

Lecture 16

Generative Adversarial Networks (GAN)

Generative Adversarial Networks (GAN)

- Original paper:
 - Generative Adversarial Nets
- Authors:
 - Ian J. Goodfellow, Jean Pouget-Abadie, Mehdi Mirza, Bing Xu, David Warde-Farley, Sherjil Ozair, Aaron Courville, Yoshua Bengio (2014)
- Organization:
 - Université de Montréal
- URL:
 - <https://arxiv.org/abs/1406.2661>

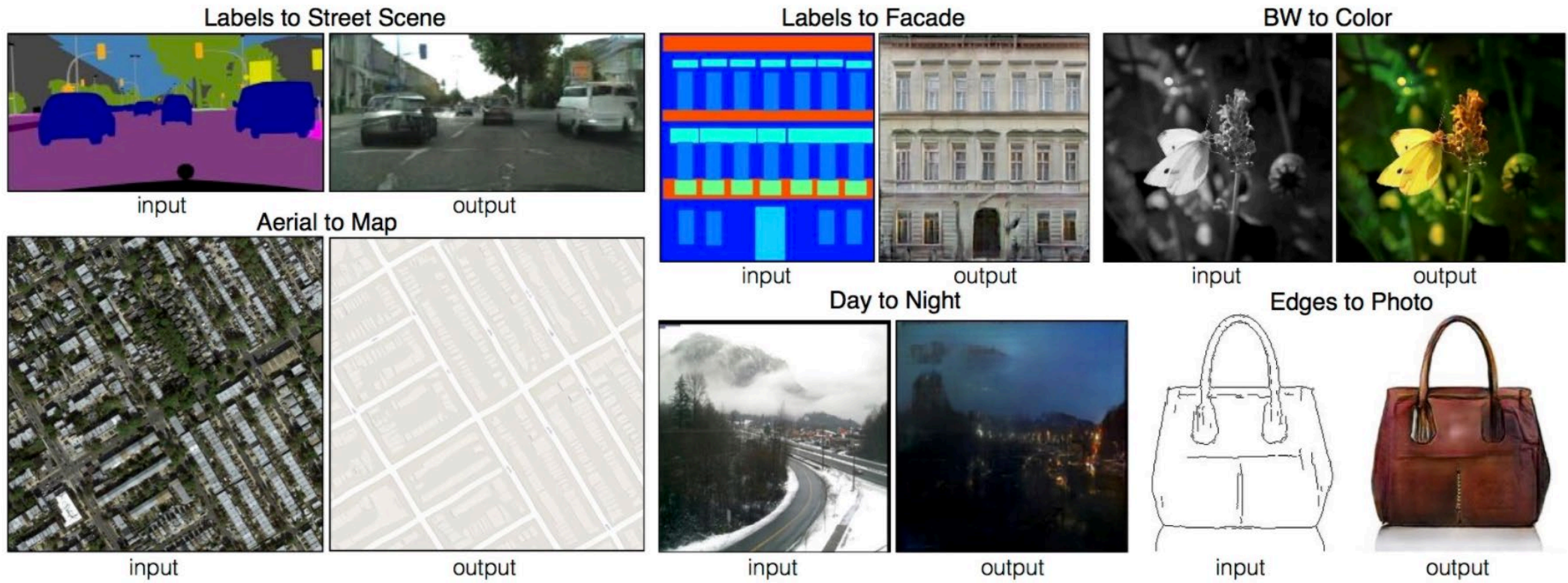
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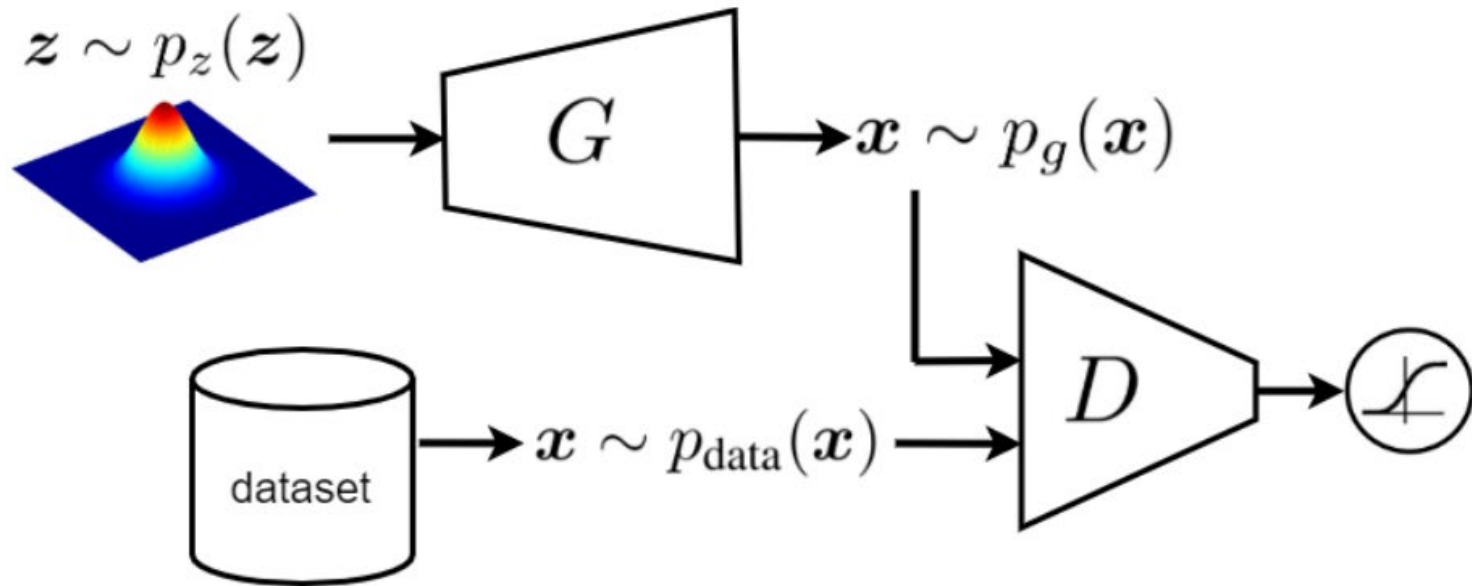
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Different Applications



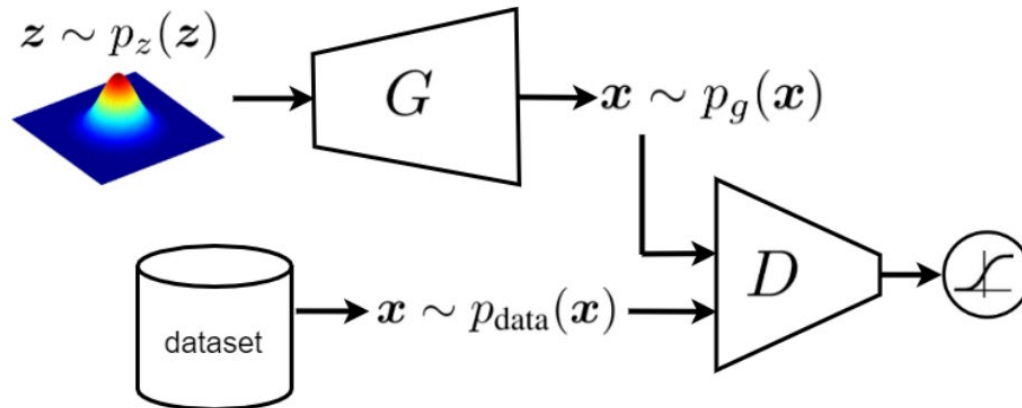
Adversarial Learning



Adversarial Learning

$$\min_G \max_D V(D, G)$$

$$V(D, G) = \mathbb{E}_{x \sim P_{data}(x)} [\log D(x)] + \mathbb{E}_{z \sim P_z(z)} [\log(1 - D(G(z)))]$$



Training Generative Adversarial Networks

$$\min_G \max_D V(D, G)$$

$$\max_D V(D, \mathbf{G}) \Rightarrow \min_G V(\mathbf{D}, G) \Rightarrow \max_D V(D, \mathbf{G}) \Rightarrow \min_G V(\mathbf{D}, G) \Rightarrow$$

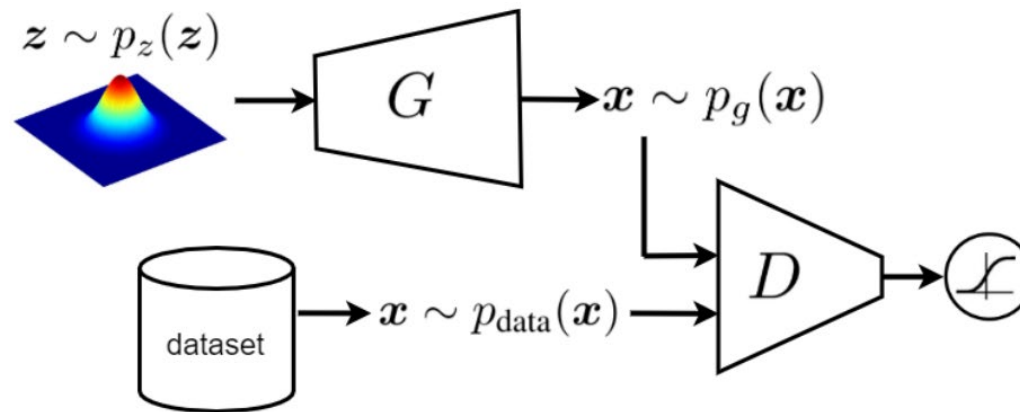
$$V(D, G) = \mathbb{E}_{x \sim p_{data}(x)}[\log D(x)] + \mathbb{E}_{z \sim p_z(z)}[\log(1 - D(G(z)))]$$

$$\begin{aligned} V(D, G) &= \mathbb{E}_{x \sim p_{data}(x)}[\log D(x)] + \mathbb{E}_{z \sim p_z(z)}[\log(1 - D(G(z)))] \\ &= \int_x p_{data}(x) \log(D(x)) dx + \int_z p_z(z) \log(1 - D(G(z))) dz \end{aligned}$$

