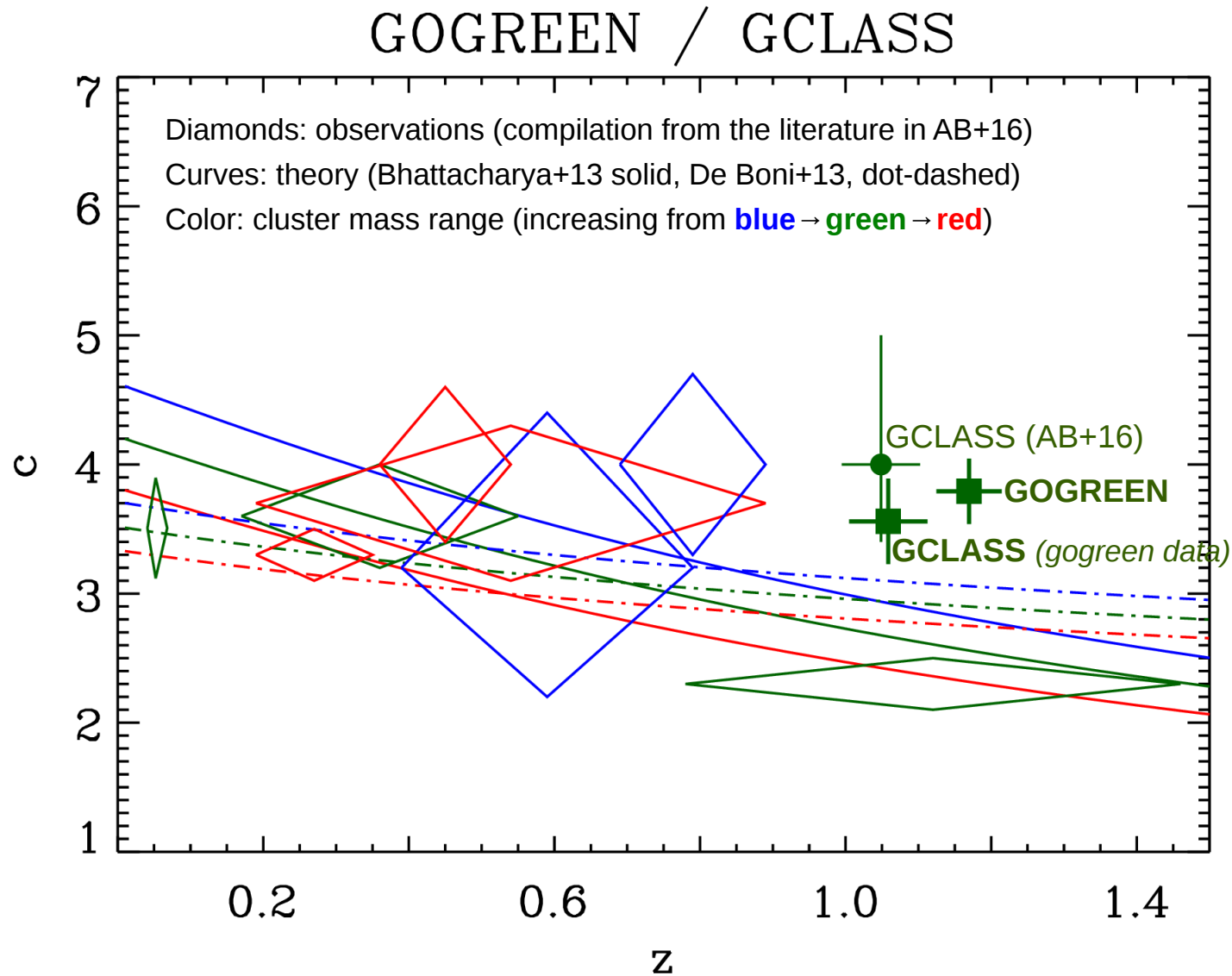
Model-likelihood weighted average $M(r)$ projected onto the line-of-sight velocity dispersion profile (red) compared with the data (black dots)

