Resource Allocation for Cellular-based Inter-Vehicle Communications in Autonomous Multiplatoons

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Abstract—As commuter population grows in megacities everywhere, traffic congestion is becoming a severe impediment to human mobility, leading to long travel delays and large economic cost on a global scale. Platooning is a promising intelligent transportation framework that can improve road capacity, on-road safety, and fuel efficiency. Furthermore, enabling inter-vehicle communications within a platoon and among platoons (in a multiplatoon) can potentially enhance platoon control by keeping constant inter-vehicle and inter-platoon distances. However, an efficient resource allocation (RA) approach is required for the timely and successful delivery of inter-vehicle information within multiplatoons. In this paper, subchannel allocation scheme and power control mechanism are proposed for LTE-based inter-vehicle communications in a multiplatooning scenario. We combine the evolved multimedia broadcast multicast services (eMBMS) and device-to-device (D2D) multicast communications to enable intra- and inter-platoon communications such that a desired trade-off between the required cellular resources and the imposed communication delay can be achieved. Numerical results show that the proposed approaches outperform a D2D-unicast based RA scheme in terms of transmission delay, especially in a multiplatoon scenario with a large number of vehicles.

Index Terms—Multiplatooning; Resource allocation; D2D communication; Cellular network; Autonomous vehicle.

I. INTRODUCTION

The fast growth of metropolitan areas has caused an increasing influx of vehicular traffic to and from big cities. As a result, urban roads and highways are plagued by traffic congestions and road crashes, resulting in serious socio-economic problems. Platooning has been identified as a promising vehicle traffic management strategy to reduce traffic congestions and increase road traffic capacity [1]–[3]. In platooning, autonomous/semi-autonomous vehicles on the same lane are grouped into a platoon \(^1\), such that each vehicle moves at the same speed and maintains a constant small inter-vehicle distance from a head\(^2\). Platooning not only can reduce traffic congestion but also can improve the driving safety of autonomous vehicles and reduce fuel consumption and exhaust emissions [7]. Although the idea of platooning dates back to the 1960s [8], the popularization of autonomous vehicles (e.g., the Google’s driveless car [9]) and the mature advanced traffic management system (ATMS) introduce new prospects for platooning. They have motivated the establishment of several national and international projects dedicated to the research and development (R&D) in platooning, including both state-funded pilot deployment projects [10], [11] and privately-funded projects by auto-mobile manufacturers [5], [12].

Despite the potential benefits of platooning, controlling the platoon (i.e., controlling the speed and acceleration of the vehicles in the platoon) to maintain a constant speed and inter-vehicle spacing within the platoon is a very challenging task, especially in highly dynamic highway scenarios [13], [14]. The main challenge in platoon control is to maintain string stability, i.e., ensure that the inter-vehicle spacing error does not amplify upstream from vehicle to vehicle within the platoon [15]. The inter-vehicle spacing error amplifies significantly when the number of vehicles increases in the platoon [15], which result in maintaining string stability becomes more challenging and, therefore only small number of vehicles are allowed in a platoon [5]. A multiplatoon, i.e., a chain of platoons that follow one-another, is considered when the number of vehicles on the road is large [6], [16]. Each platoon is led by a leader vehicle, enabling a lower management complexity and a higher road traffic capacity [6], [17]. In a multiplatoon, both intra- and inter-platoon control are required. Maintaining the string stability in a multiplatoon becomes more challenging as the inter-vehicle spacing error propagates among vehicles and across platoons. Enabling the prompt exchange of vehicle information (velocity, acceleration, deceleration and/or leave/join platoon information) within a multiplatoon through wireless communications is a promising approach to assist platoon control in maintaining string stability [2], [5], [18]–[20]. Sharing the leader and preceding vehicles’ velocity and acceleration information is a necessary condition for intra-platoon control [18]. Furthermore, when a vehicle leaves/enters a platoon, sending a message to alert its following vehicles in the multiplatoon can allow simultaneous reactions, thus preventing an increase in spacing error and enhancing platoon control [2].

There are two potential technologies that can enable inter-vehicle communications: dedicated short range communications (DSRC) and cellular network technologies [21]. The DSRC technology uses the IEEE 802.11p amendment of...
the legacy WiFi standard. Due to its low cost, the DSRC technology has been proposed for platoon communications in both academia ([2], [18]–[20], [22]) and industry [5]. However, for vehicles that are within different and far platoons, more communication hops are needed when DSRC technology is applied. Recently, much attention has been paid to the feasibility of utilizing the cellular technology for enabling inter-vehicle communications [23]–[25]. Cellular networks provide an off-the-shelf potential solution for inter-vehicle communications, which can make use of a high capacity, large cell coverage range, and widely deployed infrastructure [21]. Furthermore, there is more appetite from auto-mobile industry to deploy a mature technology, such as cellular networks, which eases the implementation and accelerates the deployment of connected vehicle services in such lucrative and competitive global market [21]. The 3rd generation partnership project (3GPP) group has recently established a new working item specifically to study the feasibility of LTE support for inter-vehicle communications and to investigate enhancements to existing cellular services, e.g., evolved multimedia broadcast multicast services (eMBMS) and device-to-device (D2D) communications, to enable reliable inter-vehicle communications [26].

In a multiplatoon, the information required for platoon control includes not only that in a basic safety message, such as velocity and acceleration, but also platoon-specific information, such as join/leave the platoon and platoon membership information. Therefore, multiplatooning communications of platoon-specific information can benefit from wide-range and low-latency multicast/broadcast LTE services. On the other hand, preceding vehicle’s velocity and acceleration information is needed only by its following vehicle and can, therefore, be shared via D2D communications. With D2D communications, vehicles communicate directly with each other over the D2D links while remaining under the control of the Evolved Node B (eNB) [27]. The transmit power of the D2D link can be adjusted according to the distance between the two vehicles. As a result, the same cellular radio resources (allocated subchannels) can be reused by different D2D links, increasing the spectral efficiency [28]. However, the higher the spatial reuse of the allocated subchannels, the higher the interference among concurrent D2D links. This trade-off calls for a resource allocation (RA) method for efficient multiplatooning communications while minimizing the burden of multiplatoon data traffic on the cellular network, such that it can accommodate the existing data traffic load from its legacy cellular users.

In this paper, we study how to efficiently combine the eMBMS and D2D communications to support multiplatooning of autonomous vehicles. Considering the potential data traffic overload in the cellular network and the requirement for communication delay in a multiplatoon scenario [2], we present efficient RA approaches for LTE-based inter-vehicle communications in a multiplatooning scenario, to balance the trade-off between the needed cellular resources and the communication delay. The main contributions of this paper are summarized as follows:

1) Using eMBMS and D2D communications, the communication models required for sharing vehicle and platoon information within the multiplatoon are proposed to reduce the number of required transmission hops;
2) Leveraging the trade-off between the number of required subchannels and the interference of concurrent D2D links, subchannel allocation scheme is proposed to increase the amount of spatial reuse of cellular radio resources while maintaining low interference;
3) Power control scheme is presented to guarantee the transmission rate of each D2D link while minimizing the transmission power of each vehicle.