$$V(D, G) = \mathbb{E}_{x \sim p_{\text{data}}(x)}[\log D(x)] + \mathbb{E}_{z \sim p_z(z)}[\log(1 - D(G(z)))]$$

$$= \int_x p_{\text{data}}(x) \log(D(x)) dx + \int_z p_z(z) \log(1 - D(G(z))) dz$$

$$x = G(z) \Rightarrow z = G^{-1}(x) \Rightarrow dz = (G^{-1})'(x) dx$$



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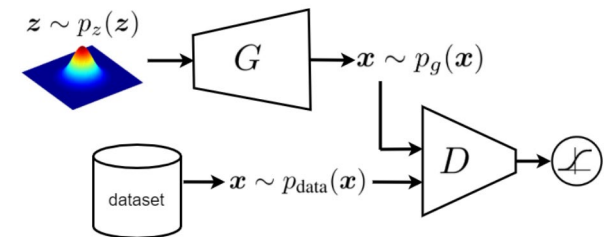
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$$x = G(z) \Rightarrow z = G^{-1}(x) \Rightarrow dz = (G^{-1})'(x) dx$$

$$\Rightarrow p_g(x) = p_z(G^{-1}(x))(G^{-1})'(x)$$

If you have a random variable z with a known distribution $p_z(z)$, and you transform z using a function G , to get a new random variable $x = G(z)$, then the distribution of x will generally be given by:

$$p_g(x) = p_z(G^{-1}(x)) \cdot (G^{-1})'(x)$$



$$V(D, G) = \mathbb{E}_{x \sim p_{data}(x)}[\log D(x)] + \mathbb{E}_{z \sim p_z(z)}[\log(1 - D(G(z)))]$$

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$$\begin{aligned}
V(D, G) &= \mathbb{E}_{x \sim p_{data}(x)}[\log D(x)] + \mathbb{E}_{z \sim p_z(z)}[\log(1 - D(G(z)))] \\
&= \int_x p_{data}(x) \log(D(x)) dx + \int_z p_z(z) \log(1 - D(G(z))) dz \\
&\quad x = G(z) \Rightarrow z = G^{-1}(x) \Rightarrow dz = (G^{-1})'(x) dx \\
&\quad \Rightarrow p_g(x) = p_z(G^{-1}(x))(G^{-1})'(x) \\
&= \int_x p_{data}(x) \log(D(x)) dx + \int_x p_z(G^{-1}(x)) \log(1 - D(x))(G^{-1})'(x) dx \\
&= \int_x p_{data}(x) \log(D(x)) dx + \int_x p_g(x) \log(1 - D(x)) dx
\end{aligned}$$

$$V(D, G) = \mathbb{E}_{x \sim p_{data}(x)}[\log D(x)] + \mathbb{E}_{z \sim p_z(z)}[\log(1 - D(G(z)))]$$

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$$= \int_x p_{data}(x) \log(D(x)) dx + \int_x p_g(x) \log(1 - D(x)) dx$$

$$= \int_x p_{data}(x) \log(D(x)) + p_g(x) \log(1 - D(x)) dx$$

Understanding the objective function

$$\max_D V(D, G) = \max_D \int_x p_{data}(x) \log(D(x)) + p_g(x) \log(1 - D(x)) dx$$

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$$\frac{\partial}{\partial D(x)} (p_{data}(x) \log(D(x)) + p_g(x) \log(1 - D(x))) = 0$$

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$$\Rightarrow \frac{p_{data}(x)}{D(x)} - \frac{p_g(x)}{1 - D(x)} = 0$$

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$$\Rightarrow \frac{p_{data}(x)}{D(x)} - \frac{p_g(x)}{1 - D(x)} = 0$$

$$\Rightarrow D(x) = \frac{p_{data}(x)}{p_{data}(x) + p_g(x)}$$

Understanding the objective function

Suppose the discriminator is optimal $D_G^*(x)$,
the optimal generator makes: $p_{data}(x) = p_g(x)$

$$\Rightarrow D_G^*(x) = \frac{p_{data}(x)}{p_{data}(x) + p_g(x)}$$

Understanding the objective function

$$C(G) = \max_D V(G, D)$$

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Understanding the objective function

$$\begin{aligned} C(G) &= \max_D V(G, D) \\ &= \max_D \int_x p_{data}(x) \log(D(x)) + p_g(x) \log(1 - D(x)) dx \\ &= \int_x p_{data}(x) \log(D_G^*(x)) + p_g(x) \log(1 - D_G^*(x)) dx \end{aligned}$$

Understanding the objective function

$$\begin{aligned}C(G) &= \max_D V(G, D) \\&= \max_D \int_x p_{data}(x) \log(D(x)) + p_g(x) \log(1 - D(x)) dx \\&= \int_x p_{data}(x) \log(D_G^*(x)) + p_g(x) \log(1 - D_G^*(x)) dx \\&= \int_x p_{data}(x) \log\left(\frac{p_{data}(x)}{p_{data}(x) + p_g(x)}\right) + p_g(x) \log\left(\frac{p_g(x)}{p_{data}(x) + p_g(x)}\right) dx\end{aligned}$$

Understanding the objective function

$$C(G) = \max_D V(G, D)$$

$$= \max_D \int_x p_{data}(x) \log(D(x)) + p_g(x) \log(1 - D(x)) dx$$

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$$= \int_x p_{data}(x) \log\left(\frac{p_{data}(x)}{\frac{p_{data}(x) + p_g(x)}{2}}\right) + p_g(x) \log\left(\frac{p_g(x)}{\frac{p_{data}(x) + p_g(x)}{2}}\right) dx - \log(4)$$

Understanding the objective function

$$\begin{aligned}C(G) &= \max_D V(G, D) \\&= \max_D \int_x p_{data}(x) \log(D(x)) + p_g(x) \log(1 - D(x)) dx \\&= \int_x p_{data}(x) \log(D_G^*(x)) + p_g(x) \log(1 - D_G^*(x)) dx \\&= \int_x p_{data}(x) \log\left(\frac{p_{data}(x)}{p_{data}(x) + p_g(x)}\right) + p_g(x) \log\left(\frac{p_g(x)}{p_{data}(x) + p_g(x)}\right) dx \\&= \int_x p_{data}(x) \log\left(\frac{p_{data}(x)}{\frac{p_{data}(x) + p_g(x)}{2}}\right) + p_g(x) \log\left(\frac{p_g(x)}{\frac{p_{data}(x) + p_g(x)}{2}}\right) dx - \log(4) \\&= KL[p_{data}(x) \parallel \frac{p_{data}(x) + p_g(x)}{2}] + KL[p_g(x) \parallel \frac{p_{data}(x) + p_g(x)}{2}] - \log(4)\end{aligned}$$

Understanding the objective function

$$C(G) = \underset{\geq 0}{KL[p_{data}(x) \parallel \frac{p_{data}(x) + p_g(x)}{2}]} + \underset{\geq 0}{KL[p_g(x) \parallel \frac{p_{data}(x) + p_g(x)}{2}]} - \log(4)$$

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$$\min_G C(G) = 0 + 0 - \log(4) = -\log(4)$$

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$$\text{when } p_{data}(x) = \frac{p_{data}(x) + p_g(x)}{2}$$

$$\Rightarrow p_{data}(x) = p_g(x)$$

KL (Kullback-Leibler) divergence

- ▶ Jensen-Shannon Divergency (symmetric KL):

$$JSD(P||Q) = \frac{1}{2}D_{KL}(P||M) + \frac{1}{2}D_{KL}(Q||M),$$

$$M = \frac{1}{2}(P + Q)$$

Summary:

- ▶ Generator G , Discriminator D

$$V = \mathbb{E}_{x \sim P_{data}} [\log D(x)] \\ + \mathbb{E}_{x \sim P_G} [\log(1 - D(x))]$$

Summary:

- ▶ Generator G , Discriminator D
- ▶ Looking for G^* such that

$$G^* = \arg \min_G \max_D V(G, D)$$

$$V = \mathbb{E}_{x \sim P_{data}} [\log D(x)] \\ + \mathbb{E}_{x \sim P_G} [\log(1 - D(x))]$$

Summary:

- ▶ Generator G , Discriminator D
- ▶ Looking for G^* such that

$$G^* = \arg \min_G \max_D V(G, D)$$

- ▶ Given G , $\max_D V(G, D)$

$$= -2\log(2) + 2\text{JSD}(P_{data}(x) || P_G(x))$$

$$V = \mathbb{E}_{x \sim P_{data}} [\log D(x)] \\ + \mathbb{E}_{x \sim P_G} [\log(1 - D(x))]$$

|

Summary:

