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A Rotation Bijection for Lattice Paths above a Line of Integer Slope

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Abstract   We provide a direct geometric bijection for the number of lattice paths that never go below the line $y = kx$ for a positive integer k. This solution to the Generalized Ballot Problem is in the spirit of the reflection principle for the Ballot Problem (the case $k = 1$), but it uses rotation instead of reflection.