Efficient Location-aware Web Search

J. Shane Culpepper

Department of Computer Science and Information Technology, RMIT University, Australia.

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Efficient, Scalable Algorithm Design

- Create new algorithms and data representations to support efficient query processing (verbose queries).
- Extend and refine in-memory indexing algorithms to support parallel, distributed, and dynamic indexing of massive data sets more efficiently.
- Search algorithms.
 Search algorithms.
- Investigate new approaches to combining structured and unstructured search.
- **5** Develop and understand IR evaluation best practices.

- Energy costs can now exceed hardware costs in many "big data" applications.
- 2 Every 100 ms boost in search speed increases revenue by 0.6% at Bing.[†]
- 3 Commodity computer systems can now support over 1 TB RAM and 40+ CPU cores in a single machine, but trends in practical algorithmic design have not mirrored these advances.

[†] R. Kohavi, A. Deng, B. Frasca, T. Walker, Y. Xu, and N. Pohlmann: "Online controlled experiments at large scale." In Proc. KDD, pages 1168–1176, 2013.

State-of-the-Art in GOV2



Data from the RIGOR Workshop at SIGIR 2015. All systems are ran on a single EC2 instance using the TREC GOV2 collection with queries 701-850. More at http://github.com/lintool/IR-Reproducibility.

Multi-Stage Retrieval



Bing – Sequence of select, rank, prune steps

- L0 Boolean Logic
- L1 BOW IR Scoring
- L2/L3/L4 Learning to Rank

1. Burges et al. "Learning to Rank Using Gradient Descent." In ICML 2005. 2. Jan Pedersen: "Query Understanding at Bing." SI-GIR Industry Keynote, 2010.

The Inverted Index



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- Score-safe processing guarantees that an identical top-*k* ordering will occur for a given set ranking metric.
 - MAXSCORE
 - WAND
 - BLOCK-MAX

• Heuristic processing approximates the true top-k list.

- STOP and CONTINUE
- SCORE-AT-A-TIME / impact ordered indexing

Weak AND, or Weighted AND - WAND

Given a list of Boolean variables X_1, X_2, \ldots, X_t and a list of associated positive *weights*, w_1, w_2, \ldots, w_t and a threshold θ , WAND $(X_1, w_1, \ldots, X_t, w_t, \theta)$ is true iff

$$\sum_{|\leq i\leq t} x_i w_i \geq \theta,$$

where x_i is the indicator variable for X_i , that is

$$x_i = \begin{cases} 1 & \text{if } X_i \text{ is true} \\ 0 & \text{otherwise.} \end{cases}$$

A. Z. Broder, D. Carmel, H. Herscovici, A. Soffer, and J. Zien: "Efficient query evaluation using a two-level retrieval process." In Proc. CIKM, pages 426–434, 2003.

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 $\sum U_i > \theta$ $1 \le i \le t$

- Assume the Ut is the maximum score a term t ∈ q can contribute in an additive scoring regime.
- If we set θ to the current score of the k·th smallest item in a heap of k items, only items that *might* be able to enter the heap will ever be scored.
- If we set $\theta = \infty$, then only the first k items evaluated can ever enter the heap.
- By varying the threshold, WAND can move from being close to an **OR** operation to being close to an **AND** operation.

How to use WAND (Sketch)

Index Time:

- 1 Pick an additive ranking metric and build a document ordered inverted index.
- 2 For each inverted list, pre-calculate a value U_t which represents the maximum contribution term t can have for that scoring metric.

Query Time:

- 1 Perform a standard *document-at-a-time* traversal with one twist.
- 2 Set a *finger* pointing to the first unevaluated document in each list.
- 3 Set the term processing order of the lists using the document id smallest to largest.
- 4 While the sum of the U_t values are less than θ step to the next list.
- 6 As soon as we exceed θ, the document ID in the current list is selected as the *pivot*.
- 6 A finger search is initiated for all lists evaluated before the pivot, and the current pivot document ID is scored if all of the previous list document IDs match the pivot.
- 7 If the real document score exceeds the minimum value in a k heap, it is added to the heap, and θ is set to the new minimum heap score.

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BM-WAND in action



2. S. Ding and T. Suel: "Faster top-k retrieval using block-max indexes." In Proc. SIGIR, pages 993–1002, 2011.

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- Recent talks at SIGIR and CIKM have highlighted the fact that the number of mobile searches have surpassed the number of desktop searches in all of the major search engines.
- For mobile searches, more than 50% of all queries have local intent.
- Leveraging GPS data for search is now a key feature in mobile applications.
- We know that the interaction between 10s or even 100s of features improves effectiveness. There is value in studying important features in isolation to better understand when and where they work best.