- ▶ Generator G , Discriminator D
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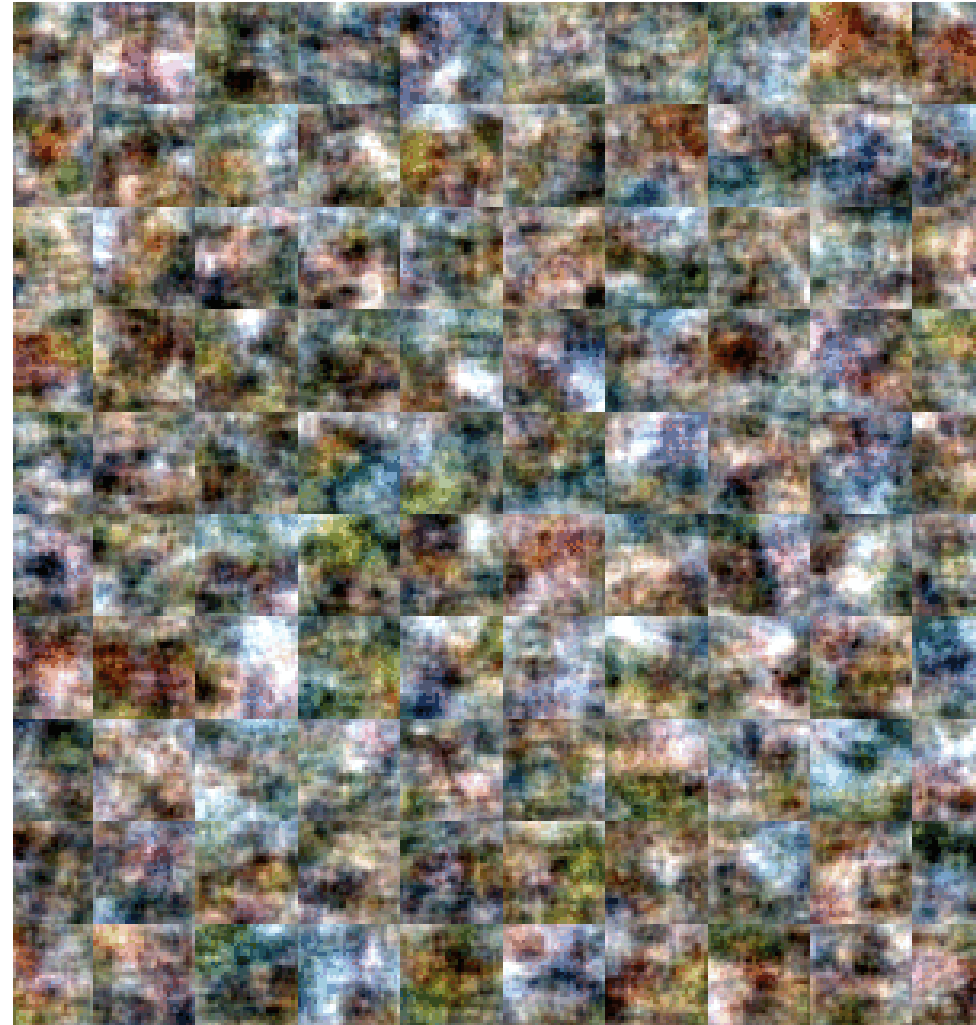
$$= -2\log(2) + 2JSD(P_{data}(x) || P_G(x))$$

- ▶ What is the optimal G ? It is G that makes JSD smallest = 0:

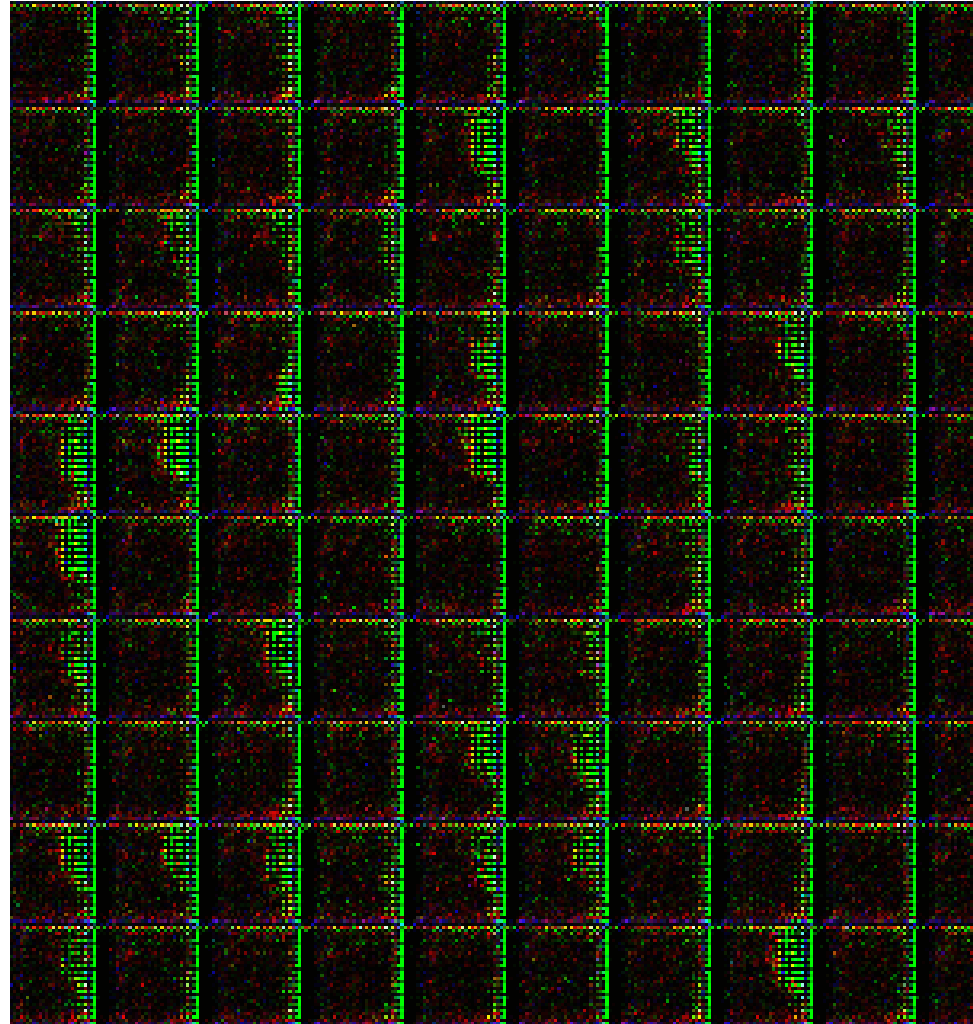
$$P_G(x) = P_{data}(x)$$

$$V = \mathbb{E}_{x \sim P_{data}} [\log D(x)] \\ + \mathbb{E}_{x \sim P_G} [\log(1 - D(x))]$$

VAE



GAN



VAE



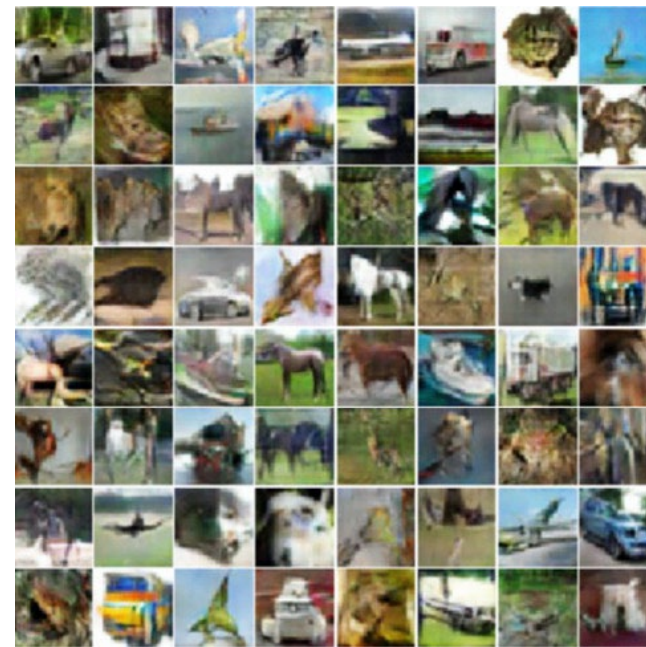
GAN



Real images (CIFAR-10)



Generated images



Source Code

- Original paper (theano):
 - <https://github.com/goodfeli/adversarial>
- Tensorflow implementation:
 - <https://github.com/ckmarkoh/GAN-tensorflow>

Conditional GAN, Mode Collapse, AAE and Applications of GAN

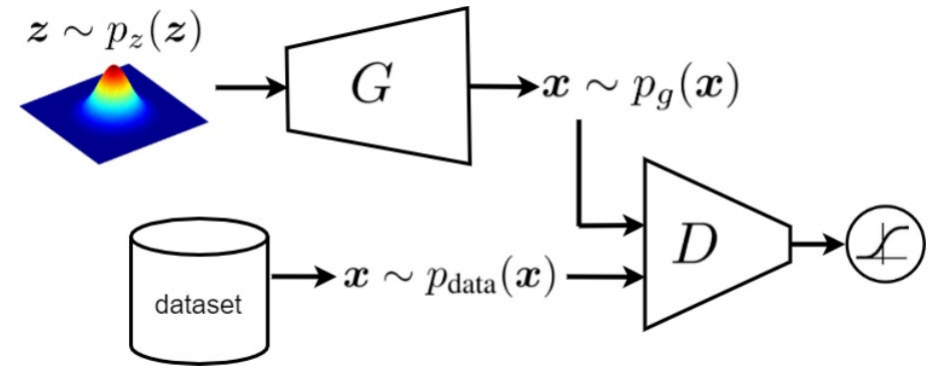
- Tutorial

[Generative Adversarial Networks and Adversarial Autoencoders: Tutorial and Survey](#)

Generative adversarial network (GAN)

$$\min_G \max_D V(D, G)$$

$$V(D, G) = \mathbb{E}_{x \sim P_{data}(x)} [\log D(x)] + \mathbb{E}_{z \sim P_z(z)} [\log(1 - D(G(z)))]$$



Mode Collapse Problem in GAN

- The mode collapse problem (Metz et al., 2017), also known as the Helvetica scenario (Goodfellow, 2016), is a common problem in GAN models.

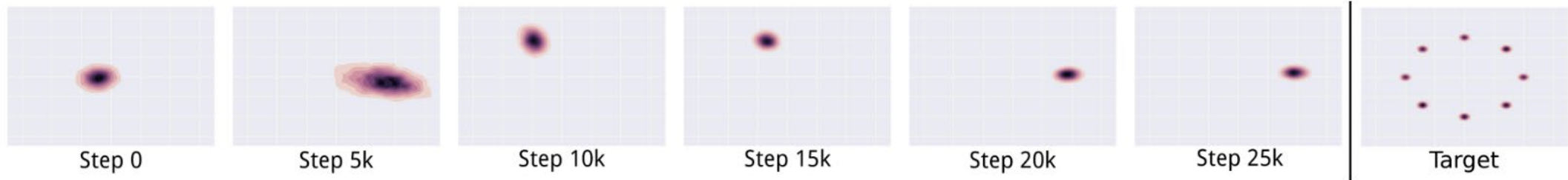
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- The generator learns to map several different z values to the same generated data point x .

