

ECRYPT II
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Cryptographic Hash Functions: Theory and Practice

Bart Preneel
Katholieke Universiteit Leuven - COSIC
firstname.lastname@esat.kuleuven.be



Hash functions

X.509 Annex D
MDC-2
MD2, MD4, MD5
SHA-1

→

RIPEMD-160
SHA-256
SHA-512

→

SHA-3

This is an input to a cryptographic hash function. The input is a very long string, that is reduced by the hash function to a string of fixed length. There are additional security conditions: it should be very hard to find an input hashing to a given value (a preimage) or to find two colliding inputs (a collision).

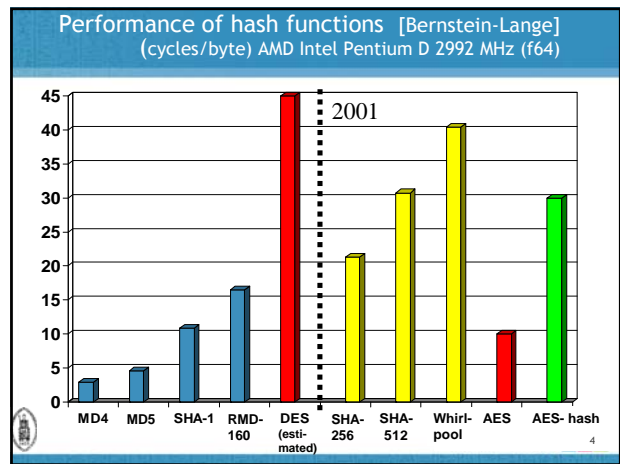
h

→

1A3FD4128A198FB3CA345932

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Hash function history 101



Applications

- short unique identifier to a string
 - digital signatures
 - data authentication
- one-way function of a string
 - protection of passwords
 - micro-payments
- confirmation of knowledge/commitment
- pseudo-random string generation/key derivation
- entropy extraction
- construction of MAC algorithms, stream ciphers, block ciphers,...

2005: 800 uses of MD5 in Microsoft Windows

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Agenda

Definitions

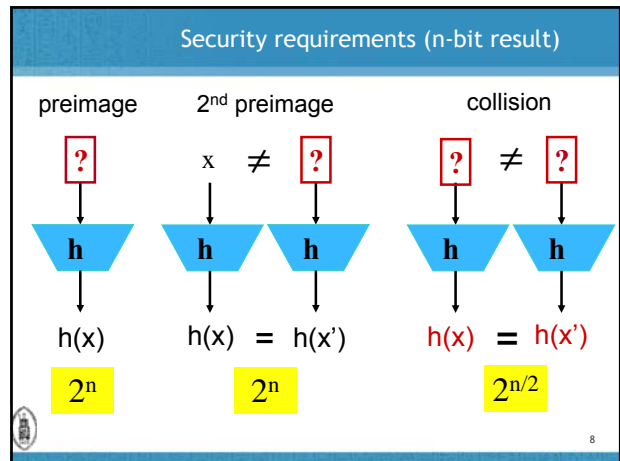
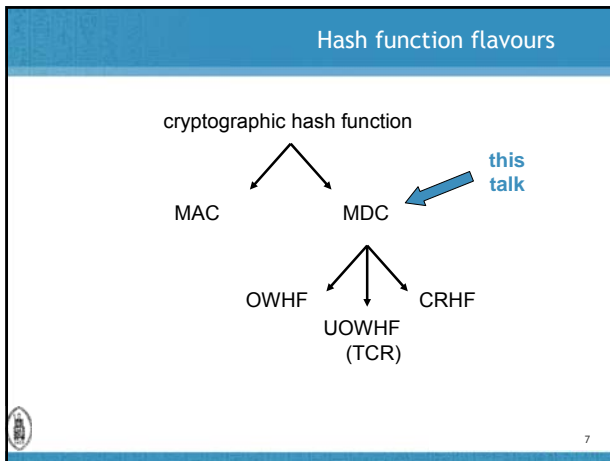
Iterations (modes)

