

Abstract Let \mathcal{G} be a planar graph and let T be a subset of vertices of \mathcal{G} of even cardinality. Suppose that there exists a T -cut of \mathcal{G} of cardinality at most five and that the parity of the cardinality of every T -cut is the same. We show that in that case the cardinality of the smallest T -cut is equal to the maximum number of pairwise disjoint T -joins. As a corollary we obtain that for $k \in \{4, 5\}$, a k -regular planar graph has chromatic index k if and only if for every subset of vertices X of odd cardinality there are at least k edges with exactly one end in X . The case where $k = 4$ was conjectured by Seymour in 1979.