Mode Collapse Problem in GAN

- The mode collapse problem (Metz et al., 2017), also known as the Helvetica scenario (Goodfellow, 2016), is a common problem in GAN models.
- The generator learns to map several different z values to the same generated data point x .
- Mode collapse usually happens in GAN when the distribution of training data, $p_{data}(x)$, has multiple modes.

Mode Collapse example



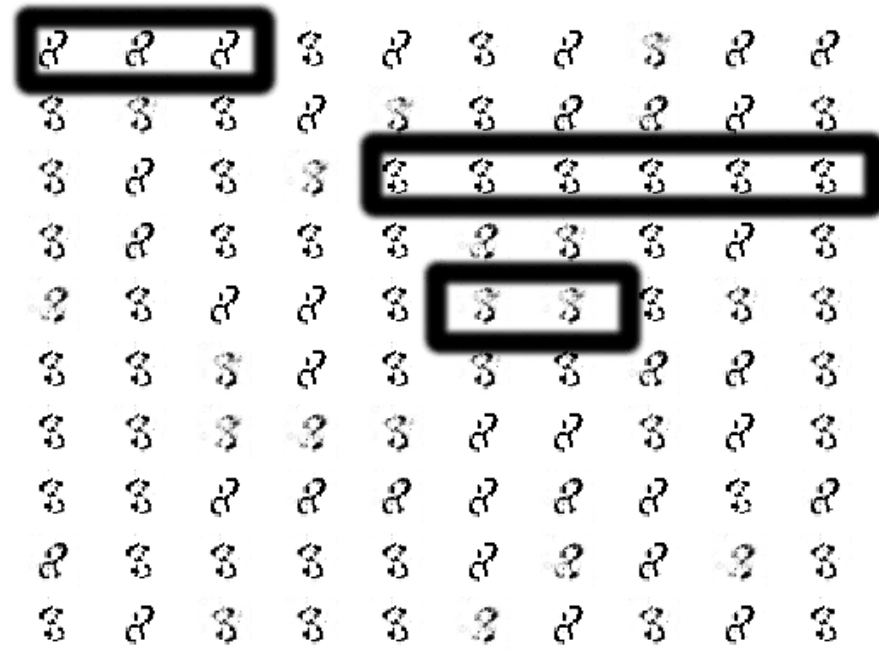
An example of mode collapse in GAN.

Credit : Metz et al., 2017

Mode Collapse example

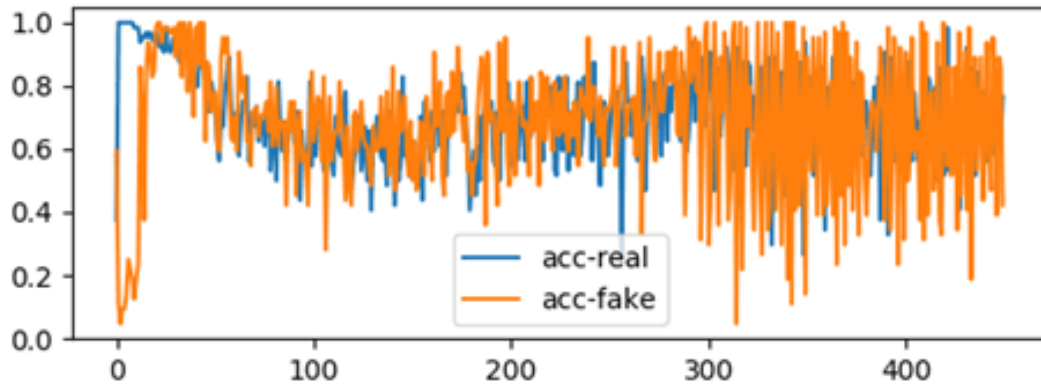


Stable GAN

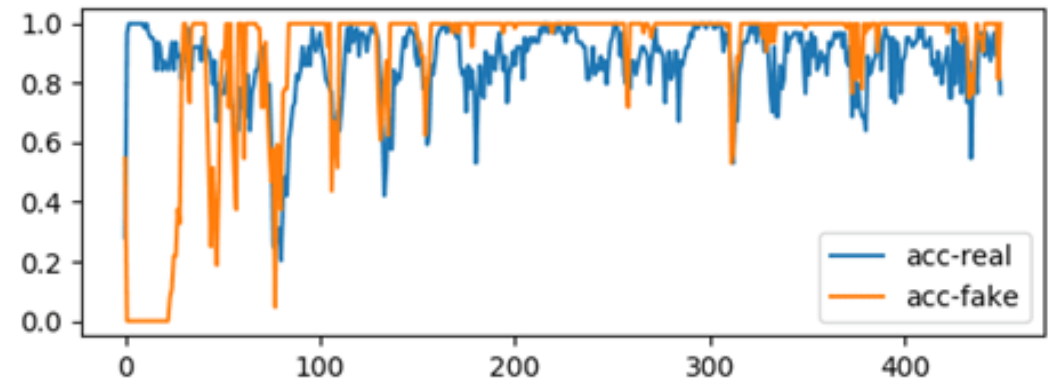


Mode Collapse.

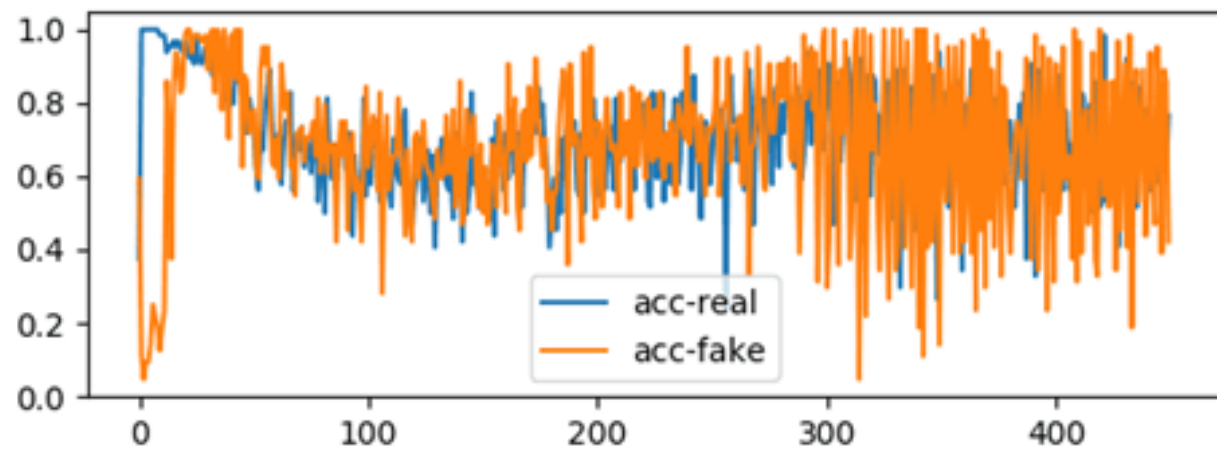
Mode Collapse example



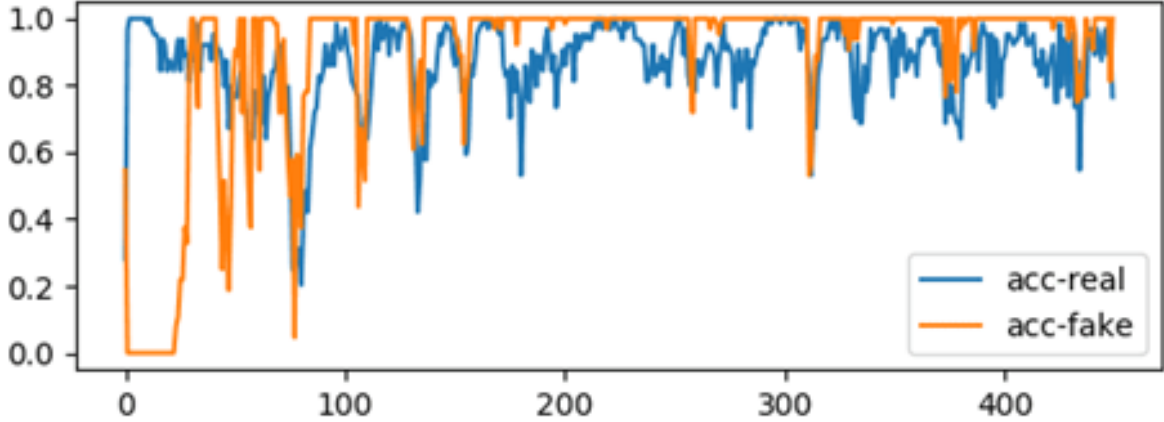
Accuracy for a Stable GAN



Accuracy for a GAN with Mode Collapse



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Minibatch discrimination

- One way to resolve the mode collapse problem is minibatch discrimination (Salimans et al., 2016)

Minibatch discrimination

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- One way to resolve the mode collapse problem is minibatch discrimination (Salimans et al., 2016)
- When mode collapses, all images created look similar.
- Feed real images and generated images into the discriminator separately in different batches and compute the similarity of the image x with images in the same batch.

Minibatch discrimination

- Append the similarity $o(x)$ in one of the dense layers in the discriminator to classify whether this image is real or generated.

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Minibatch discrimination

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- If the mode starts to collapse, the similarity of generated images increases.
- The discriminator can use this score to detect generated images and penalize the generator if mode is collapsing.

Alternative Strategies to Prevent Mode Collapse

- **Unrolled GANs:** They allow the generator to update itself using a copy of the discriminator from several steps ahead, preventing the generator from overfitting to the current discriminator.
- **Experience Replay:** This involves keeping a memory bank of past generated images and occasionally showing them to the discriminator, which helps maintain diversity in the generator's output.
- **Modified Training Objectives:** Alternative loss functions, like Wasserstein loss or least squares loss, provide more stable gradients and can help prevent mode collapse.