Two common spatial queries:

- Range query Given a location *p* and a maximum travel distance, a range query returns all items whose location fall within that distance from *p*. An example of a spatial range query is when a user wants to find all of the petrol stations within 5 km of their current location.
- KNN query Given a specific location *p*, the query returns the *k* items closest to *p*.

Two common textual queries:

- - $t_1 \dots t_q$, return all documents containing all terms.
- **Disjunctive Boolean (OR) query** Given a set of query terms $t_1 ldots t_q$, return all documents containing any of the terms.

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Research Question 1: Which indexing approaches provide the best efficiency trade-offs for bag-of-words, top-*k knn* search in large document collections?

Research Question 2: What are the efficiency and effectiveness trade-offs for the two most common spatially constrained query types when applied to bag-of-words, location-aware search?

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- Filter-based Methods Apply a spatial filter (KNN or MBR) to identify a subset of candidate documents. Reorder the documents using a textual similarity function to get the final top-*k* document list.
 - Use an R-Tree to do efficient range filtering.
 - Use a KD-Tree or an R*-Tree to do efficient KNN filtering.
 - Score the filter set using BM25 or any TF-IDF ranking metric.
- **Top-***k* **KNN Methods** Score the top-*k* documents in a single pass using both components to prune to search space.
 - Use a hybrid index such as an IR-Tree.
 - Use an augmented inverted index.



Fig. 4. An example IR-tree. (a) IR-tree content. (b) Node MBBs.

G. Cong, C. S. Jensen, and D. Wu: "Efficient retrieval of the top-k most relevant spatial web objects." PVLDB, 2(1):337348, Aug. 2009.

Z. Li, K. C. K. Lee, B. Zheng, W.-C. Lee, D. Lee, and X. Wang: "IR-tree: An efficient index for geographic document search." TKDE, 23(4):585599, Apr. 2011.

Spatial-Textual Ranking

Given a spatial-textual query q and a document d, the spatial-textual similarity can be computed as:

$$S(q, c) = \alpha \cdot \beta(\ell_q, \ell_d) + (1 - \alpha) \cdot \sum_{t \in q} \gamma_t$$

where $\beta(\ell_q, \ell_d)$ is the spatial similarity, γ_t is the textual similarity, and $\alpha \in (0, 1)$ is a parameter that can be used to add weight the importance of the two components.

•
$$\beta(\ell_q, \ell_d) = (1 - \frac{\text{Euclidean}(\ell_q, \ell_d)}{d_{\max}}) \cdot \sum_{t \in q} U(\gamma_t)$$

- In this work, γ_t is the BM25 ranking function. However, any TF-IDF scoring function could be used.
- This is referred to as a top-*k knn* query.

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Algorithm 2: WAND processing with geospatial weights, replacing steps 10–21 in Algorithm 1 of Petri et al. [23].

2.1
$$text_limit \leftarrow 0$$
; $spatial_limit \leftarrow 0$; $pivot \leftarrow 0$
2.2 while $pivot < |q| - 1$ do
2.3 $text_limit \leftarrow text_limit + (1 - \alpha) \cdot U[pivot]$
2.4 $spatial_limit \leftarrow spatial_limit + \alpha \cdot U[pivot]$
2.5 if $text_limit + spatial_limit > \theta$ then
2.6 $| s \leftarrow text_limit + spatial_limit$
2.7 $| break, and continue from Step 2.9.$
2.8 $pivot \leftarrow pivot + 1$
2.9 if $c_0 = c_{pivot}$ then
2.10 $t \leftarrow 0$
2.11 $s \leftarrow s - spatial_limit + \alpha \cdot \beta(\ell_q, \ell_{pivot})$
2.12 while $t < |q| - 1$ and $c_0 = c_{pivot}$ do
2.13 $s \leftarrow s - (1 - \alpha) \cdot U[t] + (1 - \alpha) \cdot \gamma_t$
2.14 $| if s < \theta$ then
2.15 $| break, and reset all pointers to c_{pivot} + 1.$
 \triangleright Update heap and $\theta \dots$ remaining computation similar to the approach described in Algorithm 1 of of Petri et al. [23].