MAMPOSSt: concentration of $M(r)$



Predicted and observed evolution of the total mass concentration

MAMPOSSt: concentration of $M(r)$



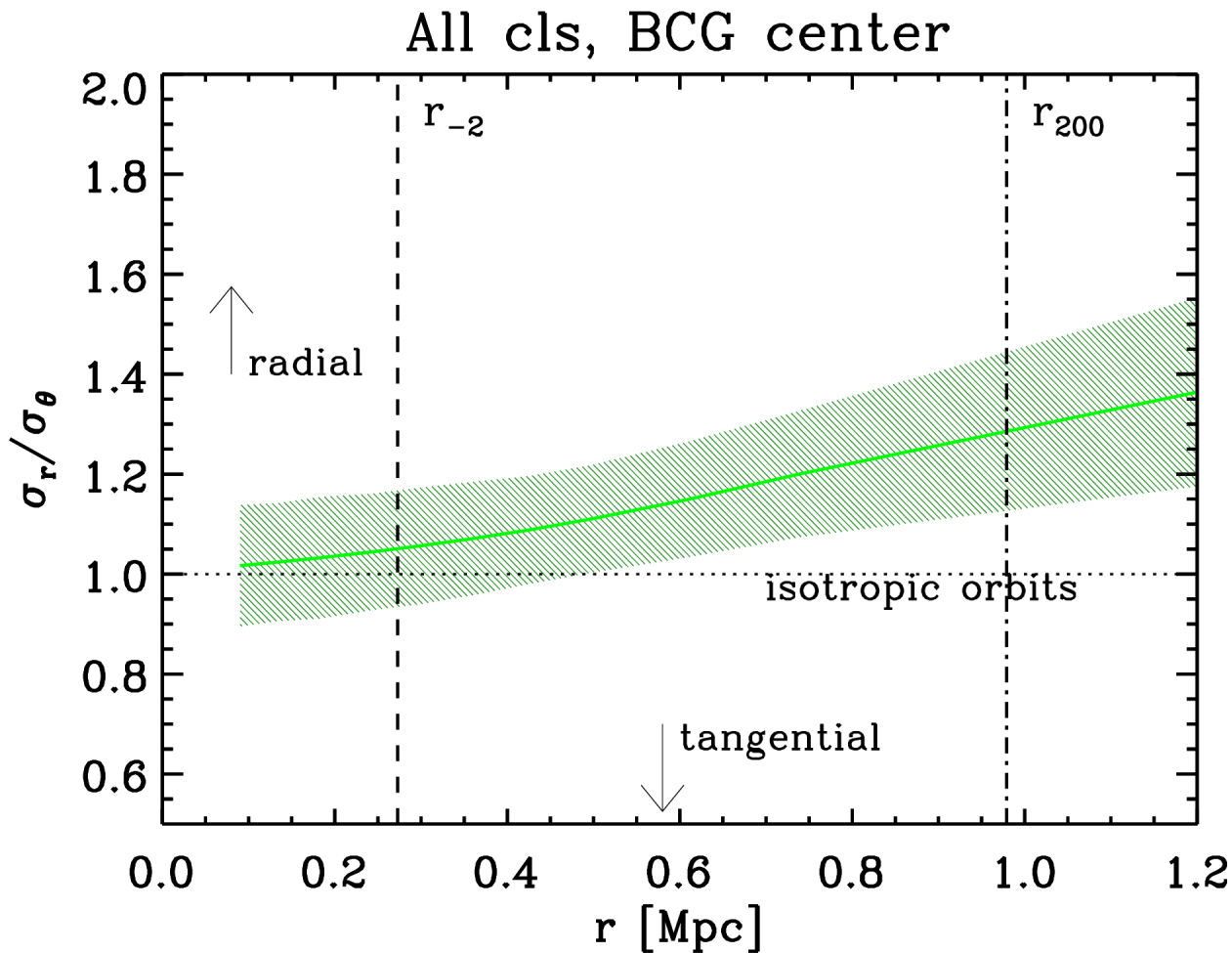
Extending the constraints on c to higher z : tension with theory
No redshift-dependence

Velocity anisotropy profiles, $\beta(r)$



Jeans inversion: velocity anisotropy

Use weighted average $M(r)$ from MAMPOSSt analysis, observed (incompleteness-corrected) number density profile and observed velocity dispersion profile (using membership weights)

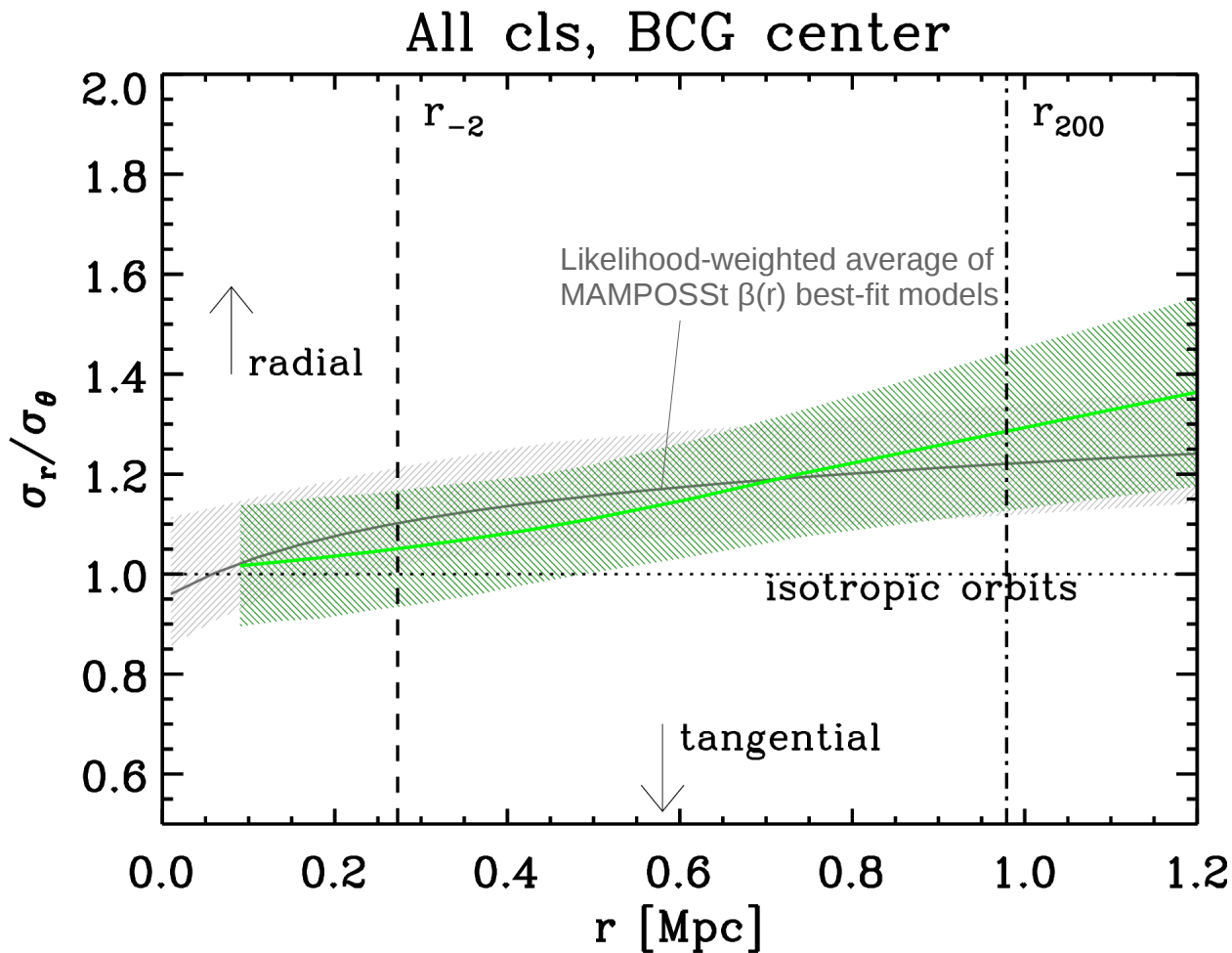


$$\beta(r) = 1 - \frac{\sigma_\theta^2(r)}{\sigma_r^2(r)}$$

Ratio between the radial and tangential components of the 3-d velocity dispersion vs. the 3-d cluster-centric distance