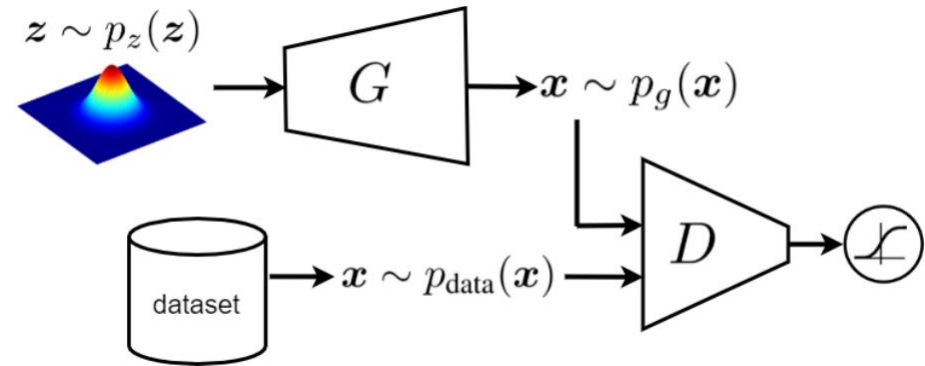
Alternative Strategies to Prevent Mode Collapse

- **Regularization:** Adding noise to inputs or labels, or using dropout in the discriminator, can prevent it from making overly confident decisions, which in turn pressures the generator to be more diverse.
- **Architecture Tweaks:** Adjusting the network architecture, such as adding more layers or changing activation functions, can help the generator explore a wider range of outputs.
- **Feature Matching:** The generator is trained to match the statistical features of the real data in some intermediate layer of the discriminator, promoting diversity in the generated data.

Alternative Strategies to Prevent Mode Collapse

- **Penalizing the Discriminator:** Introducing penalties for the discriminator when it gets too confident can prevent it from overpowering the generator, leading to a more varied generation.
- **Two Time-Scale Update Rule (TTUR):** Using different learning rates for the generator and the discriminator can help balance their training and prevent the generator from collapsing to a few modes.

Generative adversarial network (GAN)



$$\min_G \max_D V(D, G)$$

$$V(D, G) = \mathbb{E}_{x \sim P_{data}(x)} [\log D(x)] + \mathbb{E}_{z \sim P_z(z)} [\log(1 - D(G(z)))]$$

Conditional GAN

- Assume that the dataset with which GAN is trained has c number of classes.

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- The original GAN generates points from any class, and we do not have control to generate a point from a specific class.
- Conditional GAN (Mirza & Osindero), also called the conditional adversarial network, gives the user the opportunity to choose the class of generation of points.

GAN

$$\min_G \max_D V(D, G) := \mathbb{E}_{x \sim P_{data}(x)} [\log D(x)] + \mathbb{E}_{z \sim P_z(z)} [\log(1 - D(G(z)))]$$

Conditional GAN

For the dataset $\{x_i \in \mathbb{R}^d\}_{i=1}^n$, let the one-hot encoded class labels be $\{y_i \in \mathbb{R}^c\}_{i=1}^n$. In conditional GAN, we can use the following loss function instead:

$$\min_G \max_D V_C(D, G) := \mathbb{E}_{x \sim p_{data}(x)} [\log(D(x|y))] + \mathbb{E}_{z \sim p_z(z)} [\log(1 - D(G(z|y)))]$$

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Implementation of Conditional GAN

- Concatenate the one-hot encoded label y to the point x for the input to the discriminator.

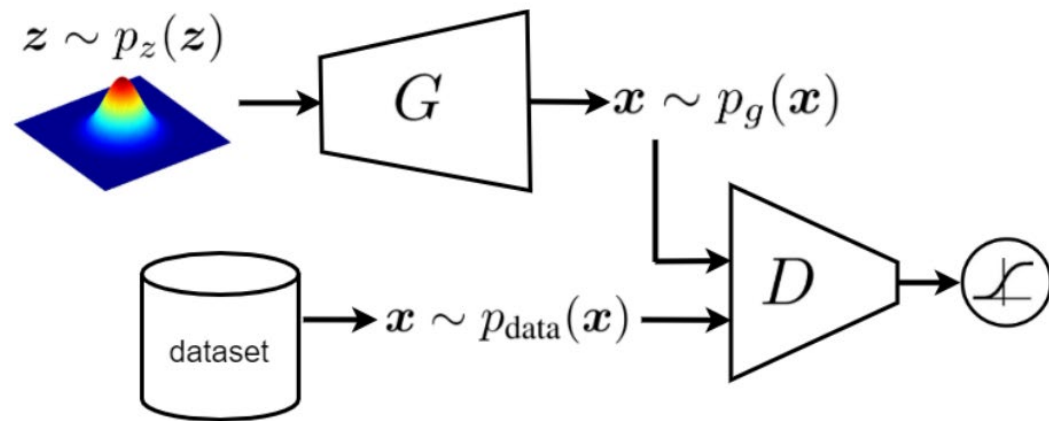
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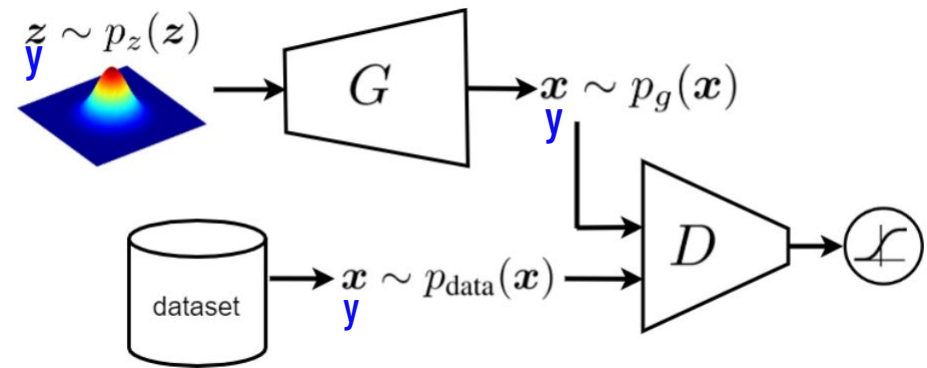
Implementation of Conditional GAN

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- For these, the input layers of discriminator and generator are enlarged to accept the concatenated inputs

GAN

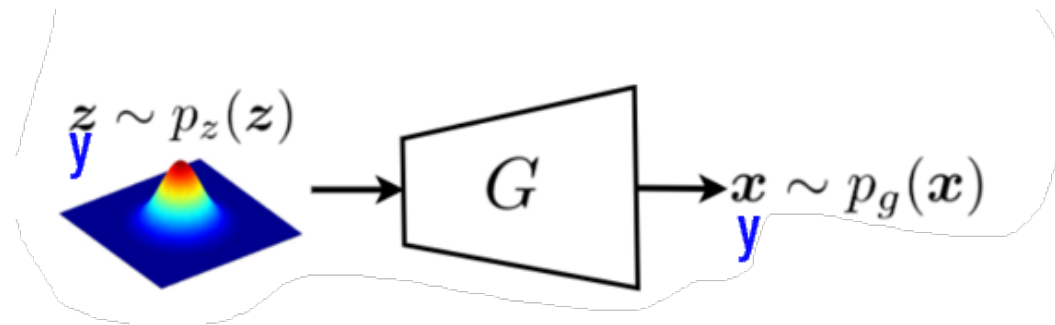


Conditional GAN



Inference from Conditional GAN

- In the inference phase, the user choose the desired class label and the generator generates a new point from that class.





Generated MNIST digits, each row conditioned on one label

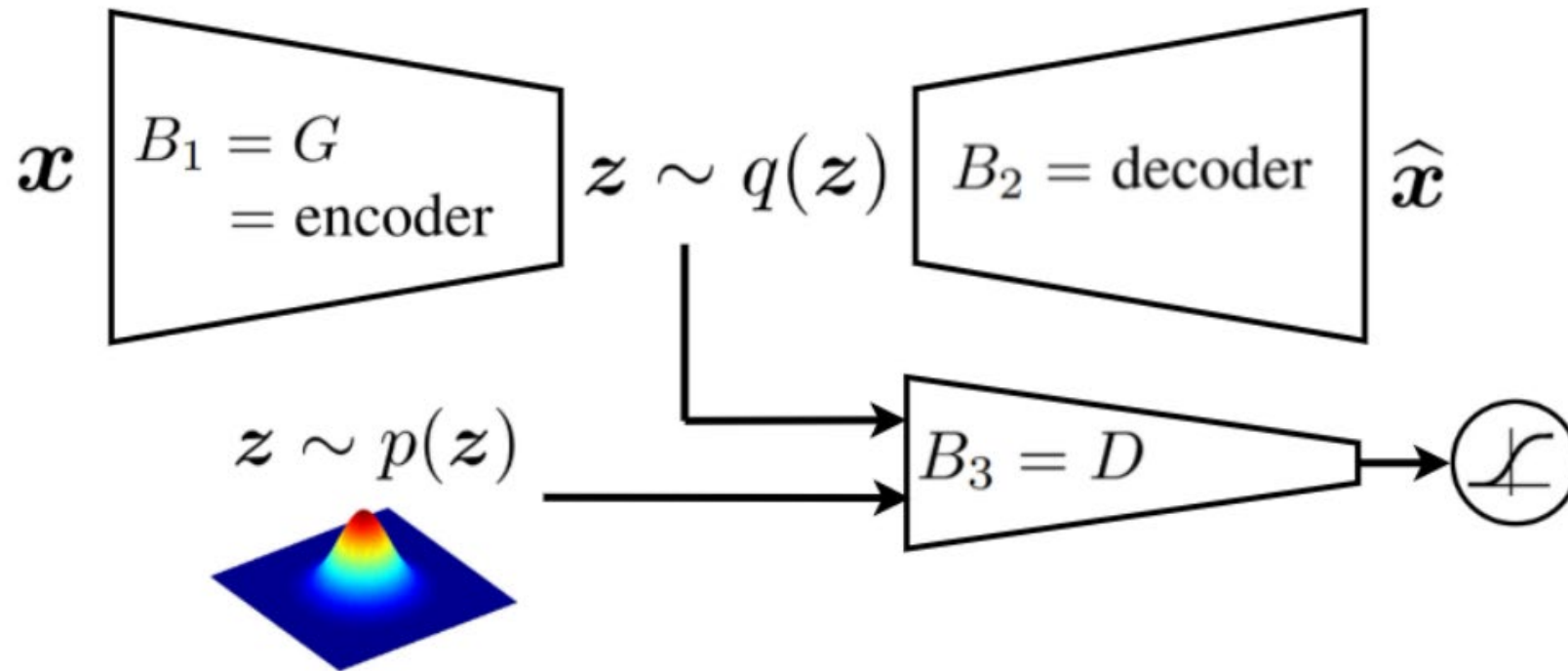
Adversarial Autoencoder (AAE)

- Adversarial Autoencoder (AAE) was proposed in (Makhzani et al., 2015).