Compression functions

SHA-{0,1,2}

SHA-3 bits and bytes

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- ### Informal definitions
- no secret parameters
 - input string x of arbitrary length \Rightarrow output $h(x)$ of fixed bitlength n
 - computation “easy”
 - One Way Hash Function (OWHF)
 - preimage resistance
 - 2nd preimage resistance
 - Collision Resistant Hash Function (CRHF): OWHF +
 - collision resistant
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Formal definition: (2nd) preimage resistance

Notation: $\Sigma = \{0, 1\}, l(n) > n$

A **one-way hash function (OWHF)** h is a function with domain $D = \Sigma^{l(n)}$ and range $R = \Sigma^n$ that satisfies the following conditions:

- **preimage resistance:** let x be selected uniformly in D and let M be an adversary that on input $h(x)$ uses time $\leq t$ and outputs $M(h(x)) \in D$. For each adversary M ,

$$\Pr_{x \in D} \{ h(M(h(x))) = h(x) \} < \epsilon$$
 Here the prob. is also taken over the random choices of M .
- **2nd preimage resistance:** let x be selected uniformly in $D = \Sigma^{l(n)}$ and let M' be an adversary who on input x uses time $\leq t$ and outputs $x' \in D$ with $x' \neq x$. For each adversary M' ,

$$\Pr_{x \in D} \{ h(M'(x)) = h(x) \} < \epsilon$$
 Here the prob. is taken over the random choices of M' .

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Formal definitions: collision resistance

A **collision-resistant hash function (CRHF)** h is a function with domain $D = \Sigma^{l(n)}$ and range $R = \Sigma^n$ that satisfies the following conditions:

- for **each** collision string finder F that uses time $\leq t$ and outputs either “?” or a pair $x, x' \in \Sigma^{l(n)}$ with $x' \neq x$ such that $h(x') = h(x)$ we have that

$$\Pr \{ F(h) \neq \text{“?”} \} < \epsilon$$
 Here the prob. is taken over the random choices of F .

Is this correct?

No! For every h there are many (short) colliding strings, and so there **exist** many very simple collision string finders F that output a collision with probability 1

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Formal definitions: collision resistance

A **collision-resistant hash function family (CRHF)** H is a function family $\{h_S\}$ with domain $D = \Sigma^{l(n)}$ and range $R = \Sigma^n$ and indexed by a “key” S that satisfies the following conditions:

- collision resistance: let F be a collision string finder that on input $S \in \Sigma^s$ uses time $\leq t$ and outputs either “?” or a pair $x, x' \in \Sigma^{l(n)}$ with $x' \neq x$ such that $h_S(x') = h_S(x)$. For each F ,

$$\Pr_S \{ F(H) \neq \text{“?”} \} < \epsilon$$
 Here the prob. is also taken over the random choices of F .

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Formal definitions - continued

- for collision resistance: formalization requires a family, but see [Stinson'06], [Rogaway'06]: "formalizing human ignorance"
- for (2nd) preimage resistance, one can choose the challenge (x) and/or the key (S) that selects the function. This gives three flavors [Rogaway-Shrimpton'04]:
 - random challenge, random key (Pre and Sec)
 - random key, fixed challenge (ePre and eSec - everywhere) (eSec=UOWHF)
 - fixed key, random challenge (aPre and aSec - always)
- complex relationship (see figure on next slide)

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Relation between properties

[Rogaway-Shrimpton'04]
[Stinson'06]
[ReyhaniTabar-Susilo-Mu'10]
[Andreeva-Stam'10]

Even if $\text{Coll} \Rightarrow \text{xSEC/Pre}$: bound always $2^{n/2} \ll 2^n$

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Brute force (2nd) preimage

- multiple target second preimage (1 out of many):** if one can attack 2^t simultaneous targets, the effort to find a single preimage is 2^{n-t}
- multiple target second preimage (many out of many):**
 - time-memory trade-off with $\Theta(2^n)$ precomputation and storage $\Theta(2^{2n/3})$ time per (2nd) preimage: $\Theta(2^{2n/3})$ [Hellman'80]
 - full cost per (2nd) preimage from $\Theta(2^n)$ to $\Theta(2^{2n/5})$ [Wiener'02] (if $\Theta(2^{3n/5})$ targets are attacked)
- answer: randomize hash function: key, parameter, salt, spice,...**

