# Syllabus: ECON 212 – Introduction to Game Theory Fall 2016

## Instructor:

Prof. Joel N. Blit

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## **Teaching Assistant:**

**TBD** 

#### **Objectives:**

Game Theory is the study of strategic interactions between individuals where the outcome for an individual depends not only on his choice of action but also on the actions of other players. This course is an introduction to Game Theory. We will develop game theoretic tools that can be used to analyze all sorts of situations including a game of poker, negotiations, auctions, military strategy, or the inability of the world community to curb carbon emissions. We will develop methods for determining the optimal strategies for the different players and for determining the equilibrium outcomes of games.

The course will also have a hands-on component. You will put the theory into action by playing games against fellow students. These will teach you to think strategically. But beware, theory and practice don't always line up!

## **Required Readings:**

- Martin J. Osborne. An introduction to Game Theory, Oxford University Press, 2004.
  - Partial solutions to the exercises are available at: http://www.economics.utoronto.ca/osborne/igt/index.html

## **Prerequisites:**

You will be expected to know algebra well enough to solve systems of equations. Some calculus is beneficial but not necessary.

## My Expectations:

- You will come to class and you will participate
- You will stay on top of the material
- You will participate fully in the out of class exercises and submit them on time
- You will complete the assigned problems from the book

#### Method of Evaluation:

Games (8): 20% of final grade (3%, 1%, 4%, 2%: 1%, 2%, 4%, 3%)

Midterm Examination: Date TBD (in TBD) - 30% of final grade

Final Examination: Date TBD - 50% of final grade

Participation: Exceptional participation may earn a bonus of 1%-2%

NOTE: Students who write the midterm exam but do better on the final exam will have half of the weight of the midterm shifted to the final. Thus your final mark would be 20% Games, 15% midterm, and 65% final.

Note: While the games are nominally worth 20% of the final mark, it is possible to score above 100% or below 0% in a given exercise. Thus, they could effectively contribute more than 20% to your final mark.

#### **Late Submission of Strategies for Games:**

Because of the nature of the games (each student submission plays against all others), late submissions will not be accepted and will earn a grade of 0. Failure to submit will also earn a grade of 0 for that game.

## **Absence from Exams:**

Failure to write an exam results in a grade of zero. Exceptions will only be made under the most extreme circumstances, with a written note, and according to the policies of the department of economics and faculty of Arts.

If you miss the midterm due to illness or other excused absence the 30% weight will be shifted to the final examination.

If you miss the final exam it is your responsibility to petition the department of economics as per the regulations for the opportunity to write a make-up exam.

#### **Course Outline:**

Some of the major topics covered include: strictly and weakly dominated strategies; static games of complete information (Nash equilibrium and mixed strategy equilibrium); dynamic games of complete information (subgame perfect equilibrium); and repeated games with complete information. Depending on time we may cover other topics.

The following is a tentative course schedule/outline and will be updated as we proceed through the course.

Note: Problems marked with an asterisk do not have publicly available solutions.

## Week 1: Introduction, Strategic Games

Chapter 1 and Sections 2.1-2.5

Problems:

- 16.1 Working on a joint project
- 17.1 Games equivalent to the Prisoner's Dilemma
- 20.1 Games without conflict

Game 1: Choose 2/3 of the Average is due Wednesday at 5pm Game 2: Take II: Choose 2/3 of the Average is due Sunday night

## Week 2: Nash Equilibrium, Best Response Functions, Dominated Actions

**Sections 2.6-2.9** 

Problems:

- 27.2\* Selfish and altruistic social behaviour
- 33.1\* Contributing to a public good
- 34.2\* Voter participation
- 37.1 Finding NE using best response functions
- 38.1 Constructing best response functions
- 38.2 Dividing money
- 42.1\* Finding NE using best response functions
- 42.2\* A joint project
- 47.1 Strict equilibria and dominated actions
- 47.2 NE and weakly dominated actions
- 48.1\* Voting

# Week 3: Cournot, Bertrand, Electoral Competition

Sections 3.1-3.3

Problems:

- 52.2 Equilibrium for pairwise interactions in a single population
- 58.1 Cournot game with linear inverse demand and different unit costs
- 59.2\* Cournot game with linear inverse demand and a fixed cost
- 60.2 NE of Cournot game and collusive outcomes

- 61.1\* Cournot game with many firms
- 63.1 Interaction among resource users
- 67.1 Bertrand game with constant unit cost
- 68.1 Bertrand oligopoly game
- 68.2 Bertrand duopoly game with different unit costs
- 73.1 Electoral competition with asymmetric voters' preferences
- 74.1\* Electoral competition with three candidates
- 76.1 Competition in product characteristics

Game 3: Bidding for a dollar is due Sunday night

# Week 4: Auctions

Section 3.5

# Problems:

- 84.1\* Nash equilibrium of 2<sup>nd</sup> price sealed bid auction
- 85.1 Second price sealed bid auction with two bidders
- 86.1\* Auctioning the right to choose
- 86.2 Nash equilibrium of 1<sup>st</sup> price sealed bid auction
- 87.1 First price sealed bid auction
- 88.1\* Third price auction