Jeans inversion: velocity anisotropy

Using MAMPOSSt $M(r)$ to get $\beta(r)$ from Jeans equation inversion gives consistent results with $\beta(r)$ obtained directly from MAMPOSSt



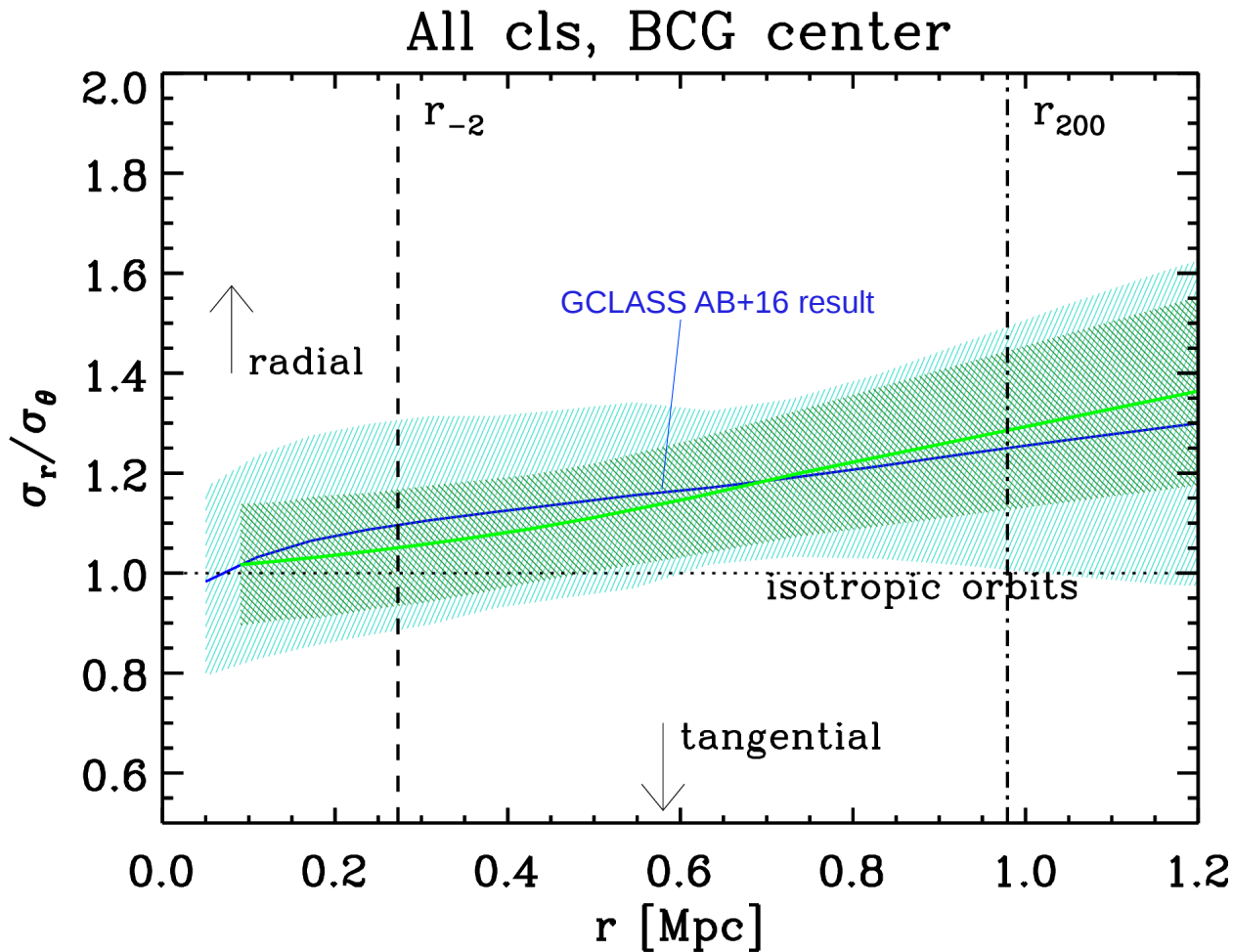
$$\beta(r) = 1 - \frac{\sigma_\theta^2(r)}{\sigma_r^2(r)}$$

MAMPOSSt $\beta(r)$ error bars are smaller than for Jeans inversion because of the restricted range of models considered