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Quantum computers

- in principle exponential parallelism
- inverting a one-way function: 2^n reduced to $2^{n/2}$ [Grover'96]
- collision search:
 - $2^{n/3}$ computation + hardware [Brassard-Hoyer-Tapp'98]
 - [Bernstein'09] classical collision search requires $2^{n/4}$ computation and hardware (= standard cost of $2^{n/2}$)

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Brute force attacks in practice

- (2nd) preimage search
 - $n = 128$: 23 B\$ for 1 year if one can attack 2^{40} targets in parallel
- parallel collision search: small memory using cycle finding algorithms (distinguished points)
 - $n = 128$: 1 M\$ for 8 hours (or 1 year on 100K PCs)
 - $n = 160$: 90 M\$ for 1 year
 - need 256-bit result for long term security (30 years or more)

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Collision resistance

- hard to achieve in practice**
 - many attacks
 - requires double output length $2^{n/2}$ versus 2^n
- hard to achieve in theory**
 - [Simon'98] one cannot derive collision resistance from "general" preimage resistance (there exists no black box reduction)
- hard to bypass**
 - UOWHF (TCR, eSec) randomize hash function after choosing the message [Naor-Yung'89]
 - how to enforce this in practice? (insider attacks i.e. attacks by the signer)
 - randomized hashing: RMX mode [Halevi-Krawczyk'05]
 - $H(r \parallel x_1 \oplus r \parallel x_2 \oplus r \parallel \dots \parallel x_t \oplus r)$
 - needs e-SPR (not met by MD5)
 - issues with insider attacks
 - [Gauravaram-Knudsens09]: $2^{n/2}$ complexity but on-line

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Properties in practice

- collision resistance is not always necessary
- other properties are needed:
 - pseudo-randomness if keyed (with secret key)
 - pseudo-random oracle property
 - near-collision resistance
 - partial preimage resistance (most of input known)
 - multiplication freeness
- how to formalize these requirements and the relation between them?

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Pseudo-random function

computationally indistinguishable from a random function

$$\text{Adv}_n^{\text{prf}} = \Pr [\kappa \xleftarrow{\$} \mathbf{K}: A^{h(\cdot)} \Rightarrow 1] - \Pr [\kappa \xleftarrow{\$} \text{RAND}(m,n): A^f \Rightarrow 1]$$

RAND(m,n): set of all functions from m-bit to n-bit strings

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Indifferentiability from a random oracle or PRO property [Maurer+04]

variant of indistinguishability appropriate when distinguisher has access to inner component (e.g. building block of a hash function)

\exists Simulator S, \forall distinguisher D, $\text{Adv}^{\text{PRO}}(H,S)$ is small

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Iteration

(mode of compression function)

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Hash function: iterated structure

Split messages into blocks of fixed length and hash them block by block with a compression function f

Efficient and elegant
But ...

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Security relation between f and h

- iterating f can degrade its security
 - trivial example: 2nd preimage

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Security relation between f and h (2)

- solution: Merkle-Damgård (MD) strengthening
 - fix IV, use unambiguous padding and insert length at the end
- f is collision resistant \Rightarrow h is collision resistant [Merkle'89-Damgård'89]
- f is ideally 2nd preimage resistant \Leftrightarrow h is ideally 2nd preimage resistant [Lai-Massey'92]
 - few hash functions have a strong compression function
 - very few hash functions treat x_i and H_{i-1} in the same way

Security relation between f and h (3)

length extension: if one knows $h(x)$, easy to compute $h(x || y)$ without knowing x

solution: output transformation

Property preservation

[Andreeva-Mennink-P'10] for overview

Sec/Pre preservation seems to be problematic
Is Pre preservation meaningful?

