ABSTRACT. We survey the recent developments in algorithms for the elliptic and hyperelliptic curve discrete logarithm problems, and explore the connections between these problems. We also consider some computational problems that are of interest in pairing-based cryptography.