Jeans inversion: velocity anisotropy

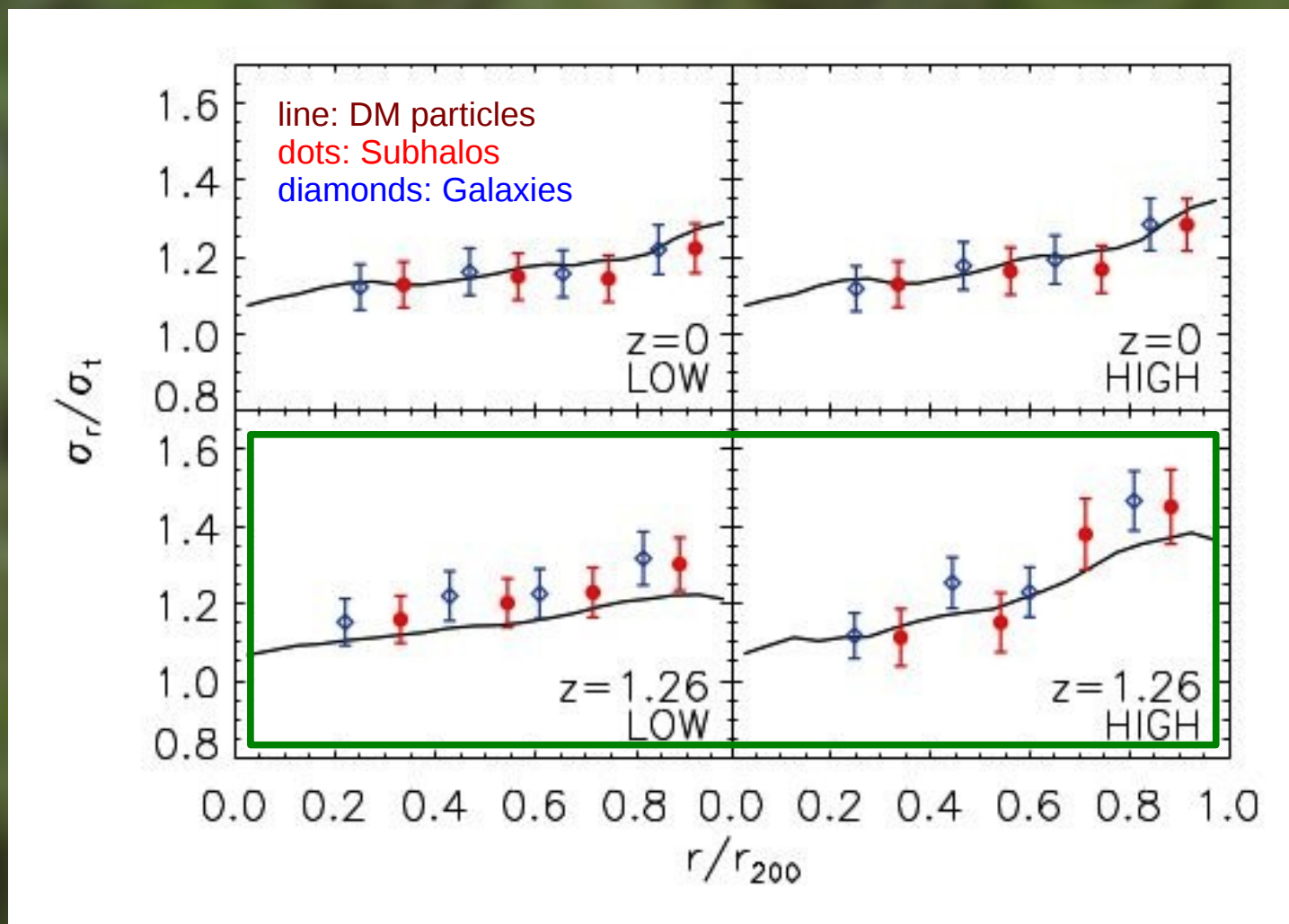
Comparison with result of AB+16 based on the GCLASS sample:
no difference, but smaller error bars