	Coll	Sec	Pre	Pro	aSec	eSec	aPre	ePre
Suffix- & Prefix-free MD	Green	Red	Red	Green				
Envelope MD	Green	Red	Red	Green				
BCM	Green	Green	Red	?				
Haifa	Green	Red	Red	Green				
RMX	Green	Red	Red	Red				
Shoup UOWH	Green	Red	Red	Red	Green	Green	Red	Green
ROX	Green	Green	Green	Red	Green	Green	Green	Green

Not applicable

More on property preservation/domain extension

- PRO preservation \Rightarrow Col, Sec and Pre for ideal compression function
 - but for narrow pipe bounds for Sec and Pre are at most $2^{n/2}$ rather than 2^n
- MD + f = Preimage Aware (PRA) \Rightarrow PRO [Dodis-Ristenpart-Shrimpton'09]
 - Property "in between" CR (collision resistance) and PRO
- MD + split padding + f = csPre (chosen suffix preimage) \Rightarrow Pre (similar for Sec) [Yasuda'08]
- MD with envelope method $h(K || x || K)$ \Rightarrow pseudo-randomness/MAC [Bellare-Cannetti-Krawczyk'96]
 - but some problems and HMAC is a better construction

Attacks on MD-type iterations

- multi-collision attack and impact on concatenation [Joux'04]
- long message 2nd preimage attack [Dean-Felten-Hu'99], [Kelsey-Schneier'05]
 - Sec security degrades lineary with number 2^t of message blocks hashed: $2^{n+t+1} + t 2^{n/2+1}$
 - appending the length does not help here!
- herding attack [Kelsey-Kohn'06]
 - reduces security of commitment using a hash function from 2^n
 - on-line 2^{n-1} + precomputation $2.2^{(n+1)/2}$ + storage 2^t
- recent work [Andreeva-Bouillaguet-Dunkelman-Kelsey'09], [Andreeva+09]
 - long message 2nd preimage and herding extended to MD variants (e.g., dither hash, zipper hash, ROX, Shoup hash...)
 - Trojan message attack

How (NOT) to strengthen a hash function?

[Joux'04]

- answer: concatenation
- h_1 (n_1 -bit result) and h_2 (n_2 -bit result)

- intuition: the strength of g against collision/(2nd) preimage attacks is the product of the strength of h_1 and h_2
 - if both are "independent"
- but....

Multiple collisions \neq multi-collision

Assume "ideal" hash function h with n -bit result

- $\Theta(2^{n/2})$ evaluations of h (or steps): 1 collision
 - $h(x)=h(x')$
- $\Theta(r \cdot 2^{n/2})$ steps: r^2 collisions
 - $h(x_1)=h(x'_1)$; $h(x_2)=h(x'_2)$; ...; $h(x_r)=h(x'_r)$
- $\Theta(2^{2n/3})$ steps: a 3-collision
 - $h(x)=h(x')=h(x'')$
- $\Theta(2^{n(t-1)/t})$ steps: a t -fold collision (multi-collision)
 - $h(x_1)=h(x_2)=\dots=h(x_t)$

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Multi-collisions on iterated hash function (2)

- for IV: collision for block 1: x_1, x'_1
- for H_1 : collision for block 2: x_2, x'_2
- for H_2 : collision for block 3: x_3, x'_3
- for H_3 : collision for block 4: x_4, x'_4

now $h(x_1||x_2||x_3||x_4) = h(x'_1||x_2||x_3||x_4) = h(x'_1||x'_2||x_3||x_4) = \dots = h(x'_1||x'_2||x'_3||x'_4)$ **a 16-fold collision**

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Multi-collisions [Joux '04]

consider h_1 (n_1 -bit result) and h_2 (n_2 -bit result), with $n_1 \geq n_2$.
 concatenation of 2 iterated hash functions ($g(x) = h_1(x) || h_2(x)$)
 is **as most as strong as the strongest** of the two (even if both are independent)

- cost of collision attack against g at most
 $n_1 \cdot 2^{n_2/2} + 2^{n_1/2} \ll 2^{(n_1+n_2)/2}$
- cost of (2nd) preimage attack against g at most
 $n_1 \cdot 2^{n_2/2} + 2^{n_1} + 2^{n_2} \ll 2^{n_1+n_2}$
- if either of the functions is weak, the attacks may work better.
- main observation: finding multiple collisions for an iterated hash function is not much harder than finding a single collision (if the size of the internal memory is n bits)

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Summary

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Improving MD iteration

salt + output transformation + counter + wide pipe

security reductions well understood
 many more results on property preservation
 impact of theory limited