The rest of this paper is organized as follows. Firstly, the multiplatooning scenario, communication models and channel model under consideration are described in Section II. Section III presents the subchannel allocation scheme for the communication links in the considered multiplatoon. Power control for each vehicle is designed in Section IV. Then, the multiplatoon communication performance in terms of transmission rate and communication delay is analyzed in Section V. Section VI is devoted to numerical results of the proposed subchannel allocation and power control schemes. Finally, in Section VII, we conclude this work and highlight our future research.

II. SYSTEM MODEL

This section describes the multiplatooning scenario, the proposed communication models, and the channel model.

A. Multiplatooning

Consider a multiplatoon on one of highway lanes located within the coverage area of an eNB, as illustrated in Figure 1. The eNB is positioned with distance $D_o$ from the middle point of the highway segment, which is defined as the origin of three-dimensional coordinates, $O$. The origin point divides the highway segment to two halves, where the length of each half is defined by $D_o$ (i.e., the length of the highway segment within the coverage area of the eNB is $2D_o$). Let $R$ denote the communication range of the eNB in meters and $D_e$ the height of the eNB. Therefore, the position of the top point on the eNB, point $A$, has the coordinates $(0, D_o, D_e)$. The multiplatoon under consideration is composed of $n$ equal-sized connected platoons, traveling on the same lane in a straight multi-lane highway. Let $m$ denote the platoon size in terms of the number of vehicles in the platoon. The $n$ connected platoons in the multiplatoon are labeled with platoon IDs $P(1), P(2), \ldots, P(n-1), P(n)$, where $P(1)$ is the leading platoon and $P(n)$ is the last following platoon. A vehicle in the multiplatoon can be either a leader vehicle or a member vehicle. A leader vehicle is the first vehicle in a platoon which is responsible of

a) forming and managing the platoon with the help of ATMS, such as controlling the number of vehicles in its platoon;
b) collecting information from and transmitting information to its member vehicles;
c) relaying information to or from the eNB.

A member vehicle, on the other hand, is a non-leader vehicle within the platoon. Vehicles within platoons follow a specified
driving strategy [17]. Vehicles not belonging to any platoon are referred to as free vehicles, and are regarded as candidates for joining the multiplatoon.

Let $V_i^{(j)}$ denote the vehicle ID of the $i$th vehicle in the platoon $P_i^{(j)}$, for $1 \leq i \leq m$ and $1 \leq j \leq n$. That is, $V_i^{(j)}$ is the ID of the leader vehicle in platoon $P_i^{(j)}$ for $1 \leq j \leq n$. Note that, the ATMS has the multiplatoon’s membership information, i.e., platoon ID and vehicle ID, collected during the platoon formation period. The position of vehicle $V_i^{(j)}$ is defined as the middle point on vehicle with coordinates $(x_i^{(j)}, 0, 0)$, where $-D_a \leq x_i^{(j)} \leq D_a$. All vehicles in the multiplatoon are assumed to be identical autonomous vehicles. Let $D_v$ be the vehicle’s distance headway, which is the distance between the middle points on two consecutive vehicles on the same lane. Let $D_p$ be the inter-platoon spacing defined as the distance between the middle points on the leader vehicle in a platoon and the last following vehicle in the preceding platoons. We assume that the position of a vehicle is the same as the position of its transceiver, and the eNB’s transceiver is located at point A.

B. Communication model

In a multiplatoon, vehicles share two types of information: velocity and acceleration (VaA), and braking and leaving (BaL) information.

a) VaA information: When the constant-spacing policy is used [18], VaA information from the leader and member vehicles needs to be shared to guarantee the string stability of each platoon. In a platoon, the leader vehicle shares its VaA information with all member vehicles, and each member vehicle shares its VaA information only with its following vehicle. For example, in platoon $P_i^{(j)}$, $V_i^{(j)}$ shares its VaA information with vehicles $\{V_1^{(j)}, V_2^{(j)}, \ldots, V_i^{(j)}, \ldots, V_m^{(j)}\}$, while $V_i^{(j)}$ shares its VaA information with vehicle $V_{i+1}^{(j)}$, $\forall 2 \leq i < m$.

b) BaL information: Platoon control and road safety can be enhanced if a vehicle shares its BaL information with its following vehicles in the multiplatoon [2].

The eNB is utilized to multicast leader vehicle’s VaA information within one platoon or relay BaL information among platoons, while only D2D unicast communications are utilized for sharing member vehicle’s VaA information. This can be explained as follows:

a) When only LTE unicast transmissions are utilized, every member vehicle needs to communicate with the eNB directly, thus limiting the spatial reuse of the orthogonal subchannels within a multiplatoon;

b) For short range communications, such as that required within a platoon, D2D communications can improve the utilization of the cellular radio resources due to spatial reuse within the multiplatoon [29];

c) The eNB can be utilized to relay information among different platoons, thus reducing the number of required transmission hops for both VaA and BaL information.

We refer to a direct transmission between two nodes (vehicle or eNB) as one-hop transmission. A vehicle shares its BaL information with vehicles in the following platoons by transmitting it to the leader vehicle and the eNB first, which then relay the BaL information to the vehicles in the following platoons. Consider the transmission of BaL information of vehicle $V_i^{(j)}$ to vehicles in platoon $P_{i+1}^{(j+1)}$ ($1 \leq j < n$). The transmission includes the following steps:

a) $V_i^{(j)}$ transmits its BaL information to $V_{i+1}^{(j)}$ via D2D communications;

b) $V_{i+1}^{(j)}$ delivers this BaL information to the eNB using LTE unicast communication or D2D multicast communication;

c) The eNB delivers this BaL information to $V_{i'}^{(j')}$, $\forall 1 \leq i' \leq m$ and $1 \leq j' \leq n$, using eMBMS, or delivers this BaL information to $V_{i+1}^{(j')}$, $\forall j < j' \leq n$, using LTE-unicast first, which is then relayed by every leader vehicle $V_{i}^{(j')}$.
$j < j' \leq n$, to every member vehicle $V_{i''}^{(j')}$, $\forall 1 < i'' \leq m$, via D2D multicast communications.

In addition to relaying the BaL information to the eNB, a leader vehicle also needs to share its VaA information with all member vehicles in the same platoon. Two communication models are established for the eNB and the leader vehicle to reduce the number of required transmission hops for transmitting vehicle’s VaA and BaL information, as shown in Figure 2 (a) and (b). The first model is an eMBMS based model, where the eMBMS technology is used by the eNB to multicast aggregated information to member vehicles as illustrated in Figure 2(a) [30]. The aggregated information received by member vehicles from the eNB includes VaA information of the leader vehicle and the BaL information of vehicles in other platoons. We assume that the member vehicles have already subscribed to the multicast service during the platoon formation, and do not consider latency and control signaling overhead associated with the join and leave procedures of creating a multicast group in the eMBMS service3. The second model is D2D-multicast based model as illustrated in Figure 2(b). Each leader vehicle shares information with the eNB and its member vehicles via D2D multicast communications. Upon receiving the BaL information of vehicles in other platoons from the eNB, the leader vehicle aggregates the BaL information with its VaA information and multicasts the aggregated information to the member vehicles.

