

Active Site Identification and Mathematical Modeling of Polypropylene Made with Ziegler-Natta Catalysts

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OUTLINE

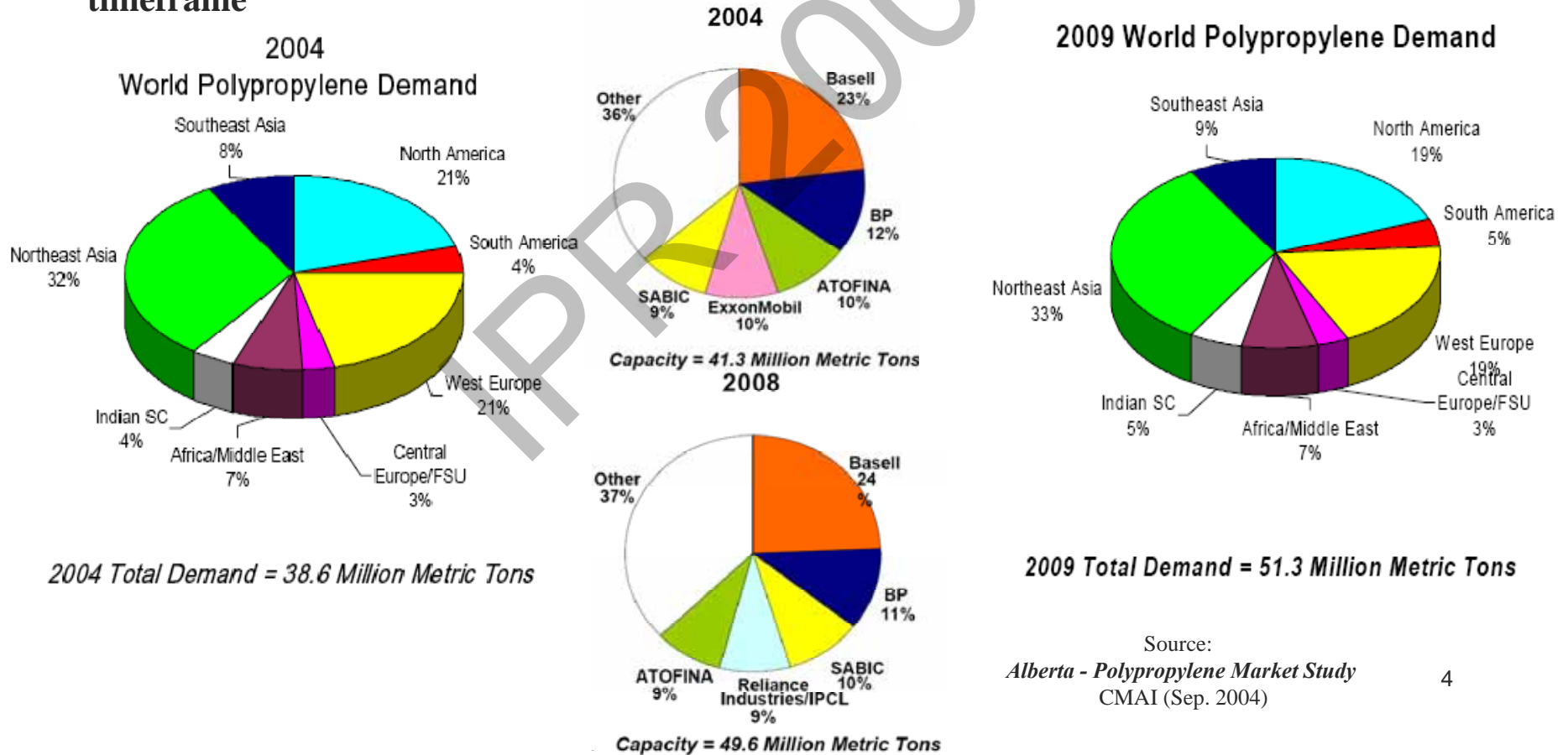
- **OBJECTIVES**
- **INTRODUCTION**
 - **Saudi Basic Industries Corporation “SABIC”**
 - **Polypropylene Facts & Figures**
 - **Polypropylene Structure**
- **MODEL & RESULTS**
 - **Population Balance and Method of Moments:**
 - ❖ **Model**
 - ❖ **Results:**
 - **Steady State vs. Dynamic CSTR’s Solutions**
 - **Monte Carlo Approach:**
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- **CONCLUSION**