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Improving MD iteration

- degradation with use: salting (family of functions, randomization)
 - or should a salt be part of the input?
- PRO: strong output transformation g
 - also solves length extension
- long message 2nd preimage: preclude fix points
 - counter $f \rightarrow f_i$ [Biham-Dunkelman'07]
- multi-collisions, herding: avoid breakdown at $2^{n/2}$ with larger internal memory: known as wide pipe
 - e.g., extended MD4, RIPEMD, [Luks'05]

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Compression functions

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Block cipher (E_K) based

Davies-Meyer

Miyaguchi-Preneel

- output length = block length
- 12 secure compression functions (in ideal cipher model)
- requires 1 key schedule per encryption
- analysis [Black-Rogaway-Shrimpton'02], [Duo-Li'06], [Stam'09],...

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Block cipher (E_K) based

- which assumptions are needed on the block cipher E to prove MD iterated Davies-Meyer secure?
 - standard model: no security results (PRF/PRP is not sufficient)
 - ideal cipher model: ok to prove collision resistance and (second) preimage resistance
 - can this be relaxed?
 - PRO preserving with chop or NMAC/HMAC
 - PRA preserving

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Permutation (π) based

sponge

MD6

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Permutation (π) based: sponge

Examples: Panama, RadioGatun, Grindahl, Keccak (no buffer)

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Permutation (π) based

JH

Grøstl

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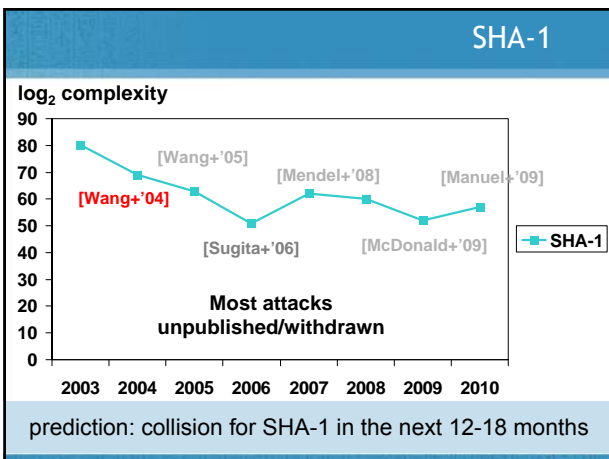
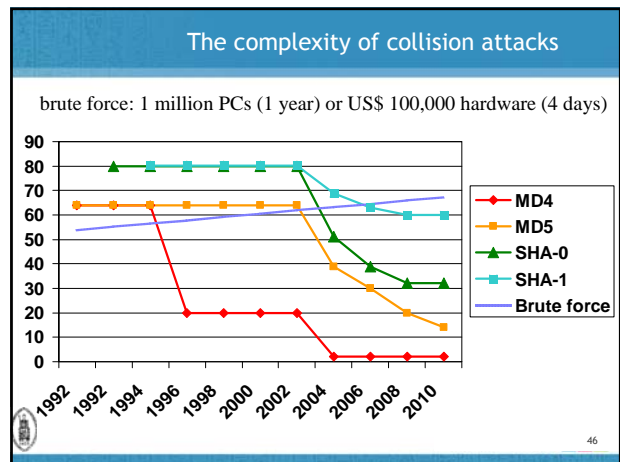
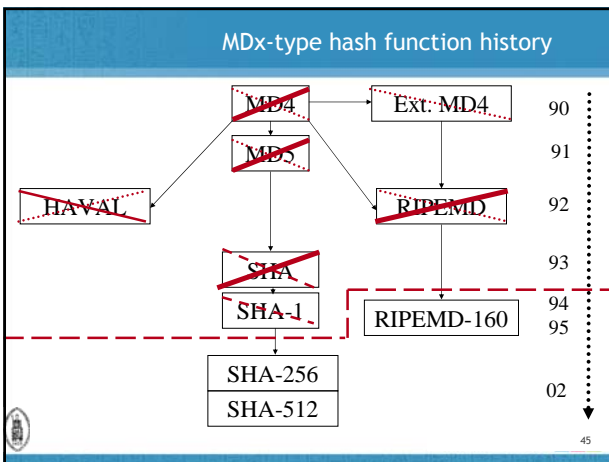
Iteration modes