⇒ orbits are now *inconsistent* with isotropy



$$\beta(r) = 1 - \frac{\sigma_\theta^2(r)}{\sigma_r^2(r)}$$

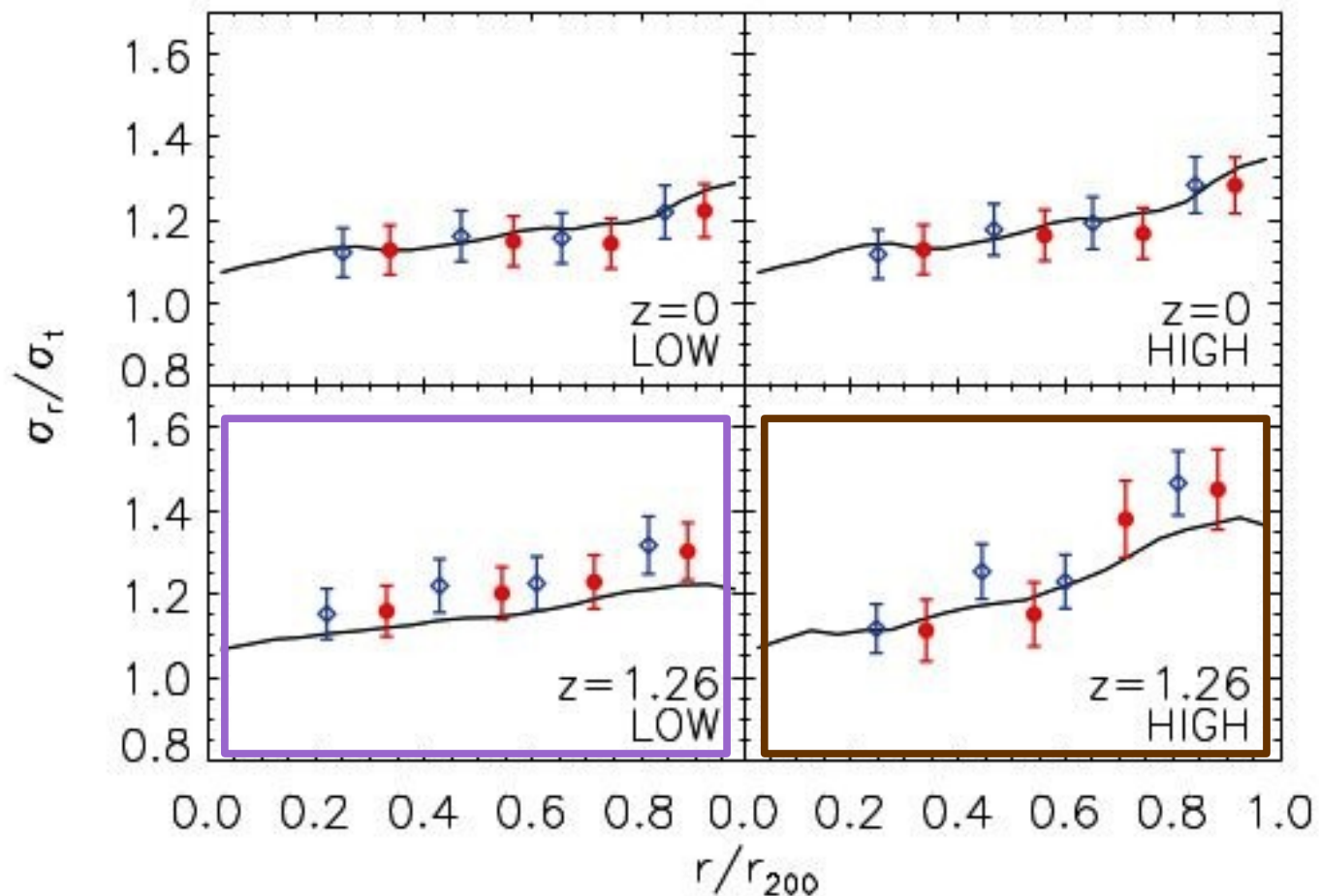
Orbits in numerical simulations



Munari, AB +13: orbits of dark matter particles, subhalos and “galaxies” are similar

Good agreement with GOGREEN velocity anisotropy profile

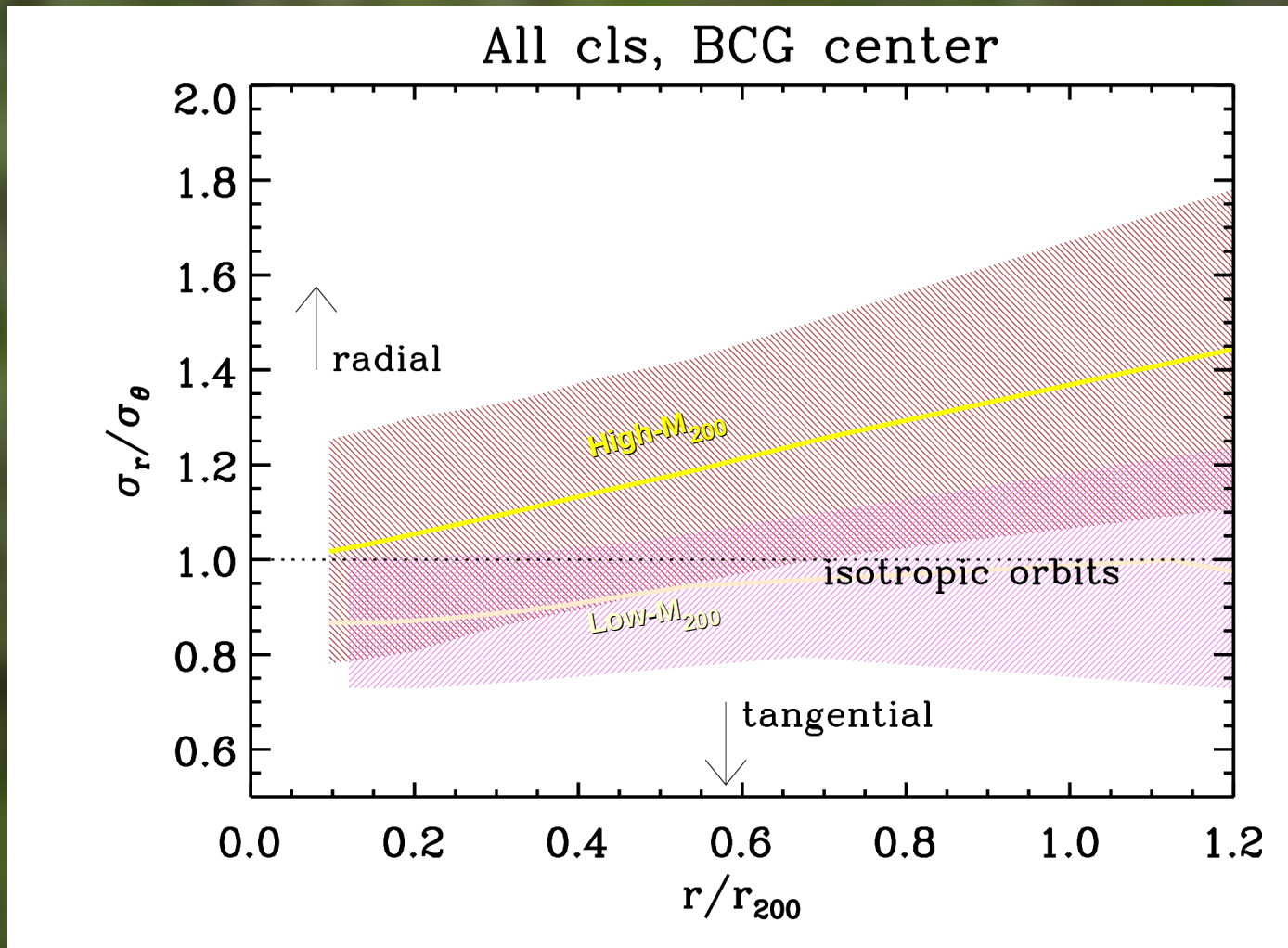
Orbits in numerical simulations



Munari, AB +13:
mild dependence on halo mass (LOW / HIGH) and redshift ($z=0$ / $z=1.26$).
Good agreement with observed velocity anisotropy profile