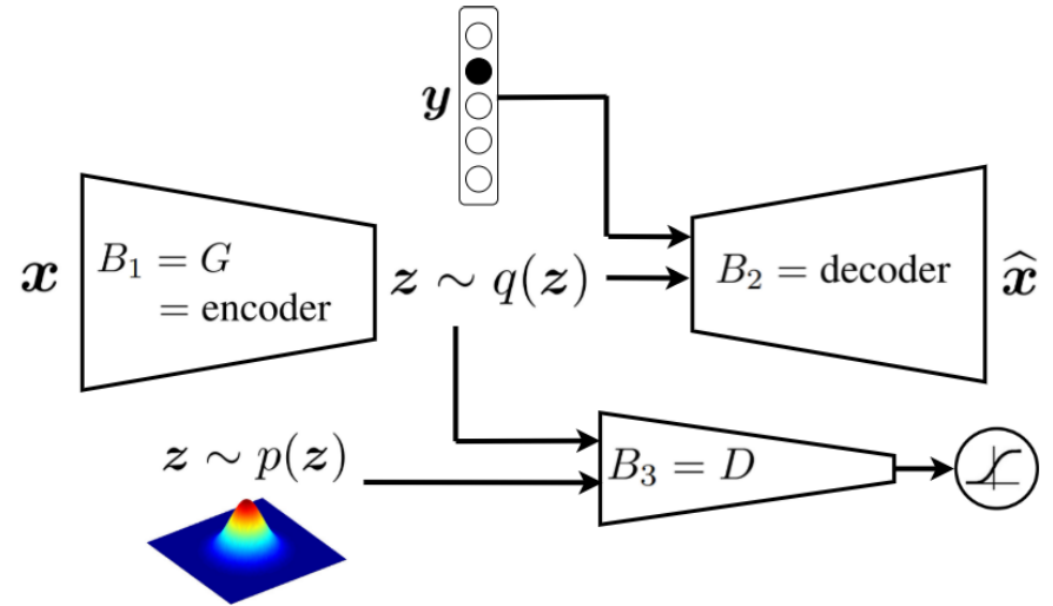
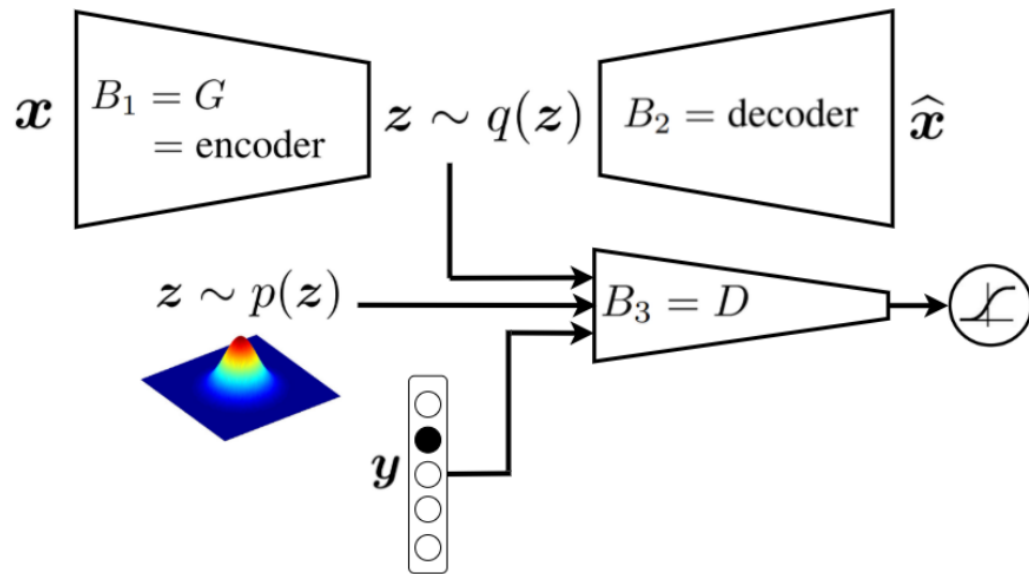
Adversarial Autoencoder (AAE)

- Adversarial Autoencoder (AAE) was proposed in (Makhzani et al., 2015).
- In contrast to variational autoencoder (Kingma & Welling, 2014) which uses KL divergence and evidence lower bound, AAE uses adversarial learning for imposing a specific distribution on the latent variable in its coding layer.

Unsupervised AAE



Supervised AAE



Clustering with AAE

- Assume we have c number of clusters.

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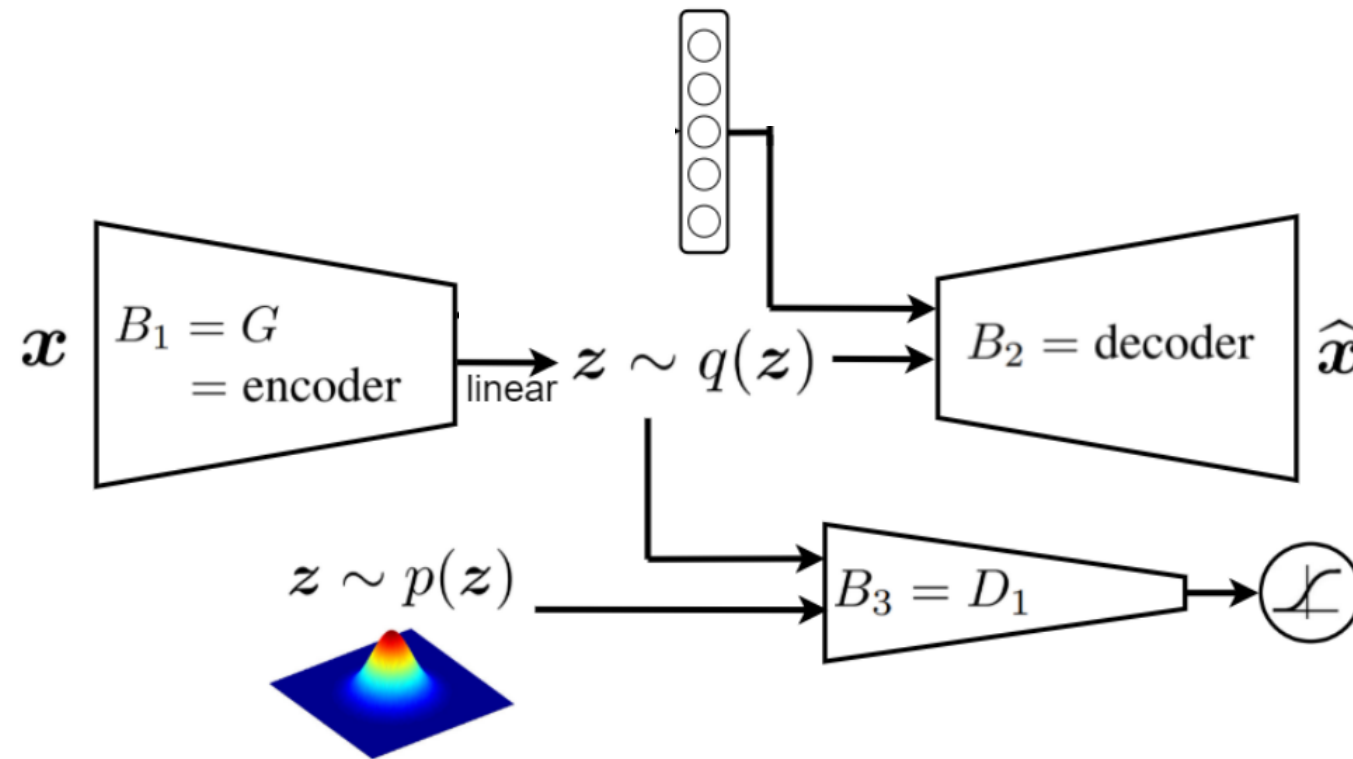
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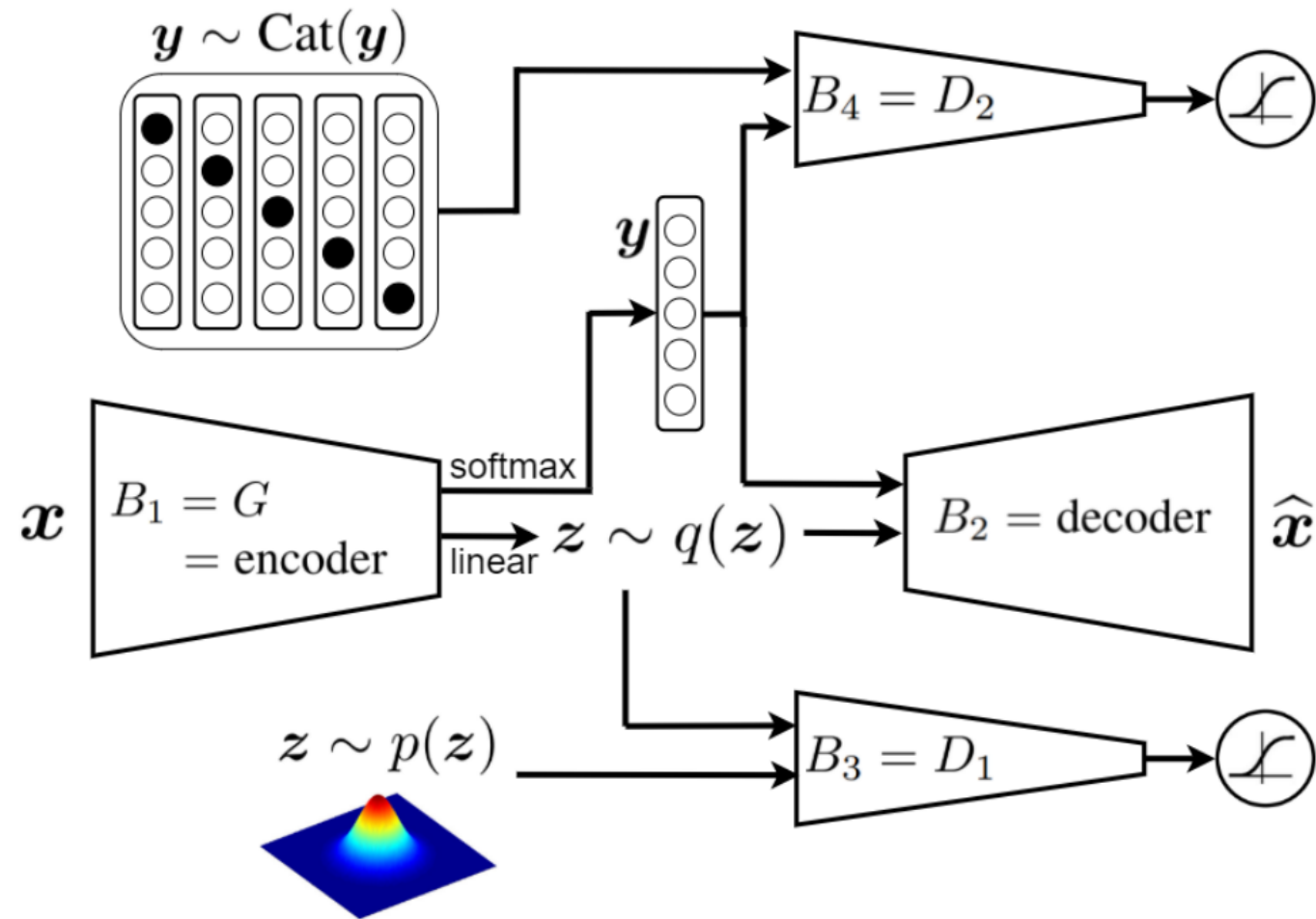
Clustering with AAE