- security of simple modes well understood
- powerful tools available
- analysis of slightly more complex schemes very difficult
- which properties are meaningful?
- which properties are preserved?
- MD versus sponge is still open debate

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SHA-{0,1,2}

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NIST and SHA-1

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Rogue CA attack

[Sotirov-Stevens-Appelbaum-Lenstra-Molnar-Osvik-de Weger '08]

- request user cert; by special collision this results in a fake CA cert (need to predict serial number + validity period)

impact: **rogue CA** that can issue certs that are trusted by all browsers

- 6 CAs have issued certificates signed with MD5 in 2008:
 - Rapid SSL, Free SSL (free trial certificates offered by RapidSSL), TC TrustCenter AG, RSA Data Security, Verisign.co.jp

Upgrades

- RIPEND-160 is good replacement for SHA-1
- upgrading algorithms is always hard
- TLS uses MD5 || SHA-1 to protect algorithm negotiation (up to v1.1)
- upgrading negotiation algorithm is even harder: need to upgrade TLS 1.1 to TLS 1.2**

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SHA-2 [NIST'02]

- SHA-224, SHA-256, SHA-384, SHA-512
 - non-linear message expansion
 - more complex operations
 - 64/80 steps
 - SHA-384 and SHA-512: 64-bit architectures
- SHA-256 collisions: 24/64 steps [Sanadhya-Sarkar'08]
- SHA-256 preimages: **43/64 steps** [Aoki+'09]
- implementations today faster than anticipated
- adoption
 - industry may migrate to SHA-2 by 2011 or may wait for SHA-3
 - very slow for TLS/IPsec (no pressing need)

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SHA-3

(bits and bytes)

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NIST AHS competition (SHA-3)

- SHA-3 must support 224, 256, 384, and 512-bit message digests, and must support a maximum message length of at least 2^{64} bits

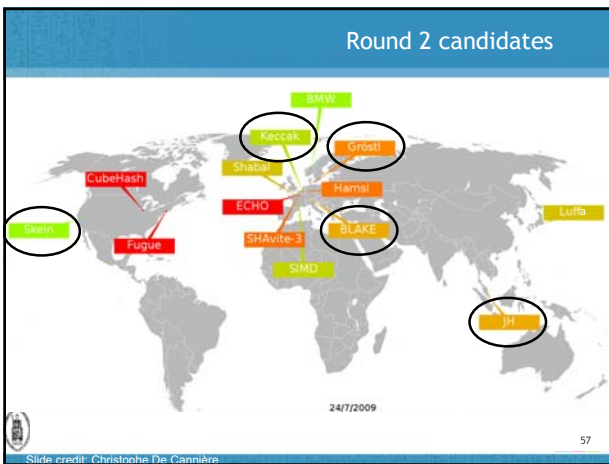
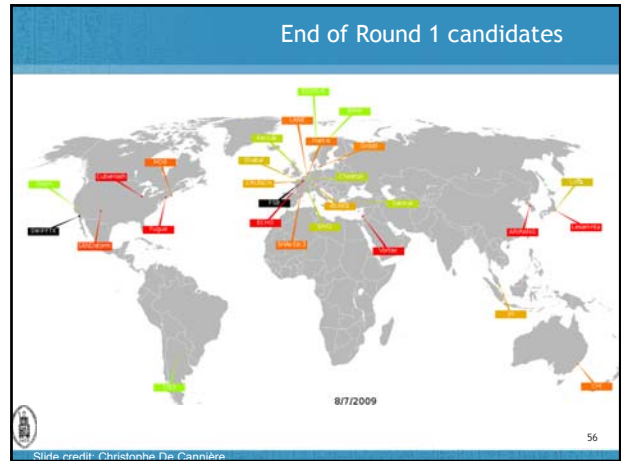
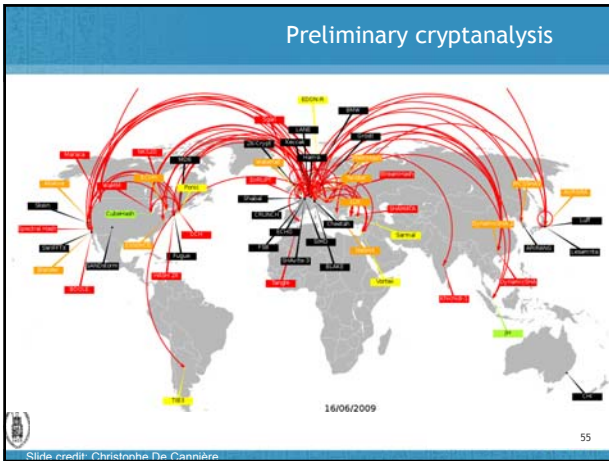
Call: 02/11/07
 Deadline (64): 31/10/08
 Round 1 (51): 9/12/08
 Round 2 (14): 24/7/09
 Final (5): 9/12/10
Standard: 2012