To share the information of a member vehicle, only D2D communication is applied since a member vehicle needs to transmit its VaA and BaL information only to the following vehicle and its leader vehicle, respectively. Figure 2(c) illustrates the proposed communication model within platoon $P^{(j)}$ for each member vehicle to share its VaA information with the following vehicle (the blue solid arrows) and its BaL information with the leader vehicle (dashed arrows). Within a platoon $P^{(j)}$, only member vehicles $V_{2}^{(j)}$, $V_{3}^{(j)}$, ..., $V_{k}^{(j)}$ communicate directly with the leader vehicle, the rest of member vehicles communicate in a multi-hop fashion. We refer to vehicle $V_{k}^{(j)}$ as the platoon’s boundary vehicle and indicates the boundary between the vehicles communicating with the leader vehicle in multi-hops and the vehicles communicating with the leader vehicle directly. The calculation of the value $k$ is discussed in details in Section III.

The wireless communication links established among vehicles share a subchannel set, $\mathcal{F} = \{1, 2, ..., F\}$ with $F = |\mathcal{F}|$ orthogonal subchannels. The $F$ subchannels are assigned to these communication links by the eNB using a standard packet scheduling procedure. Full-duplex (FD) communications are applied in each vehicle and the eNB to enable simultaneous multiple transmissions and/or receptions over the same or different subchannels [29], [32]. The eNB assigns the subchannels based on the received BaL information and the membership information, and then sends the radio resource control (RRC) connection setup to each communication link on the physical downlink control channels [33]. To meet communication delay requirements, subchannel allocation scheme and power control scheme are proposed in Sections III and IV, respectively.

C. Channel model

Consider a large scale fading channel model [34]. Since the eNB and vehicles can have different antennas types and different line-of-sight (LOS) components of radio propagation may be experienced at the receivers [28], two types of path-loss exponents are considered. Let $\alpha$ and $\beta$ denote the path-loss exponents for a link between the eNB and a vehicle and for a D2D link, respectively. Let $\mathcal{H}_{e,i}$ denote the channel gain for a link between the eNB and vehicle $i$, and $\mathcal{H}_{g,w}$ denote the channel gain of the D2D link between vehicle $g$ and vehicle $w$. The channel gains are given by

$$\mathcal{H}_{e,i} \triangleq |h_0|^2 \cdot (d_{e,i})^{-\alpha}$$  (1)

and

$$\mathcal{H}_{g,w} \triangleq |h_0|^2 \cdot (d_{g,w})^{-\beta}$$  (2)
where $d_{v_g}$ is the distance between the eNB and vehicle $i$, $d_{g,w}$ is the distance between vehicle $g$ and vehicle $w$, and $h_0$ is the complex Rayleigh fading channel coefficient. All channel gains under consideration are assumed to be reciprocal \cite{34}, i.e., $h_{e,i} = h_{i,e}$ and $h_{g,w} = h_{w,g}$.

### III. Subchannel Allocation

For the communication models discussed in Section II, the end-to-end delay of a packet carrying member vehicle’s VaA information is the delay of an one-hop D2D unicast communication\(^4\). On the other hand, the end-to-end delay of a packet carrying the leader vehicle’s VaA information is the delay of two-hop communication in the eMBMS based model and that of one-hop communication in the D2D-multicast based model. For a packet carrying the BaL information, the end-to-end delay is the delay to transmit this packet from the source to the destination in the multiplatoon and is proportional to the number of transmission hops for a given transmission rate. Since a stable transmission rate depends on the signal-to-interference-and-noise-ratio (SINR) \cite{35}, we have the following two objectives:

- a) reducing the number of transmission hops for transmitting BaL information;
- b) reducing interference caused by subchannel reuse and minimizing the transmission power of each vehicle while guaranteeing the received signal power and SINR at each receiver.

Figure 2(c) indicates that the maximum number of transmission hops for the BaL information occurs in the last vehicle of platoon $P^{(j)}$, and the value of the maximum transmission hops depends on the position of its boundary vehicle, $V_k^{(j)}$. Thus, to achieve the first objective, $k$ is restricted to the second half of the $m - 1$ member vehicles in each platoon, i.e., $\left\lfloor \frac{m+2}{2} \right\rfloor \leq k \leq m$. Then, combining subchannel allocation and power control schemes to achieve the second objective. It should be noted that, in proposed subchannel allocation scheme, the global view of the network (with all the communication links) is considered while the link-local view is considered in our power control approach.

#### A. Subchannel allocation for leader vehicles

Let $l_{g,w}^{(j)}$, $l_{i,e}^{(j)}$, $l_{c,1}^{(j)}$ denote the communication links from $V_g^{(j)}$ to $V_w^{(j)}$, from $V_{i,e}^{(j)}$ to eNB, and from eNB to $V_{c,1}^{(j)}$, respectively, where $1 \leq j \leq n$ and $1 < g, w \leq m$. For the two communication models described in Subsection II-B, the leader vehicles in the multiplatoon apply the following subchannel allocation schemes:

1) **eMBMS based model**: The leader vehicle $V_{1,c,1}^{(j)}$ communicates with the eNB in one subchannel, and the eNB multicasts the aggregated VaA and BaL information to $V_k^{(j)}$ ($1 \leq i \leq m$) in another subchannel.

2) **D2D-multicast based model**: The communication links, established when the eNB unicasts a packet to a leader vehicle or when this leader vehicle multicasts a packet to its member vehicles and the eNB (i.e., links $l_{i,e}^{(j)}$, $l_{i,c,1}^{(j)}$ and $l_{c,1}^{(j)}$, where $1 < i \leq m$), use only one subchannel. Since each leader vehicle multicasts a packet to the eNB and its member vehicles, and the packet transmitted in $l_{i,c,1}^{(j)}$ ($1 < i \leq m$) is the same as that in $l_{i,c,1}^{(j)}$. Therefore, there is no co-channel interference between these two communication links.

To reduce co-channel interference experienced at each vehicle, the subchannels occupied by communication links in the eMBMS based model and D2D-multicast based model cannot be reused by any other links. Thus, for $n$ leader vehicles, $2n$ and $n$ subchannels are needed for the eMBMS based and the D2D-multicast based models, respectively.

#### B. Subchannel allocation for member vehicles

Denote $F_1$ as the number of subchannels that can be reused by the $n \times (2m - 3)$ intra-platoon communication links shown in Figure 2(c). Due to the inter-platoon spacing, $D_p$, there is at least $D_p$ spatial separation between two intra-platoon communication links in one platoon and in another platoon. Thus, the subchannel allocated to an intra-platoon communication link in a platoon can be reused in other platoons. Scheme 1 is designed for allocating the minimum number of $F_1$ subchannels among the $2m - 3$ intra-platoon communication links in a platoon, and scheme 2 is designed for allocating these $F_1$ subchannels in the multiplatoon. Let $f_{g,w}^{(j)}$ denote the subchannel that is allocated to link $l_{g,w}^{(j)}$ where $1 \leq g, w \leq m$ and $1 \leq j \leq n$.