- Assume we have c number of clusters.
- All points are unlabeled.
- The cluster indices are sampled randomly by the categorical distribution.
- The cluster labels and the latent code are both trained.

Supervised AAE



Clustering with AAE



Semi-Supervised AAE

- Consider a partially labelled dataset.

Semi-Supervised AAE

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- The labelled part of data has c number of classes.

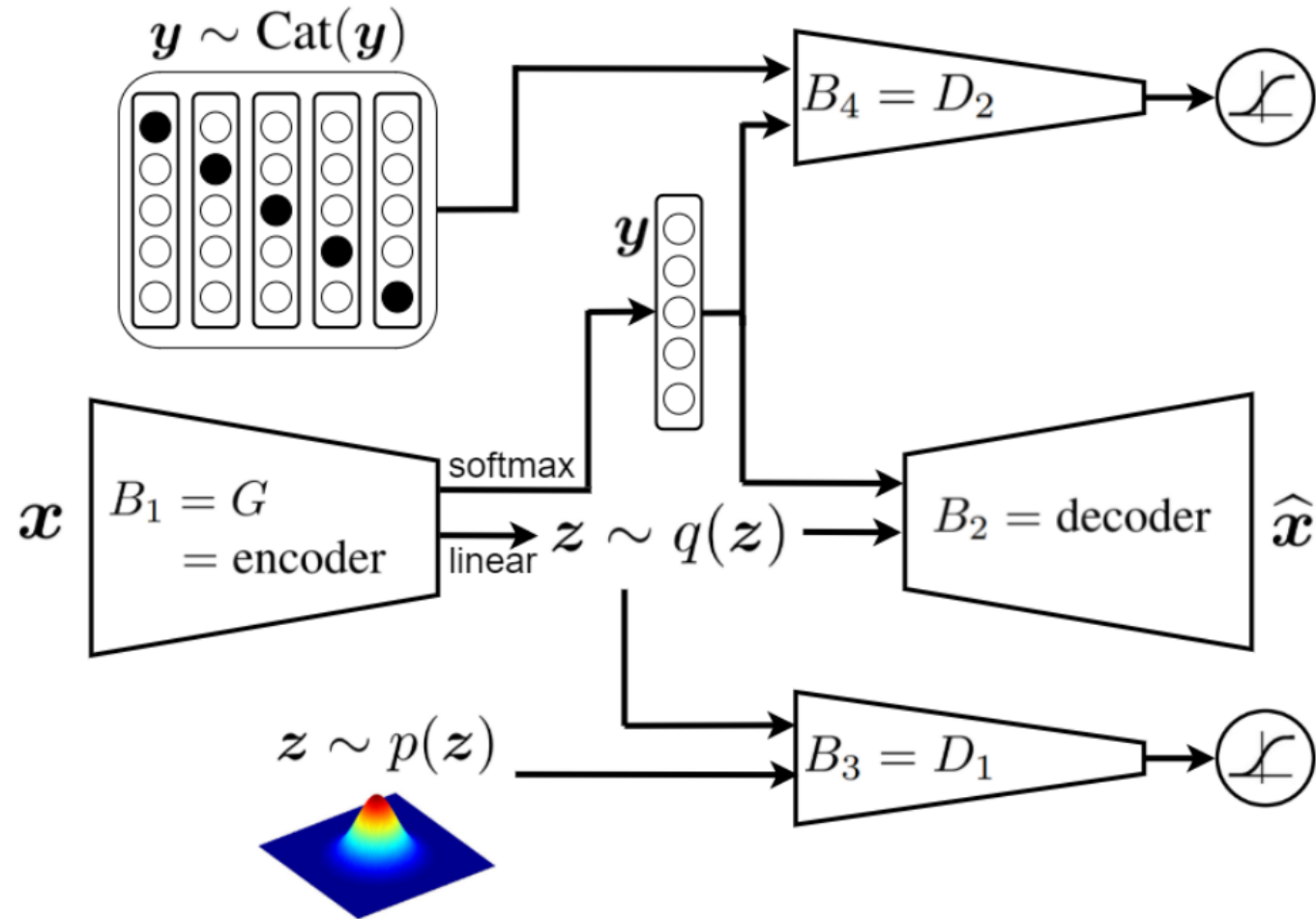
Semi-Supervised AAE

- Consider a partially labelled dataset.
- The labelled part of data has c number of classes.
- AAE can be used for semi-supervised learning with the partially labelled dataset.

Semi-Supervised AAE

- We can use the same structure for Semi-Supervised.
- But rather than the clusters, we assume we have c number of classes.
- We have a partially labelled part of the dataset.

Semi-Supervised AAE



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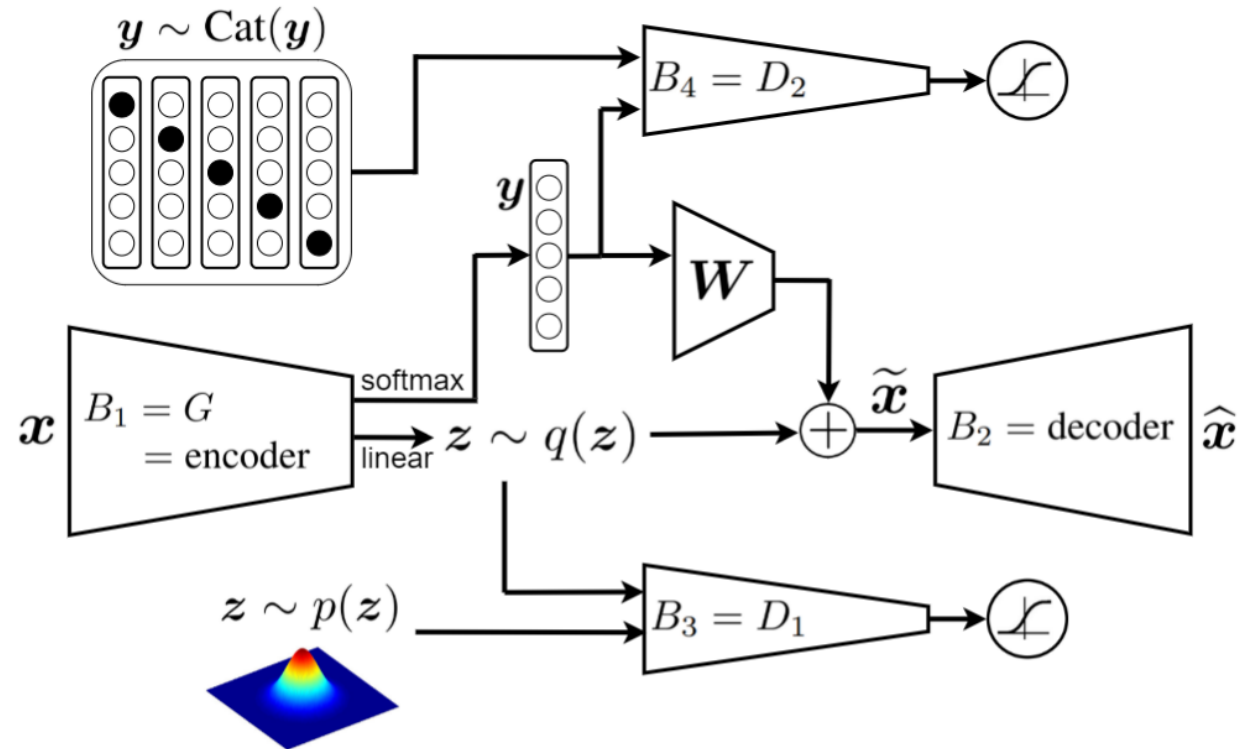
Semi-Supervised AAE

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- This categorical distribution gives a one-hot encoded vector where the prior probability of every class is estimated by the proportion of the class's population to the total number of labelled points.