Round	Candidates
Q4/08	64
Q3/09	51
Q4/10	14
Q2/12	5

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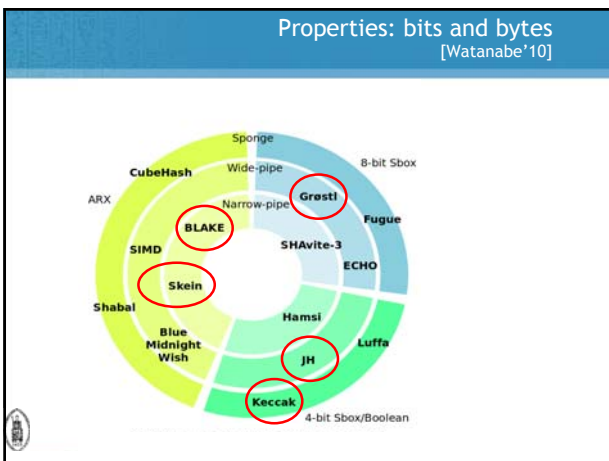
The candidates

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Compression function/iteration

	Block cipher	Permutation	MD/HAIFA
Blake			HAIFA
Grostl		2-permutation	MD
JH			JH-specific
Keccak		Sponge	
Skein	MMO		MD*/Tree (UBI)
BMW	PGV variant		MD
Cubehash		Sponge-type	
ECHO			HAIFA
Fugue		Sponge-type	
Hamsi			
Luffa		Sponge-type	
Shabal		Sponge-type	
Shavite-3	Davies-Meyer		HAIFA
SIMD	PGV variant		MD



Security reductions

[Andreeva-Mennink-P'10]

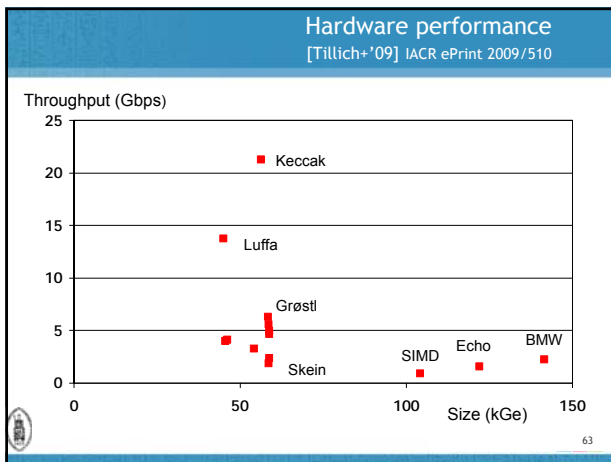
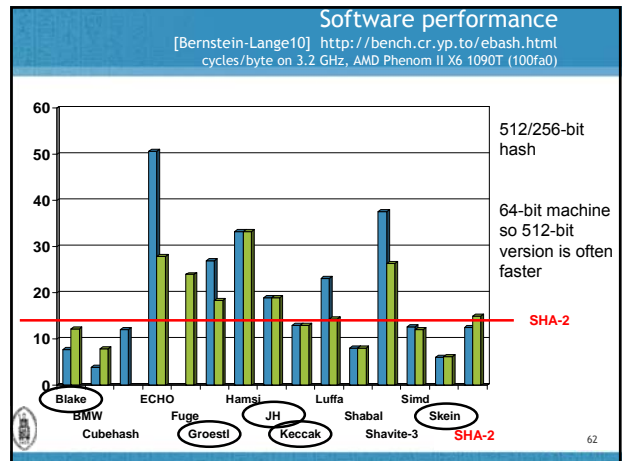
	type	of [pt]	Adv ₁ ^{cpa}	Adv ₁ ^{cpa}	Adv ₁ ^{cpa}	Adv ₁ ^{cpa}	Adv ₁ ^{cpa}	Adv ₁ ^{cpa}	Adv ₁ ^{cpa}
BLAKE	HAIFA	✓	✓						
BMW	chop-(MD+FT)	✓	✓						
Cubehash	chop-(MD+FT)	✓	✓						
ECHO	chop-HAIFA	✓	✓						
Fugue	chop-(MD+FT)	✓	✓						
Grostl	hsp-(MD+FT)	✓	✓						
Hamsi	MD+FT	✓	✓						
JH	chop-MD	✓	✓						
Keccak	chop-MD	✓	✓						
Luffa	chop-(MD+FT)	✓	✓						
Shabal	chop-MD	✓	✓						
SHAvite-3	HAIFA	✓	✓						
SIMD	chop-(MD+FT)	✓	✓						
Skein	MD	✓	✓						