**Scheme 1 intra-platoon subchannel allocation**: For the intra-platoon communication links in platoon $P^{(j)}$, the subchannel allocation is given by

$$f_{i-1,i}^{(j)} = \begin{cases} f_{i-1,i}^{(j)} & \text{if } 2 < i \leq k \\ f_{i,i-1}^{(j)} & \text{if } k < i \leq m. \end{cases} \quad (3)$$

From (3), links $l_{i-1,i}^{(j)}$ and $l_{i,i-1}^{(j)}$ use the same subchannel when $2 < i \leq k$; and links $l_{i-1,i}^{(j)}$ and $l_{i,i-1}^{(j)}$ use the same subchannel when $k < i \leq m$. This design can be explained as follows. First, the self-interference, experienced at a vehicle resulting from its transmission to its reception over the same subchannel, can be sufficiently suppressed by using existing self-interference cancellation methods, such as the distributed linear convolutional space-time coding (DLC-STC) scheme proposed in \cite{32}. The co-channel interference (due to subchannel reuse by other links) depends on the transmission power of and the distance to the interfering source. Reducing co-channel interference experienced at a receiver always affects the transmission in its interfering source. Thus, in addition to scheme 1, the following choice can be considered: when $2 < i \leq k$, $l_{i-1,i}^{(j)}$ and $l_{i,i+1}^{(j)}$ use one subchannel, and $l_{i+1}^{(j)}$ uses another subchannel; and when $k < i < m$, $l_{i-1,i}^{(j)}$ and $l_{i,i+1}^{(j)}$ use one subchannel while $l_{i+1,i}^{(j)}$ and $l_{i,i-1}^{(j)}$ use another subchannel. However, it is clear that the number of required subchannels in scheme 1 is fewer than that in this choice. Furthermore, due to interference experienced at $V_{i+1}^{(j)}$ generated by $l_{i-1,i}^{(j)}$ ($2 \leq i < m$) and interference experienced at $V_{i-1}^{(j)}$ generated by $l_{i+1,i}^{(j)}$ ($k \leq i < m$), the total interference experienced at vehicles in this choice is larger than that in scheme 1.

\(^{4}\)In this work, the queuing and access delays are neglected, since the cellular resource is assumed to be allocated during the multiplatoon formation state.
Suppose that the DLC-STC scheme is used in each transmitter, and the self-interference is neglected [36]. Based on scheme 1, we can get the subchannel allocation results for member vehicles in platoon $P^{(j+1)}$, i.e., $f_{g,w}^{(j+1)}$, where $1 \leq g, w \leq m$. Then, scheme 2 can be described as follows.

**Scheme 2 inter-platoon subchannel allocation**: The subchannels allocated for the intra-platoon communication links in platoon $P^{(j)}$ are related to those in platoon $P^{(j+1)}$ according to

$$f_{2,1}^{(j)} = f_{k-1,k}^{(j+1)}$$

(4)

and

$$f_{i-1,i}^{(j)} = \begin{cases} f_{(k+2)-i,1}^{(j+1)}, & \text{if } 2 < i \leq 2k - m \\ f_{i+(m-k),i+(m-k)-1}^{(j+1)}, & \text{if } 2k - m < i \leq k \\ f_{(m+2)-i,1}^{(j+1)}, & \text{if } k < i \leq m. \end{cases}$$

(5)

Based on scheme 2, $l_{i-1,i}^{(j)}$ and $l_{k-1,k}^{(j+1)}$ use one subchannel when $i = 2$; $l_{i-1,i}^{(j+1)}$ and $l_{(k+2)-i,1}^{(j+1)}$ use one subchannel when $2 < i \leq 2k - m$; $l_{i-1,i}^{(j+1)}$ and $l_{i+(m-k),i+(m-k)-1}^{(j+1)}$ use one subchannel when $2k - m < i \leq k$; and $l_{i-1,i}^{(j+1)}$ and $l_{(m+2)-i,1}^{(j+1)}$ use one subchannel when $k < i \leq m$. Scheme 2 can be explained by the following theorem, proved in Appendix A.

**Theorem 1**: In a random platoon, the transmission power of an intra-platoon communication link, required to guarantee an SINR threshold $\lambda$ at its receiver, is proportional to the distance of this link, i.e.,

$$p_1 - p_0 = \frac{\lambda I_1}{|h_0|^2} (d_{g,w})^\beta$$

(6)

where $p_0$ is the transmission power of vehicle $g$ in the presence of a background additive white Gaussian noise (AWGN), $p_1$ is the transmission power of vehicle $g$ in the presence of a background AWGN of the same power spectral density and interference $I_1$ generated by other transmissions that use the same subchannel.

Theorem 1 indicates that the power efficiency of multiplatooning communications can be improved if the interference experienced at a vehicle (which is the receiver of multiple links) is largely transmitted to the transmission over the shorter link. According to scheme 1 and scheme 2, the value of $F_1$ can be reduced to $m - 1$. An example for reusing subchannels within two consecutive platoons, $P^{(j)}$ and $P^{(j+1)}$, is illustrated in Figure 3, where $m = 7$, $k = 6$, $F_1 = 6$, and the numbers on the arrows indicate the subchannel IDs of the $F_1$ subchannels. It should be noted that, when $F_1 > m - 1$, the impact of co-channel interference on the multiplatooning communication performance reduces and the designed subchannel allocation scheme can be adjusted accordingly. On the other hand, when $F_1 < m - 1$, we can combine scheme 1 and scheme 2 with the subchannel allocation scheme proposed in [28] to support multiplatooning communications.

**IV. Power Control**

To guarantee fairness among different links that share the same subchannel, a minimum received signal power threshold, $\eta$, and a minimum received SINR threshold, $\lambda$, are set for each receiver. In order to achieve a received signal power over $\eta$ and an SINR over $\lambda$ at the receiver while minimizing the transmission power, a power control scheme is proposed in this section. Taking platoons $P^{(j)}$ and $P^{(j+1)}$ as an example, the proposed power control schemes for the eNB, leader vehicles, and member vehicles are as follows.

**A. Power control for eNB**

1) **eMBMS based model**: Denote $p_{e}^{(j)}$ as the transmission power of the eNB when it multicasts a packet to the vehicles in platoon $P^{(j)}$. The received signal power and the SINR at vehicle $V_i^{(j)}$ ($1 \leq i \leq m$) are given by

$$R_{e,i}^{(j)} = p_{e}^{(j)} |h_0|^2 \left( d_{e,i}^{(j)} \right)^{-\alpha}$$

(7)

and

$$S_{e,i}^{(j)} = \frac{p_{e}^{(j)} |h_0|^2 \left( d_{e,i}^{(j)} \right)^{-\alpha}}{\sigma}$$

(8)

In (7) and (8), $\sigma$ is the value of AWGN, $d_{e,i}^{(j)}$ is the distance between point A and vehicle $V_i^{(j)}$, and $p_{e}^{(j)}$ is the transmission power of the eNB. In (7), $\lambda$ is the SINR of vehicle $V_i^{(j)},$ and $\eta$ is the SINR threshold at the receiver.