Jeans inversion: velocity anisotropy

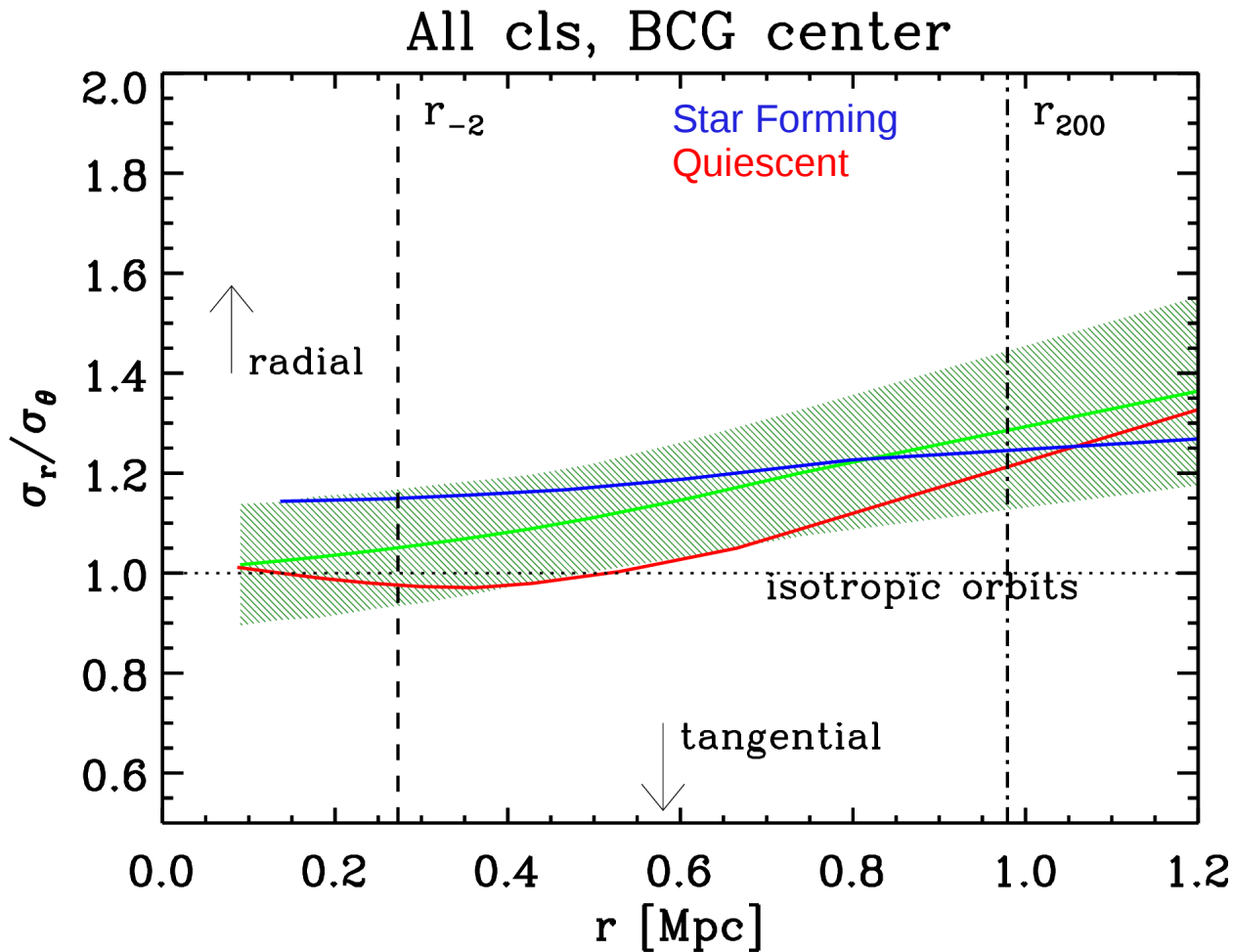
Low- M_{200} vs. High- M_{200} GOGREEN+GCLASS clusters
no difference but **trend consistent with results from simulations**



