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**The Probability that the Number of Points on an
Elliptic Curve over a Finite Field is Prime**

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Abstract The paper gives a formula for the probability that a randomly chosen elliptic curve over a finite field has a prime number of points. Two heuristic arguments in support of the formula are given as well as experimental evidence.

The paper also gives a formula for the probability that a randomly chose elliptic curve over a finite field has kq points where k is a small number and where q is a prime.