2) **D2D-multicast based model**: The eNB only unicasts packets to leader vehicle $V_1^{(j)}$ in this model. To guarantee the received signal power and the SINR at $V_1^{(j)}$, the minimum $p_{e}^{(j)}$ can be expressed as

$$p_{e}^{(j)} = \max \left\{ \eta \left( \frac{d_{e,1}^{(j)}}{|h_0|^2} \right)^\alpha, \frac{\lambda \sigma}{|h_0|^2} \right\}$$

(9)

**B. Power control for leader vehicles**

1) **eMBMS based model**: Denote $p_{1}^{(j)}$ as the transmission power of $V_1^{(j)}$. As mentioned in Subsection II-C, all channel gains are assumed to be reciprocal. Thus, based on eMBMS, the minimum $p_{1}^{(j)}$ to guarantee the received signal power and the SINR at the eNB, i.e., $p_{1}^{(j)}$, is the same as $p_{e}^{(j)}$ in the D2D-multicast based model and is given by (10).

2) **D2D-multicast based model**: As mentioned in Section III, for platoon $P^{(j)}$ ($1 \leq j \leq n$), same packets are transmitted over $l_{i,j}^{(j)}$ ($1 < i \leq m$) and $l_{i,1}^{(j)}$, and the self-interference in
each vehicle can be neglected. Thus, for vehicle \( V_i^{(j)} \) \((1 < i \leq m)\), only interference generated by the transmission in \( f_{i,1}^{(j)} \) is considered. When receiving packet from \( V_1^{(j)} \) the received signal power and SINR at \( V_i^{(j)} \) \((1 < i \leq m)\) can be expressed as

\[
R_{1,i}^{(j)} = p_{1}^{(j)} |h_0|^2 \left( d_{1,i}^{(j)} \right)^{-\beta}
\]

and

\[
S_{1,i}^{(j)} = \frac{R_{1,i}^{(j)}}{\sigma + p_{e}^{(j)} |h_0|^2 \left( d_{e,i}^{(j)} \right)^{-\alpha}}
\]

respectively, where \( p_{e}^{(j)} \) is given by (11), \( p_{1}^{(j)} \) is the transmission power of \( V_1^{(j)} \), and \( d_{1,i}^{(j)} \) is the distance between \( V_1^{(j)} \) and \( V_i^{(j)} \) and can be calculated by

\[
d_{1,i}^{(j)} = (i-1)D_v.
\]

Let \( \hat{p}_1^{(j)} \) denote the minimum transmission power of \( V_1^{(j)} \) to guarantee the signal power threshold, \( \eta \), at each member vehicle. Since \( \beta > 0 \), according to equations (12) and (14), \( \hat{p}_1^{(j)} \) is given by

\[
\hat{p}_1^{(j)} = \frac{\eta |(m-1)D_v|^\beta}{|h_0|^2}.
\]

Let \( p_{1}^{(j)} \) denote the minimum \( p_{1}^{(j)} \) to guarantee the SINR threshold, \( \lambda \), at each member vehicle. Equations (9) and (13) show that the value of \( S_{1,i}^{(j)} \) is related to \( x_{i}^{(j)} \) and is different from member vehicles when \( V_1^{(j)} \) multicasts a packet to its member vehicles with transmission power \( p_{1}^{(j)} \). For a given \( x_{i}^{(j)} \), the power control problem for leader vehicles is formulated as

\[
\min_i S_{1,i}^{(j)} = \frac{p_{1}^{(j)} |h_0|^2 \left( d_{1,i}^{(j)} \right)^{-\beta}}{\sigma + p_{e}^{(j)} |h_0|^2 \left( d_{e,i}^{(j)} \right)^{-\alpha}}
\]

subject to

\[
x_{i}^{(j)} = x_{i}^{(j)} - (i-1)D_v
\]

\[
d_{1,i}^{(j)} = (i-1)D_v
\]

\[
d_{e,i}^{(j)} = \sqrt{x_{i}^{(j)}}^2 + (D_v)^2 + (D_e)^2
\]

\[
-D_a \leq S_{i}^{(j)} \leq D_a
\]

\[
1 < i \leq m.
\]

By solving the above power control problem, the minimum \( S_{1,i}^{(j)} \) among the \( m-1 \) member vehicles can be obtained.

From the above discussion, the minimum transmission power of \( V_1^{(j)} \) to guarantee the received signal power and SINR at the eNB and member vehicles is given by

\[
p_{1}^{(j)} = \max \left\{ p_{e}^{(j)}, \hat{p}_1^{(j)} \right\}.
\]

\section{Power control for member vehicles}

Subchannels are reused among intra-platoon communication links within a single platoon and among that within multiple platoons. In platoon \( P^{(j+1)} \), scheme 1 indicates that \( l_{i-1,i}^{(j+1)} \) and \( l_{i-1,i}^{(j+1)} \) use subchannel \( f_{i}^{(j+1)} \) when \( k < i \leq m \); and \( l_{i-1,i}^{(j+1)} \) and \( f_{i}^{(j+1)} \) reuse subchannel \( f_{j}^{(j+1)} \) when \( 1 < i \leq k \). Among the intra-platoon communication links in platoon \( P^{(j)} \), \( l_{i-1,i}^{(j)} \) \((1 < i \leq k)\) is a link between two consecutive vehicles with link distance \( D_v \), which is small compared to that of \( l_{i-1,i}^{(j)} \).

Hence, the transmission power of the transmitter in \( l_{i-1,i}^{(j)} \) \((1 < i \leq k)\) is relatively small. Therefore, for the transmissions in intra-platoon communication links in \( P^{(j)} \) which reuse \( f_{j}^{(j+1)} \) \((1 < i \leq k)\), only interference generated by \( l_{i-1,i}^{(j)} \) is considered.

According to scheme 2, the value of \( k \) impacts the subchannel allocation results among intra-platoon communication links in platoons \( P^{(j)} \) and \( P^{(j+1)} \). In (4) and (5), links \( l_{i-1,i}^{(j+1)} \) and \( l_{i-1,i}^{(j+1)} \) are between two consecutive vehicles when \( 2k - m < i \leq k \) and \( k < i \leq m \). Furthermore, the transmission power in these two links are small and the proposed subchannel allocation scheme avoids allocating a subchannel to two adjacent communication links. Thus, interference experienced at \( V_1^{(j)} \) generated by the transmission in \( l_{i-1,i}^{(j+1)} \) \((2k - m < i \leq k)\), and interference experienced at \( V_1^{(j+1)} \) generated by the transmission in \( l_{i-1,i}^{(j+1)} \) \((2k - m < i \leq k)\), which are small compared to that of other links, are ignored.
\[ (k < i \leq m), \text{are negligible. Considering the distance between} \]
\[ \text{a receiver and its interfering source, the largest interference} \]
\[ \text{experienced at } V_{(j+1)}^{2k-m-1} \text{ is generated by the transmission} \]
\[ \text{in } V_{m-k+2}^{(j+1)} \text{ when } V_{m-k+2}^{(j+1)} \text{ transmits a packet to } V_{1}^{(j+1)} \text{ (2} \]
\[ \leq i < 2k-m). \text{This is also the largest interference experienced} \]
\[ \text{at a platoon, which is generated by its preceding platoon.} \]