$$\beta(r) = 1 - \frac{\sigma_\theta^2(r)}{\sigma_r^2(r)}$$

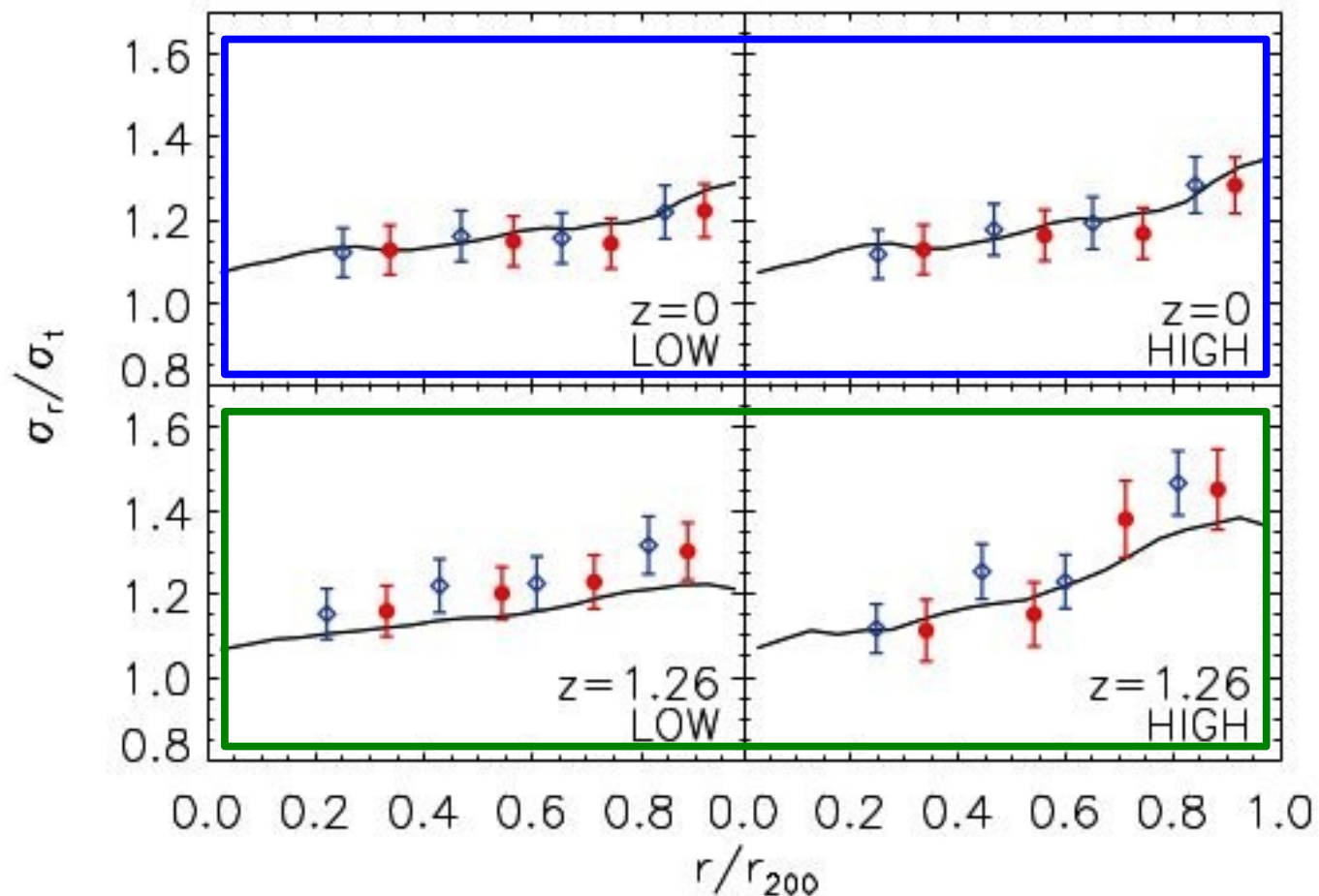
Jeans inversion: velocity anisotropy

Quiescent vs. star-forming galaxies (with $\log M_* \geq 9.0$):
no significant difference (*similar result as for GCLASS, AB+16*)



$$\beta(r) = 1 - \frac{\sigma_\theta^2(r)}{\sigma_r^2(r)}$$

Orbits in numerical simulations

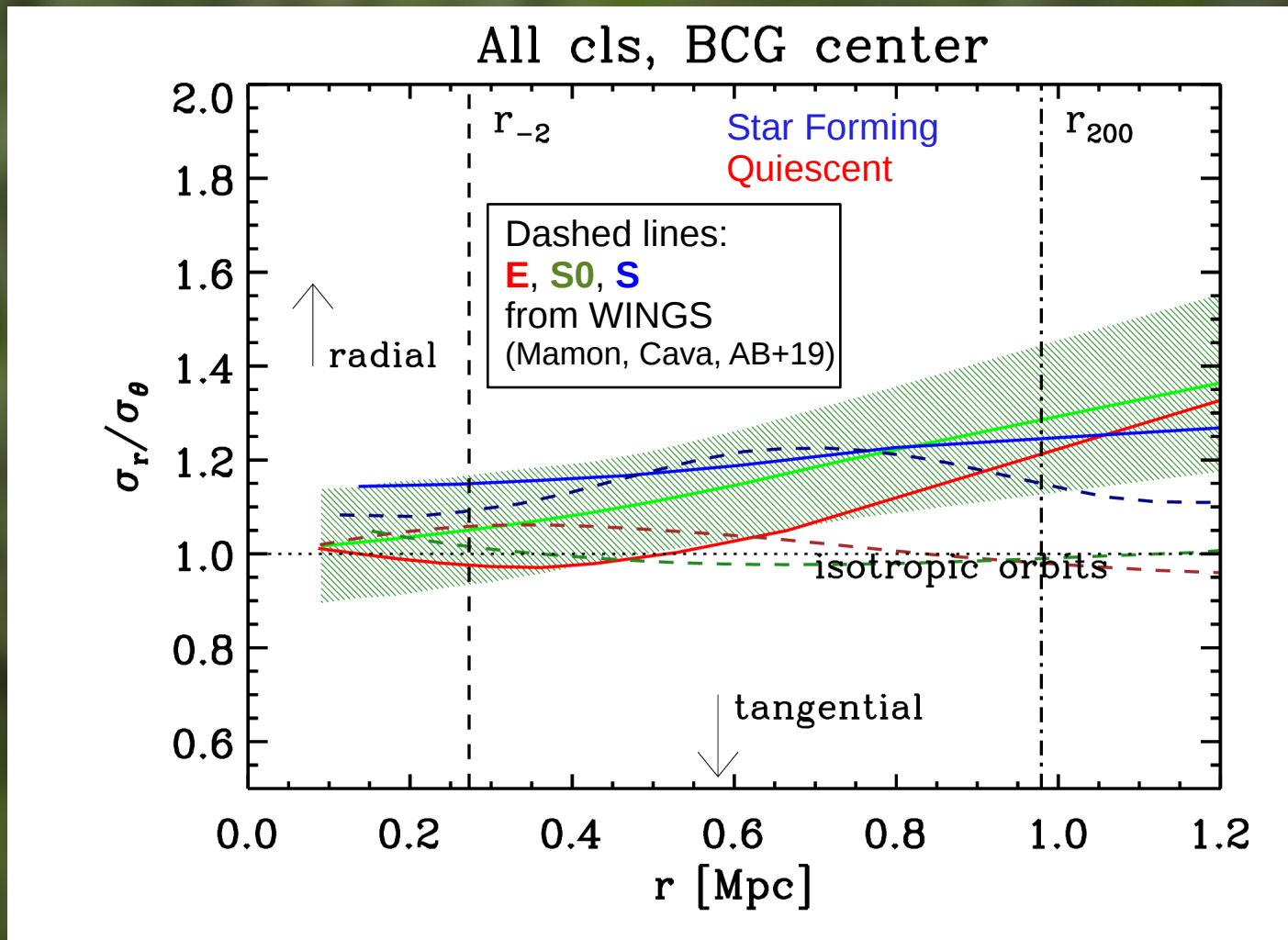


Munari, AB +13:
mild dependence on redshift ($z=0$ / $z=1.26$).