OBJECTIVES

- **Develop mathematical models for the steady-state and dynamic simulation of propylene polymerization with Ziegler-Natta catalysts in industrial reactors using different modeling approaches: population balances and method of moments and the Monte Carlo techniques**
- **Describe, for the first time, site transformation by electron donors, with a mathematical model and quantify its effect on polymer chain microstructure**

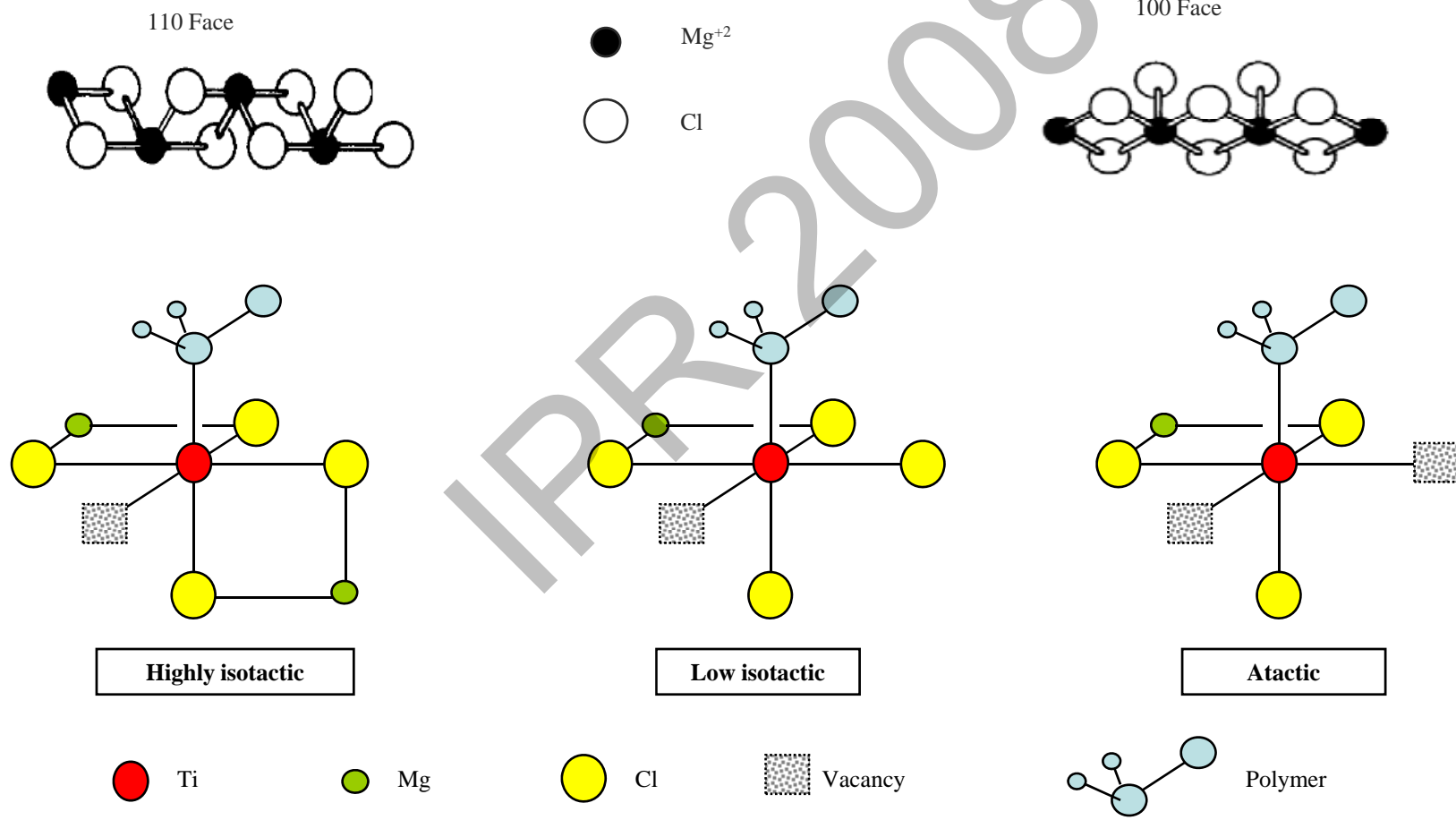
INTRODUCTION

- SABIC is the world's fourth largest producer of polyolefins. It is the world's third largest producer of polyethylene and the fifth largest producer of polypropylene.
- Overall polypropylene demand is forecasted to grow globally at a rate of 5.8% in 2004-2009 timeframe