\[ \text{From the above discussion, a large } k \text{ means a short distance} \]
\[ \text{between } V_{2k-m}^{(j)} \text{ and } V_{1}^{(j+1)}, \text{i.e., a small} \]
\[ \text{2}(m-k)D_v + D_p, \text{which indicates large interference experienced at} \]
\[ V_{V_{1}^{(j+1)}}^{m-k+2} \text{, that is generated by the transmission in } V_{2k-m}^{(j+1)}. \text{Thus,} \]
\[ \text{resulting in high transmission powers of } V_{V_{1}^{(j+1)}}^{m-k+2} \text{ and } V_{2k-m}^{(j)} \text{ to} \]
\[ \text{guarantee the signal power and SINR thresholds at their} \]
\[ \text{receivers. However, a large } k \text{ can reduce the number of} \]
\[ \text{member vehicles communicating with the leader vehicle in} \]
\[ \text{multi-hops, and therefore, reduce the delay for transmitting the} \]
\[ \text{BaL information of these member vehicles. Thus, the} \]
\[ \text{power control problem for member vehicles is formulated} \]
\[ \text{to minimize the transmission powers of } V_{V_{1}^{(j+1)}}^{m-k+2} \text{ and } V_{2k-m}^{(j)} \text{ while} \]
\[ \text{guaranteeing the received signal powers at } V_{V_{1}^{(j+1)}}^{m-k+2} \text{ and} \]
\[ V_{2k-m}^{(j)} \text{ over the threshold } \eta, \text{and the received SINR at } V_{V_{1}^{(j+1)}}^{m-k+2} \text{ over} \]
\[ \text{the threshold } \lambda. \text{The power control problem for member} \]
\[ \text{vehicles can be represented as follows,} \]
\[ \min_k \{ p_{2k-m}^{(j)} + p_{m-k+2}^{(j+1)} \} \]
\[ \text{subject to} \]
\[ p_{2k-m}^{(j)} |h_0|^2 [(2k-m-1)D_v]^{-\beta} \geq \eta \]
\[ p_{m-k+2}^{(j+1)} |h_0|^2 [(m-k+1)D_v]^{-\beta} \geq \eta \]
\[ p_{m-k+2}^{(j+1)} |h_0|^2 [(m-k+1)D_v]^{-\beta} \geq \lambda \]
\[ \frac{\sigma + p_{2k-m}^{(j)} |h_0|^2 [2(m-k)D_v + D_p]^{-\beta}}{m + 2} \leq k \leq m \]
\[ \text{where (18a) and (18b) guarantee the signal power thresholds} \]
\[ \text{at } V_{V_{1}^{(j+1)}}^{m-k+2} \text{ and } V_{2k-m}^{(j)} \text{, (18c) guarantees the SINR threshold at} \]
\[ V_{V_{1}^{(j+1)}}^{m-k+2} \text{, and (18d) indicates that fewer than half of member} \]
\[ \text{vehicles communicate with the leader vehicle in multi-hops.} \]
\[ \text{The optimal } k, k_{opt}, \text{can be obtained by solving the above} \]
\[ \text{power control problem, which minimizes the sum of the} \]
\[ \text{transmission powers of } V_{V_{1}^{(j+1)}}^{m-k+2} \text{ and } V_{2k-m}^{(j)}. \]

\[ \text{As proved in Appendix B, the above power control problem} \]
\[ \text{can be simplified according to the following theorem.} \]
\[ \text{Theorem 2: The power control problem for member} \]
\[ \text{vehicles can be simplified to the following} \]
\[ \min_{k^*,k'} \{ \Lambda(k^*), \Omega(k') \} \]
\[ \text{subject to} \]
\[ \Lambda(k^*) = \Gamma_1(k^*) + \Gamma_2(k^*) \]
\[ \Omega(k') = \Gamma_1(k') [1 + \Gamma_3(k')] + \Gamma_4(k') \]
\[ \Gamma_2(k') \geq \Gamma_1(k') \Gamma_3(k') + \Gamma_4(k') \]
\[ \Gamma_2(k') < \Gamma_1(k') \Gamma_3(k') + \Gamma_4(k') \]
\[ \frac{m + 2}{2} \leq k^*, k' \leq m \]
\[ \text{where } \Gamma_1(k), \Gamma_2(k), \Gamma_3(k), \text{and } \Gamma_4(k) \text{ are} \]
\[ \Gamma_1(k) = \frac{\eta}{|h_0|^2 [(2k-m-1)D_v]^{-\beta}} \]
\[ \Gamma_2(k) = \frac{\eta}{|h_0|^2 [(m-k+1)D_v]^{-\beta}} \]
\[ \Gamma_3(k) = \frac{\lambda [(m-k)D_v + D_p]^{-\beta}}{[(m-k+1)D_v]^{-\beta}} \]
\[ \Gamma_4(k) = \frac{|h_0|^2 [(m-k+1)D_v]^{-\beta}}{\sigma \lambda} \]

V. Multiplatooning Communication Analysis

In Sections III and IV, we have proposed subchannel allocation and power control schemes for vehicles in a multiplatoon, which can guarantee the received signal power and SINR of each communication link. In this section, the multiplatooning communication performance, in terms of the transmission rate and transmission delay, is analyzed.

1) Transmission rate: Section IV shows that the received SINR in each communication link is guaranteed to reach the SINR threshold. Thus, the achievable transmission rate in a communication link, denoted by \( r \), satisfies
\[ r \geq W \log_2 (1 + \lambda) \]
(21)

where \( W \) is the subchannel bandwidth.

2) Transmission delay: Define \( E[L] \) as the average size of the packet carrying the VaA or BaL information. As mentioned in Subsection II-B, each leader vehicle needs to share its VaA information with all member vehicles in the same platoon and each member vehicle needs to share its VaA information with its following member vehicle. According to the communication model and the proposed subchannel allocation and power control schemes, the end-to-end delay for a packet carrying the member vehicle’s VaA information is the delay of a D2D link and can be expressed as
\[ T_{V_{AvA}} = \frac{E[L]}{r} \leq \frac{2E[L]}{W \cdot \log_2 (1 + \lambda)} \]
(22)

\[ (i) \text{In the eMBMS based model: As illustrated in Figure 2(a), the leader vehicle unicasts its VaA information to the eNB first, then the eNB multicasts this information using eMBMS to the member vehicles in the same platoon. Thus, the end-to-end delay for a packet carrying the leader vehicle’s VaA information, } \]
\[ T_{V_{AvA}} \]
\[ \text{is the delay of the two-hop communication, which can be expressed as} \]
\[ T_{V_{AvA}} = 2 \frac{E[L]}{r} \leq \frac{4E[L]}{W \cdot \log_2 (1 + \lambda)} \]
(23)