Good agreement with GOGREEN velocity anisotropy profile

Jeans inversion: velocity anisotropy

Quiescent vs. star-forming galaxies (with $\log M_* \geq 9.0$):
comparison with nearby clusters (WINGS, $0.04 < z < 0.07$)



$$\beta(r) = 1 - \frac{\sigma_\theta^2(r)}{\sigma_r^2(r)}$$

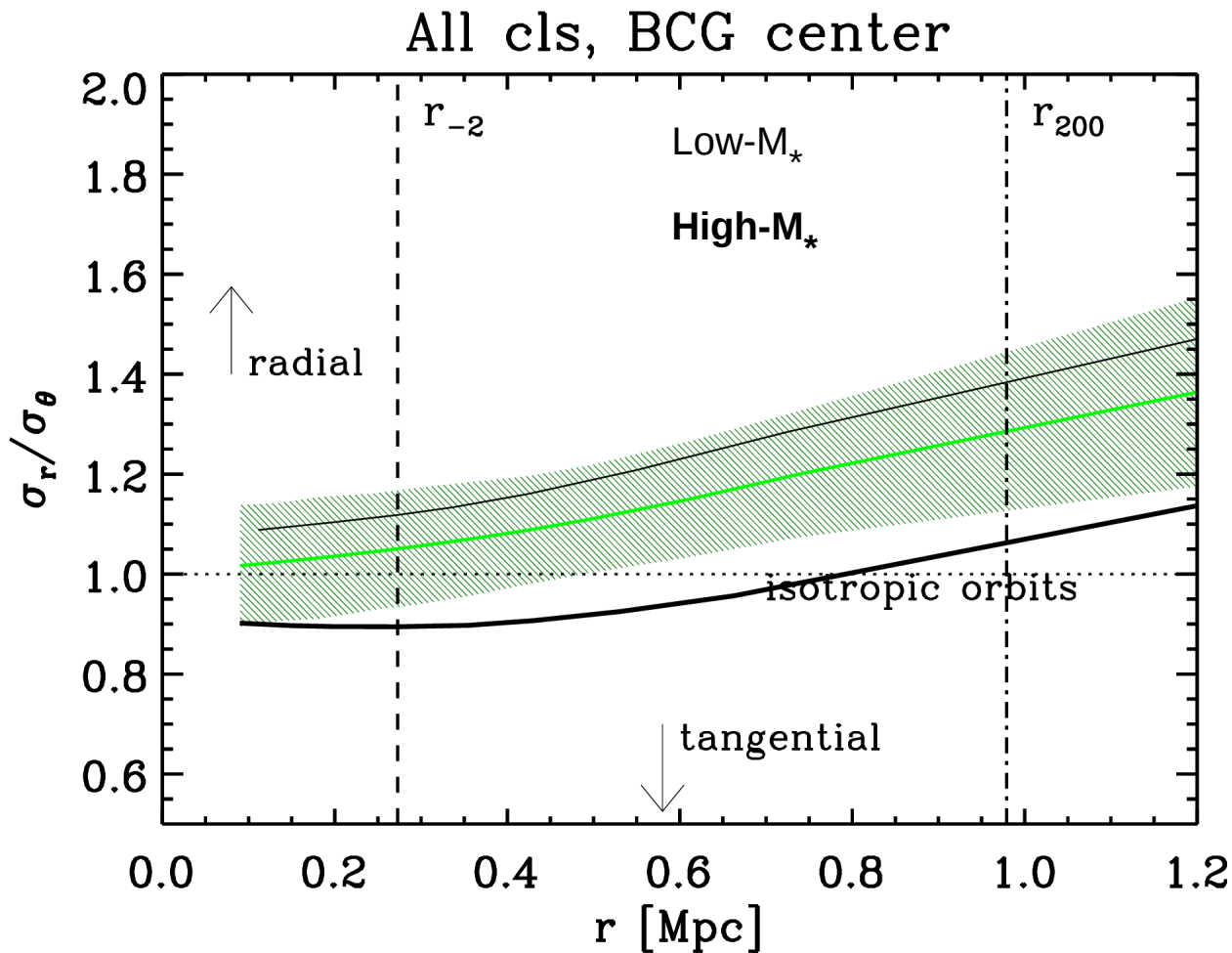
Star Forming:
no orbital evolution

Quiescent:
*orbital isotropization
beyond $\approx 0.5 r_{200}$*

Jeans inversion: velocity anisotropy

High- M_* vs. Low- M_* galaxies (with $\log M_* \geq 9.0$):

no significant difference, **but stronger than between Q and SF**



$$\beta(r) = 1 - \frac{\sigma_\theta^2(r)}{\sigma_r^2(r)}$$

Orbital difference
more related to
stellar mass than
to star-formation
activity

Summary (1/2)

Mass profile, $M(r)$:

- Highest- z cluster $M(r)$ determination so far
- Statistics is not good enough to discriminate among different $M(r)$ models
- Mass concentration significantly higher than predicted from simulations

In better agreement with De Boni+13 hydro simulations than Bhattacharya+13 DM-only simulations; this suggests the discrepancy might be related to baryonic physics not correctly accounted for in the simulations.



Summary (2/2)

Velocity anisotropy profile (orbits), $\beta(r)$:

- Highest- z cluster $\beta(r)$ determination so far
- Orbits change from slightly tangential near the center to slightly radial outside
- *More radial orbits for galaxies in more massive clusters*
- *Moderate evolution with z (more isotropic at low- z)*
- *Galaxies of lower stellar mass on more radial orbits*

Lacking significant statistical evidence

In agreement with predictions from numerical simulations