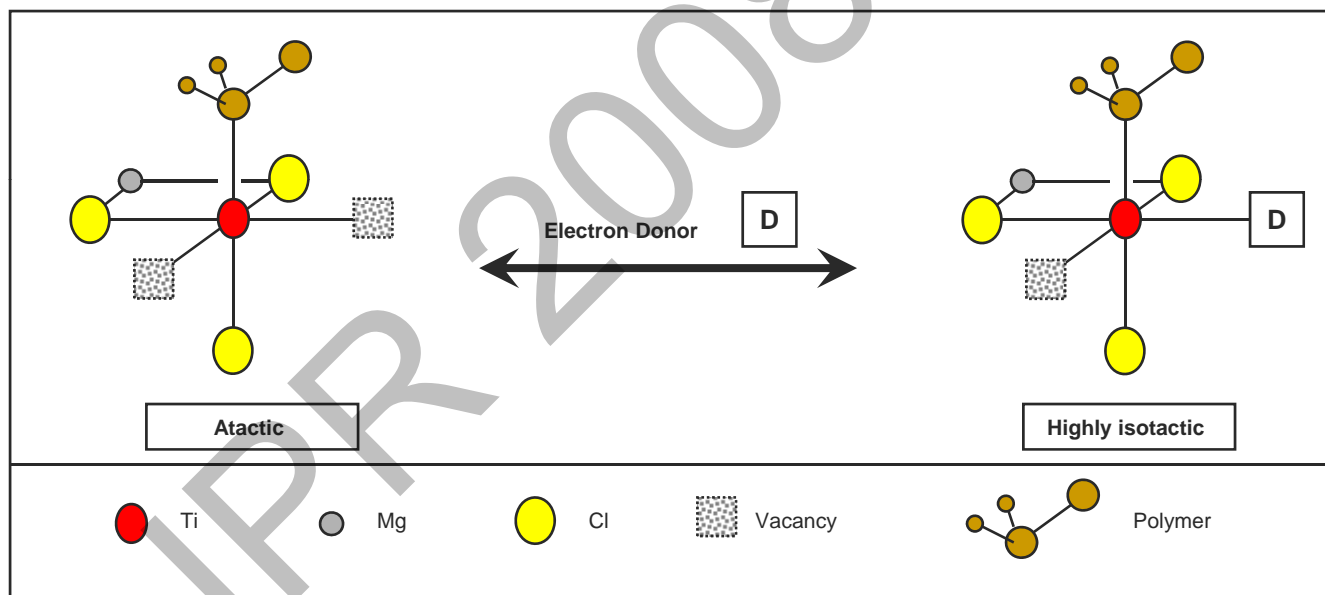
Source:
Alberta - Polypropylene Market Study
 CMAI (Sep. 2004)

Z-N Multiple Site Catalyst

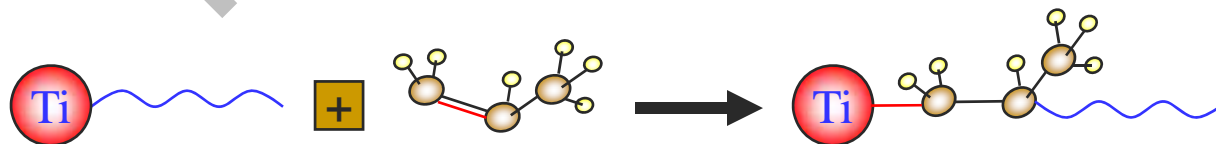


Reaction Mechanism:

➤ Site Transformation:



