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**The Largest non-integer Zero of Chromatic  
Polynomials of Graphs with Fixed Order**

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**Abstract** For any simple graph  $G$ , let  $P(G, \lambda)$  denote the chromatic polynomial of  $G$ . In this paper, we determine the largest non-integer real zero of  $P(G, \lambda)$  over all graphs  $G$  with  $n$  vertices. It shows that  $P(G, \lambda)$  has no non-integer zeros in the interval  $(n - 3, +\infty)$ . But for any  $\epsilon > 0$ , when  $n$  is large enough, there is a graph  $H$  with  $n$  vertices such that  $P(H, \lambda)$  has a real zero in  $(n - 3 - \epsilon, n - 3)$ .

**Keywords** graph, chromatic polynomial, zero