When a member vehicle in a platoon shares its BaL information with the member vehicles in other platoons, the BaL information needs to be relayed by the leader vehicle and the eNB. Thus, when \( k = k_{opt} \), the end-to-end delay for a packet carrying the BaL information in the eMBMS based model is proportional to the number of transmission hops and can be expressed as
\[ 2 \frac{E[L]}{r} \leq T_{BaL_1} \leq (m - k_{opt} + 3) \frac{E[L]}{r} \]
(24)
where \( T_{Ba,L_1} = \frac{2E[L]}{r} \) when vehicle \( V_1^{(n)} \) shares its BaL information with the member vehicles in platoon \( P^{(n)} \) and 

\[
T_{Ba,L_1} = (m - k_{\text{opt}} + 3) \frac{E[L]}{r} \text{ when vehicle } V_m^{(j)} \text{ shares its BaL information with the member vehicles in platoon } P^{(n)}, \quad j \leq u \leq n.
\]

(ii) In the D2D-multicast based model: As illustrated in Figure 2(b), a leader vehicle multicasts its VaA information aggregated with the BaL information from other member vehicles directly. Thus, based on a D2D multicast communication, the end-to-end delay for a packet carrying the leader vehicle’s VaA information, \( T_{V_{nA}} \), is the delay of a D2D link, same as \( T_{V_{AAM}} \). As in the eMBMS based model, when a member vehicle in a platoon shares its BaL information with member vehicles in other platoons, this BaL information needs to be relayed by the leader vehicle and the eNB. Thus, the end-to-end delay for a packet carrying BaL information in the D2D-multicast based model can be expressed as

\[
\frac{E[L]}{r} \leq T_{Ba,L_1} \leq (m - k_{\text{opt}} + 4) \frac{E[L]}{r}.
\] (25)

VI. NUMERICAL RESULTS

To demonstrate the multiplatooning communication performance with the proposed subchannel allocation and power control schemes, this section presents the numerical results for the proposed power control scheme, evaluates the end-to-end transmission delay of vehicle’s VaA/BaL information, and compares the results with the performance of a D2D-unicast based RA approach (proposed in [28]).

We consider a multiplatooning communication scenario with a set of parameters listed in Table I. For the D2D-unicast based RA approach proposed in [28], only communication links between two adjacent vehicles are considered. In addition, the communication links within the multiplatoon are divided into \( n \) individual groups, where the \( n \) groups reuse \( m \) subchannels and each group represents the communication links within the same platoon (including that from the leader vehicle to the last member vehicle in the preceding platoon). For a fair comparison, FD mode is considered at each vehicle when it shares its VaA/BaL information using the approach in [28], and links between two adjacent vehicles, i.e., \( t^{(j)}_{i,i+1} \) and \( t^{(j)}_{i+1,i} \), are allocated the same subchannel.

### Table I: System parameters values in analysis

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>( R )</td>
<td>500 m</td>
<td>( D_v )</td>
<td>50 m</td>
</tr>
<tr>
<td>( D_p )</td>
<td>100 m</td>
<td>( D_p )</td>
<td>487.34 m</td>
</tr>
<tr>
<td>( D_v )</td>
<td>8 m</td>
<td>( D_p )</td>
<td>40 m</td>
</tr>
<tr>
<td>( m )</td>
<td>20</td>
<td>( m )</td>
<td>5</td>
</tr>
<tr>
<td>( \beta )</td>
<td>24</td>
<td>( \eta )</td>
<td>3</td>
</tr>
<tr>
<td>( \lambda )</td>
<td>4</td>
<td>( \eta )</td>
<td>-100 dBm</td>
</tr>
<tr>
<td>( \sigma )</td>
<td>100 E[L]</td>
<td>( W )</td>
<td>2 MHz</td>
</tr>
</tbody>
</table>

### A. Power control results

Figure 4(a) compares the transmission powers of the eNB when it multicasts packet to \( V_1^{(j)} \) based on eMBMS and unicasts packet to \( V_1^{(j)} \) in the D2D-multicast based model.

The transmission power of the eNB can be adjusted according to the position of the leader vehicle to guarantee a received SINR threshold at each vehicle. Point \( O \) is closest to the eNB, thus, the closer the leader vehicle is to the point \( O \), i.e., the smaller the value of \( |x_1^{(j)}| \), the less transmission power the eNB needs. Furthermore, as mentioned in Section IV, the eNB in the eMBMS based model needs to guarantee the received signal power and SINR at the vehicle that is with the largest distance to the eNB in one platoon. However, in the D2D-multicast based model, the eNB only needs to guarantee the received signal power and SINR at the leader vehicle, which is with the same or shorter transmission distance compared to that in the eMBMS based model. As a result, the transmission power of the eNB in the D2D-multicast based model is less than that in the eMBMS based model when \( x_1^{(j)} \leq 77.5 \) m, as shown in Figure 4(a).

Figure 4(b) shows the transmission power of a leader vehicle when it communicates to the eNB or its member vehicles according to the eMBMS and D2D-multicast based models. Regardless of the leader vehicles position, the transmission power of the leader vehicle in the D2D-multicast based model is always larger than that in the eMBMS based model. This is because the leader vehicle needs to multicast packets to its member vehicles in the D2D-multicast based model. However, in the eMBMS mode, the transmission power of the leader vehicle increases due to the interference experienced at each member vehicle, which is generated by the transmission from the eNB to this leader vehicle. Furthermore, in the D2D-multicast based model, \( p_{1}^{(j)} \) tends to decrease first, then increase, and then decrease again. \( p_{1}^{(j)} \) decreases because when \( x_1^{(j)} < 0 \); since \( p_{1}^{(j)} \) increases with \( x_1^{(j)} \) when \( x_1^{(j)} > 0 \), \( p_{1}^{(j)} \) increases to guarantee the received SINR at \( V_1^{(j)} \). However, the distance between the last following vehicle \( V_m^{(j)} \) and the eNB increases with \( x_1^{(j)} \), resulting in interference reduction that gradually counteracts the increased \( p_{1}^{(j)} \) and eventually decreases the value of \( p_{1}^{(j)} \).

Figure 5(a) plots the transmission powers of vehicles \( V_{m-k+2}^{(j)} \) and \( V_{m-k-m}^{(j)} \), and the sum of them, i.e., \( p_{m-k+2}^{(j)} \), \( p_{m-k-m}^{(j)} \), and \( p_{m-k+2}^{(j)} + p_{m-k-m}^{(j)} \), for different \( k \) values. \( \frac{m-2}{2} \leq k \leq m \). A large \( k \) means a large distance between \( V_{2k-m}^{(j)} \) and \( V_1^{(j)} \), thus resulting in a high transmission power of \( V_{2k-m}^{(j)} \).