Spatial datasets



- WIKIGEO 1 Million Geotagged Documents (9 GB Uncompressed)
- CW09BGE0 24 Million Geotagged Documents (230 GB Uncompressed)

Collection Creation

- Used a combination of the GeoNames gazetteer and the Freebase annotations for the ClueWeb Corpora.
- We also used the TREC Freebase parse of the Million query track.
- If multiple locations were found in a document, we used the first one.
- If multiple locations were in a query, we replicated the query, once for each location.
- For documents, many were clustered on one exact location (New York). So, we also did location fuzzing where we randomly added a very small epsilon to the Latitude / Longitude coordinates.
- This produced 24 million unique, geotagged documents, and 5,315 geotagged queries.
- A subset of the main collection was created by taking the first million documents that were ordered by spam score, many of which turned out to be Wikipedia documents.

Systems Evaluated

System	Abbreviation
Standard WAND (text only)	W
GeoWAND	G-W
IR-Tree	IR
R*-Tree (<i>knn</i> queries)	W-R*
<i>kd-</i> Tree (<i>knn</i> queries)	W-kd
R*-Tree (1km MBR queries)	MBR-1
R*-Tree (10km MBR queries)	MBR-10
R*-Tree (100km MBR queries)	MBR-100

Table: System configurations in all experiments. The W-R^{*}, W-kd, and MBR-*k* methods all use WAND over an inverted index to rank queries once the spatial filtering has finished. The W-R^{*} and W-kd methods retrieve the $2.5 \times k$ closest documents before reording.

Experiment - WIKIGEO Performance



Figure 4: The mean running time per query as a function of k for all query type and index combinations on the WIKIGEO dataset, with $\alpha = 0.5$.

Experiment - WIKIGEO Index Size



Figure 3: A comparison of the space usage for a GEOWAND inverted index, a loosely coupled WAND inverted index combined with an R-Tree and *k*-d-Tree, and IR-Tree of varying fanouts. The space difference between the different WAND and GEOWAND indexes is negligible.

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Experiment - Tree Traversal



Figure 5: The cumulative number of branches evaluated for the IR-Tree traversal for $\alpha = 0.5$ on the WIKIGEO collection. The greedy search must search many more nodes as k increases, which results in a significant increase in the number of cache misses incurred when walking the tree.

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- The IR-Tree can use up to 2 times the space of the uncompressed collection.
- A WAND-based approach is around 20% of the size of the uncompressed collection.
- So, there is an order of magnitude difference in space usage between the two approaches.
- To be fair, the IR-Tree was designed to be ran on-disk, and object sizes are often much smaller than web documents.
- The vocabularies are therefore much smaller, and the pseudo nodes can be made smaller by reading only terms for the current query into memory at processing time.
- We were unable to build the IR-Tree on the full CW09BGE0 collection.

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Optimizing GEOWAND



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α	MBRF 1 km	MBRF 10 km	MBRF 100 km	$\begin{array}{l} \text{KNNF} \\ k = 10 \end{array}$	$\begin{array}{l}\text{KNNF}\\k=100\end{array}$	KNNF k = 1000	
MED _{RBP0.95}							
0.2	0.7164	0.6978	0.6601	0.9947	0.9936	0.9703	
0.5	0.5991	0.5746	0.5246	0.9921	0.9902	0.9551	
0.8	0.4412	0.4085	0.3432	0.9880	0.9849	0.9319	
MED _{ERR@20}							
0.2	0.6844	0.6646	0.6264	0.9655	0.8892	0.8746	
0.5	0.5589	0.5332	0.4825	0.9473	0.8354	0.8149	
0.8	0.4021	0.3682	0.3042	0.9220	0.7625	0.7406	

Table 3: The Maximum Expected Difference (MED) as measured with $MED_{RBP0.95}$ and $MED_{ERR@20}$. A MED value less than 0.2 is considered negligible. The higher the value, the more likely there is a noticeable effectiveness difference.



Figure 8: Effectiveness versus Efficiency for the CW09BGEO collection for $\alpha = 0.8$.

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Summary, Limitations, and Future Work

- GEOWAND is simple to implement, rank-safe, and efficient. We believe users like things as simple as possible.
- The efficiency of all of the methods can be improved by reordering documents in the collection using a Space Filling Curve.
- It is not clear how to use document reordering when documents and/or queries have multiple locations.
- Our data set is synthetic. No good publicly available test collections exist for experiments on location-aware search. We are talking to industry partners about this problem now.
- No relevance judgments are available, so we do not have good tools to evaluate new ranking algorithms combining non-textual features.
- Location is one of many important non-textual features that can be used for ranking.

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Questions?

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