Game 4: All-pay auction is due Wednesday at 5pm

Game 5: Bidding for a jar of pennies is due Sunday night

## Week 5: Mixed Strategy Equilibrium

**Sections 4.1-4.5** 

Read Section 4.10

#### Problems:

- 106.2 Extensions of BoS with vNM preferences
- 110.1 Expected payoffs
- 111.1 Best responses
- 114.2\* Games with mixed strategy equilibria
- 114.3\* A coordination game
- 114.4\* Swimming with sharks
- 117.2 Choosing numbers
- 118.2\* Voter participation
- 120.2 Strictly dominating mixed strategies
- 120.3 Strict domination for mixed strategies
- 121.2\* Eliminating dominated actions when finding equilibria

# Week 6: Illustrations of Mixed Strategy Equilibrium

Sections 4.6, 4.8

#### **Problems**

- 127.2\* Incompetent experts
- 128.1\* Choosing a seller

- 132.2 Reporting a crime when the witnesses are heterogeneous
- 132.3\* Contributing to a public good

## Week 7: Midterm Feb 25th (in TBD)

## **Week 8: Extensive Games with Perfect Information**

Sections 5.1-5.4

Read Section 5.5

#### **Problems**

- 156.2\* Examples of extensive games with perfect information
- 161.1\* Strategies in extensive games
- 163.1 Nash equilibria of extensive games
- 163.2\* Voting by alternating veto
- 164.2 Subgames
- 168.1 Checking for subgame perfect equilibria
- 173.2\* Finding subgame perfect equilibria
- 173.3\* Voting by alternating veto
- 177.1\* Firm-union bargaining
- 177.3 Comparing simultaneous and sequential games

Game 6: "Choosing a quantity" is due

#### Week 9: Illustrations of Extensive Games with Perfect Information

Sections 6.1-6.2

# **Problems**

- 183.1 Nash equilibria of the ultimatum game
- 183.2 Subgame perfect equilibria of the ultimatum game with indivisible units
- 183.3\* Dictator game and impunity game
- 186.1 Holdup game
- 189.1 Stackelberg's duopoly game with quadratic costs
- 191.1\* Stackelberg's duopoly game with fixed costs
- 192.1\* Sequential variant of Bertrand duopoly game

Game 7: "Eating Cookies" is due

## Week 10: Bargaining

Section 16.1, 16.3

#### Problems:

- 468.1 Two-period bargaining with constant cost of delay
- 468.2 Three-period bargaining with constant cost of delay
- 473.1\* One-sided offers
- 473.2\* Alternating offer bargaining with constant cost of delay

## Week 11: Bayesian Games

Sections 9.1 - 9.4

#### Problems:

- 276.1 Equilibria of a variant of BoS with imperfect information
- 277.1 Expected payoffs in a variant of BoS with imperfect information
- 282.1\* Fighting an opponent of unknown strength
- 282.2 An exchange game
- 282.3\* Adverse selection
- 284.1\* Infection
- 287.1 Cournot's duopoly game with imperfect information
- 288.1 Cournot's duopoly game with imperfect information this one is optional

Game 8: "Repeated Prisoner's Dilemma" is due

# Week 12: Repeated Prisoner's Dilemma

Sections 14.1 – 14.7

## Problems:

- 429.1\* Grim trigger strategies in a general Prisoner's Dilemma
- 430.1\* Limited punishment strategies in an infinitely repeated Prisoner's Dilemma
- 431.1\* Tit-for-tat in an infinitely repeated Prisoner's Dilemma
- 431.2\* Nash equilibria of an infinitely repeated Prisoner's Dilemma

# **Economics Department Deferred Final Exam Policy**

Deferred Final Exam Policy found at <a href="https://uwaterloo.ca/economics/current-undergraduates/policies-and-resources/deferred-final-exam-policy">https://uwaterloo.ca/economics/current-undergraduates/policies-and-resources/deferred-final-exam-policy</a>.

# **Academic Integrity**

# **Discipline**

A student is expected to know what constitutes academic integrity, to avoid committing academic offences, and to take responsibility for his/her actions. A student who is unsure whether an action constitutes an offence, or who needs help in learning how to avoid offences (e.g., plagiarism, cheating) or about "rules" for group work/collaboration should seek guidance from the course professor, academic advisor, or the Undergraduate Associate Dean. When misconduct has been found to have occurred, disciplinary penalties will be imposed under Policy 71 – Student Discipline. For information on categories of offenses and types of penalties, students should refer to Policy 71 - Student Discipline. For typical penalties check Guidelines for the Assessment of Penalties (https://uwaterloo.ca/secretariat-general-counsel/policies-procedures-guidelines/guidelines/guidelines-assessment-penalties).

#### Grievance

A student who believes that a decision affecting some aspect of his/her university life has been unfair or unreasonable may have grounds for initiating a grievance. Read Policy 70 - Student Petitions and Grievances, Section 4 (https://uwaterloo.ca/secretariat-general-counsel/policies-procedures-guidelines/policy-70). When in doubt, please be certain to contact the department's administrative assistant who will provide further assistance.

#### **Appeals**

A decision made or penalty imposed under Policy 70, Student Petitions and Grievances (other than a petition) or Policy 71, Student Discipline may be appealed if there is a ground. A student who believes he/she has a ground for an appeal should refer to Policy 72, Student Appeals (https://uwaterloo.ca/secretariat-general-counsel/policies-procedures-guidelines/policy-72).

#### **Note for Students with Disabilities**

The <u>AccessAbility Services</u> office, located on the first floor of the Needles Hall extension (NH 1401), collaborates with all academic departments to arrange appropriate accommodations for students with disabilities without compromising the academic integrity of the curriculum. If you require academic accommodations to lessen the impact of your disability, please register with the AS office at the beginning of each academic term.