Since \( p_{m-k+2}^{(j)} = (m - k + 1)D_v \) decreases with \( k \), the transmission power of vehicle \( V_{m-k+2}^{(j)} \) required to guarantee the received signal power and SINR at \( V_1^{(j)} \) decreases when \( k \) increases from 11 to 15. On the other hand, the value of \( 2(m-k)D_v + D_p \) decreases with \( k \), resulting in the increasing of the interference experienced at \( V_1^{(j)} \) generated by \( V_{2k-m}^{(j)} \), and therefore, \( p_{m-k+2}^{(j)} \) increases when \( k \) increases from 15 to 18. When \( 18 \leq k \leq 20 \), \( p_{m-k+2}^{(j)} \) increases again, which can be explained by Theorem 1. The optimal \( k \) values for different platoon sizes, \( 5 \leq m \leq 20 \), are shown as in Figure 5(b).

### B. Transmission delay

In this subsection, the performance of our proposed approaches in terms of the transmission delay is compared with
that in [28]. We focus on BaL information and leader vehicle’s VaA information transmissions only, since the transmission delay for sharing member vehicle’s VaA information is the delay of a D2D communication link.

Figure 6 shows the effect of the platoon size, \( m \), on the maximum end-to-end delays for sharing VaA and BaL information, which are defined as the delay for sharing the leader vehicle’s VaA information with its member vehicles and the delay for sharing the \( m \)th member vehicle’s BaL information to the \( m \)th member vehicle in one of its following platoons. Considering \( 3 \leq m \leq 20 \), we can see that the end-to-end transmission delays of the proposed approaches are always less than that in [28], especially the one according to the D2D-multicast based model. The reasons can be summarized as follows: (i) the utilized D2D multicast and eMBMS communications in our proposed approaches reduce the number of transmission hops required for sharing the leader vehicle’s VaA and BaL information to a maximum of two hops; and the intra-platoon communication model shown in Figure 2(c) further reduces the number of transmission hops required for member vehicles’ BaL information; (ii) the numbers of transmission hops for both VaA and BaL information are proportional to \( m \) in [28], since only the communication links between two adjacent vehicles are considered. Furthermore, the value of \( k_{opt} \) increases with \( m \), resulting in more vehicles communicating with the leader vehicle directly (single-hop). Although the transmission delay of the D2D-multicast based model is less than that in the eMBMS based model when sharing the leader vehicle’s VaA information, the eMBMS based model outperforms the D2D-multicast based model when sharing BaL information.

Figure 7 shows the effect of the subchannel bandwidth \( W \) on the delay performance for the three approaches. As the subchannel bandwidth \( W \) decreases, the maximum end-to-end delays of these three approaches increase. However, this increase is smaller in our proposed approaches when compared to that in [28]. Furthermore, Figures 6 and 7 show that the proposed approaches outperform the approach in [28], especially for a large platoon size and a small subchannel bandwidth.

The benefits of our proposed approaches come at the cost of the amount of subchannels and transmission power needed. This is shown in Figure 8. More subchannels are needed in our proposed approaches compared to that of [28], especially in the eMBMS based model. However, the difference in the number of required subchannels among these three approaches decreases with \( m \). On the other hand, the results in Figure 8(b)
show that more transmission power is needed in the proposed approaches, especially in the D2D-multicast based model. This is due to the longer-distance single-hop transmissions utilized in the intra-platoon communication model (in Figure 2(c)), which leads to a relatively higher transmission powers on some vehicles, and therefore, resulting in a higher average transmission power.

VII. CONCLUSIONS

In this paper, we have proposed subchannel allocation and power control schemes that utilize D2D multicast and eMBMS communications to support inter-vehicle communications in a highway multiplatooning scenario. We have analyzed the achievable transmission rate and delay of the proposed RA approaches. In order to evaluate the performance of the proposed RA approaches, we compare them to an existing D2D-unicast based RA scheme. The numerical results have demonstrated that the proposed RA approaches outperform the existing one, in terms of transmission delay for sharing vehicle and platoon information. For the future work, we will investigate the impact of communication delay on the multiplatooning control, compare the multiplatooning communication performance between the DSRC and the LTE technologies, and ultimately design an efficient DSRC-LTE hybrid approach for multiplatooning communications.

APPENDIX A

PROOF OF THEOREM 1

Proof: According to equation (2) in Subsection II-C, the received SINR at $V_w$ can be expressed as

$$S_{g, w} = \frac{p_0|h_0|^2(d_{g, w})^{-\beta}}{\sigma} = \lambda$$  \hspace{1cm} (26)
and
\[ S'_{g,w} = \frac{p_1 |h_0|^2 (d_{g,w})^{-\beta}}{\sigma + I_1} = \lambda \] (27)
respectively, where the equation (26) is the received SINR at \( V_w \) in presence of background AWGN \( \sigma \), and the equation (27) is the received SINR at \( V_w \) in presence of background AWGN \( \sigma \) and the interference \( I_1 \). Then, one can get the transmission powers \( p_0 \) and \( p_1 \) as follows,
\[ p_0 = \frac{\lambda \sigma}{|h_0|^2 (d_{g,w})^\beta} \] (28)
\[ p_1 = \frac{\lambda (\sigma + I_1)}{|h_0|^2 (d_{g,w})^\beta}. \] (29)
Thus, the value of \( p_1 - p_0 \) can be calculated as,
\[ p_1 - p_0 = \frac{\lambda (\sigma + I_1)}{|h_0|^2 (d_{g,w})^\beta} - \frac{\lambda \sigma}{|h_0|^2 (d_{g,w})^\beta} = \frac{\lambda |I_1|}{|h_0|^2 (d_{g,w})^\beta}. \] (30)
Theorem 1 is proved.

**Appendix B**

**Proof of Theorem 2**

**Proof:** According to the constraint equations (18a) and (20), the transmission power of \( V_{m-k+1}^{(j)} \) can be given by
\[ p_{m-k+2}^{(j)} \geq \frac{\eta}{|h_0|^2 ((m-k+1)D_v)^{-\beta}} \geq \Gamma_2(k). \] (31)
According to the constraint equations (18b) and (20), the transmission power of \( V_{m-k+1}^{(j+1)} \) can be given by
\[ p_{m-k+2}^{(j+1)} \geq \frac{\eta}{|h_0|^2 (m-k+1)D_v^{-\beta}} \geq \Gamma_2(k). \] (32)

According to the constraint equations (18c) and (20), one can get
\[ p_{m-k+2}^{(j)} \geq \frac{\lambda [2(m-k)D_v + D_p]^{-\beta}}{\sigma \lambda + |h_0|^2 ((m-k+1)D_v)^{-\beta}} + \frac{\beta}{2} \geq \Gamma_3(k) + \Gamma_4(k). \] (33)

Substitute equations (31), (32), and (33) back into the optimization objective function and constrain equations (equation (18a)-(18d)) of the power control problem for member vehicles, then, the relationship among the optimization objective function and the constrain equations (31), (32), and (33) can be described as Figure 9 for a given \( k \) (\( \frac{m+2}{2} \leq k \leq m \)). Thus, the power control problem for member vehicles can be simplified and theorem 2 is proved.

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**References**


Figure 9: Illustration of the relationship between the optimization objective function and constrain equations (31), (32) and (33).