Table 1. A schematic summary of all results. The first column describes the hash function construction, and the second and third columns show which hash functions have a suffix-free (sf) or prefix-free (pf) padding. A green box indicates the existence of a non-trivial upper bound, a red box means that an efficient adversary is known for the security notion, and a yellow box indicates that no result is known, but recent literature gives some confidence in the existence of a non-trivial bound.

Security: SHA-3 Zoo

http://ehash.iaik.tugraz.at/wiki/The_SHA-3_Zoo

Hash Name	Principal Submitter	Final Attack on SHA-3 Requirements	Final Attack on other Hash Requirements
BLAKE	Jean-Philippe Aumasson		
Blue Ridge	Shawn Atkinson		
Crataegus	David J. Bernstein		
ECHO	Henk Gilbert		
Fugue	Changwoo Jeon		
Groestl	Lars R. Knudsen		
Hamsi	Çağrı Koç		
JH	John Kelsey		
Keccak	Keccak Team		
Luffa	Shinji Inoue		
Shabal	Denis S. Shteynberg		
Shavite-3	Shavite Team		
Simd	Simd Team		
Skein	Scott Fluhrer		



- ### Issues arisen during Round 1
- round 1 was very short; several functions received no outside analysis
 - security
 - some controversy on complexity and relevance of attacks
 - proofs have not helped much to survive
 - performance
 - weak performance resulted in elimination
 - 7/14 designs tweaked at the beginning of round 2

- ### Issues arisen during Round 2
- security
 - few real attacks but some weaknesses
 - new design ideas harder to validate
 - performance: roughly as fast or faster than SHA-2
 - SHA-2 gets faster every day
 - widely different results for hardware and software
 - software: large difference between high end and embedded
 - hardware: FPGA and ASIC
 - what about lightweight devices and 128-core machines?
 - diversity = third selection criterion
 - expect more tweaks before final
 - variable number of rounds?
 - NIST expects that SHA-2 and SHA-3 will co-exist

- ### Final
- Blake
 - JH
 - Groestl
 - Keccak
 - Skein

SHA-4?

- an open competition such as SHA-3 is bound to result in new insights between 2008-2012
- only few of these can be incorporated using “tweaks”
- the winner selected in 2012 will reflect the state of the art in October 2008
- nevertheless, it is unlikely that we will have a SHA-4 competition before 2030



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Hash functions: conclusions

- SHA-1 would have needed 128-160 steps instead of 80
- 2004-2009 attacks: cryptographic meltdown but not dramatic for most applications
 - clear warning: upgrade asap
- half-life of a hash function is < 1 year
- theory is developing for more robust iteration modes and extra features; still early for building blocks

- nirwana: efficient hash functions with security reductions



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