Dimensionality Reduction with AAE

The low-dimensional representation of $\tilde{\mathbf{x}} \in \mathbb{R}^p$ is obtained as:

$$\tilde{\mathbf{x}} = \mathbf{W}^T \mathbf{y} + \mathbf{z},$$



Applications

Application: Image-to-Image Translation by GAN

- Interactive GAN (iGAN) (Zhu et al., 2016)
- PatchGAN (Isola et al., 2017)
- CycleGAN (Cycle-Consistent Generative Adversarial Networks) (Zhu et al., 2017)
- Simulated GAN (SimGAN) (Shrivastava et al., 2017)
- DeepFaceDrawing (Chen et al., 2020)



(a)



(b)



(c)



(d)

PatchGAN: (a) coloring a sketch, (b) changing daylight to night darkness in image, (c) changing an aerial image to a map, (d) coloring a black-and-white image,



Transforming zebra to horse and vice versa

CycleGAN

Credit: (Zhu et al., 2017)



Generating a facial image from a facial sketch.

DeepFaceDrawing

Credit: (Chen et al., 2020)

Application: Text-to-Image Generation

- Image is generated from some descriptive caption.

Application: Text-to-Image Generation

- Image is generated from some descriptive caption.
- Reed et al., 2016a;b
- Zhang et al., 2017
- Reed et al., 2017
- Nguyen et al., 2017a
- Zhang et al., 2018

This bird is red and brown in color, with a stubby beak.



This small bird has a white breast, light grey head, and black wings and tail.



StackGAN
Credit: Zhang et al., 2017

Application: Mixing Image Characteristics

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- FineGAN (Singh et al., 2019)
 - An unsupervised GAN model which disentangles the features of the generated image to background, shape, and color/texture.
 - FineGAN generates an image hierarchically. It starts with generating the background.

- MixNMatch (Li et al., 2020)

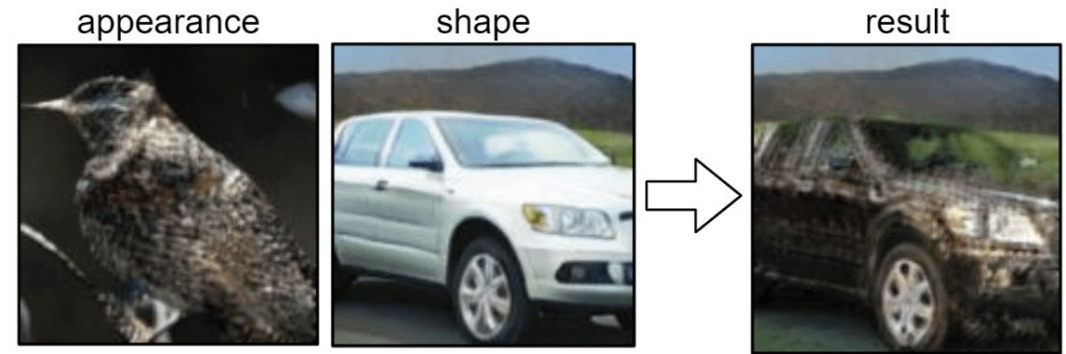
- MixNMatch (Li et al., 2020)
 - built upon FineGAN

- MixNMatch (Li et al., 2020)
 - built upon FineGAN
 - It gives the user the opportunity to choose the background, shape, and colour/texture from three pictures and it generates an image with the chosen characteristics.



generating an image by borrowing its characteristics from three images using MixNMatch

Credit: Li et al., 2020



generating an image by borrowing its characteristics from different domains using improved MixNMatch.

Credit: Ojha et al., 2021b

Other Applications

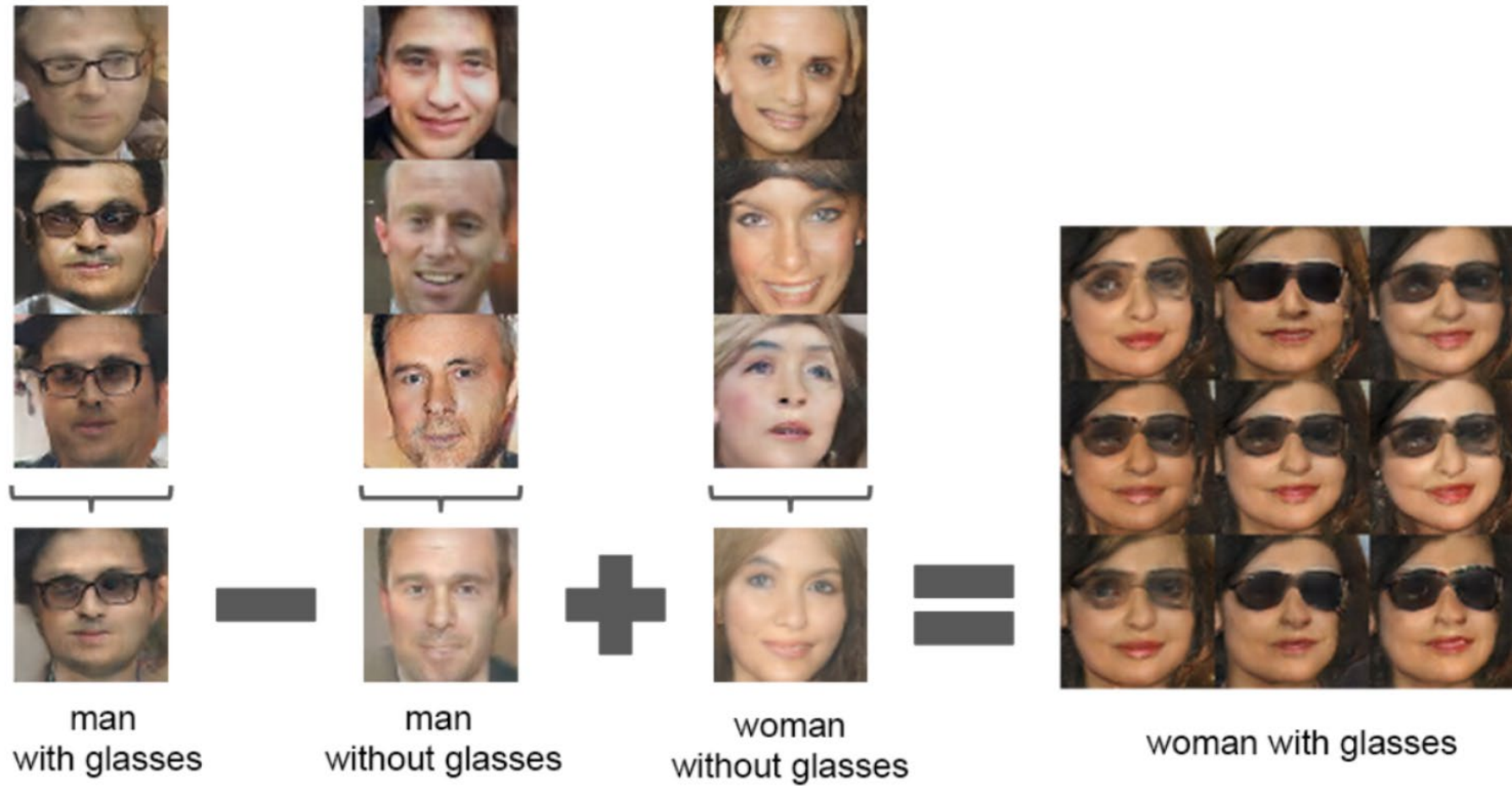
- In some structures of GAN, learned latent space is meaningful and we can do vector arithmetic in the latent space.

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- In some structures of GAN, learned latent space is meaningful and we can do vector arithmetic in the latent space.
- For example in Deep Convolutional GAN (DCGAN), proposed in (Radford et al., 2016)
- DCGAN uses an all-convolutional network for both generator and discriminator.



Vector arithmetic in the latent space on images by DCGAN.

Credit of image : Radford et al., 2016

Other Applications

- Inpainting

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- Inpainting
 - (Pathak et al., 2016). GAN learns to inpaint the lost part based on the available pixels in the image.
- Medical application
 - Generating histopathology images which can give insight into cancer diagnosis from pathology whole slide images (Levine et al., 2020).

Other Applications

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- Speech processing (Pascual et al., 2017; Sriram et al., 2018)
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- Logic (Nagisetty et al., 2021)
- Sketch retrieval (Creswell & Bharath, 2016).

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Important papers on GAN

- Original paper
[Generative Adversarial Networks](#)
- Tutorial
[Generative Adversarial Networks and Adversarial Autoencoders: Tutorial and Survey](#)
- DCGANs
[Unsupervised Representation Learning with Deep Convolutional Generative Adversarial Networks](#)

- Improved Techniques for Training GANs

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- Conditional GANs

[Conditional Generative Adversarial Nets](#)

Important papers on GAN

- Progressively Growing GANs
[Progressive Growing of GANs for Improved Quality, Stability, and Variation](#)
- BigGAN
[Large Scale GAN Training for High Fidelity Natural Image Synthesis](#)
- StyleGAN
[A Style-Based Generator Architecture for Generative Adversarial Networks](#)

- CycleGAN

[Unpaired Image-to-Image Translation using Cycle-Consistent Adversarial Networks](#)

- Pix2Pix

[Image-to-Image Translation with Conditional Adversarial Networks](#)

- StackGAN

[StackGAN: Text to Photo-realistic Image Synthesis with Stacked Generative Adversarial Networks](#)