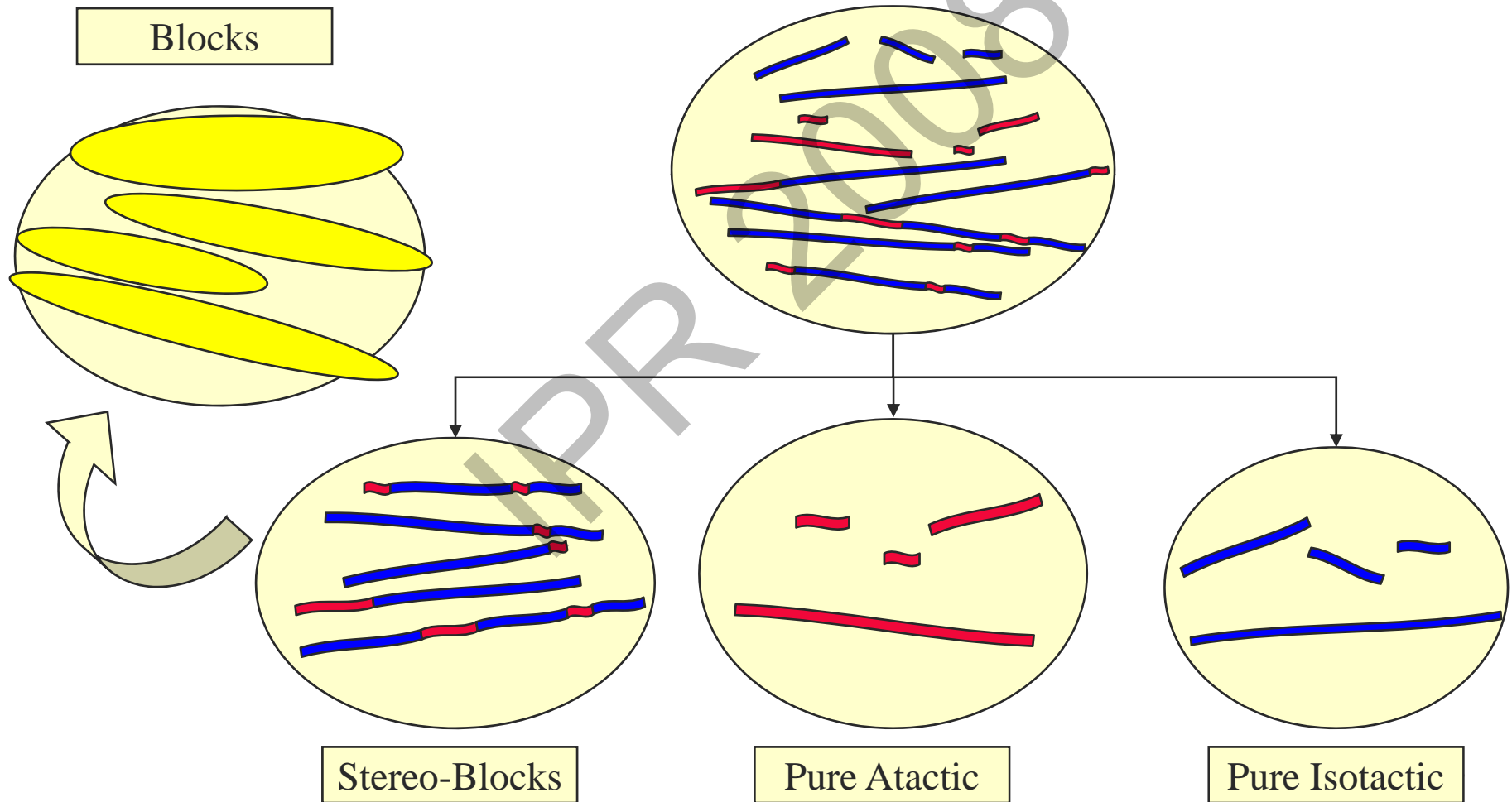
➤ Propagation:



➤ Termination:



Species Classification

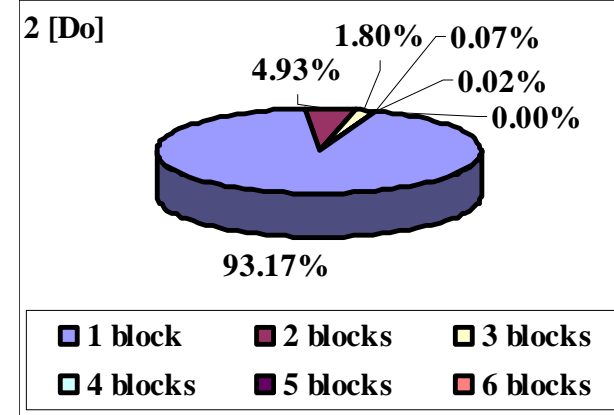
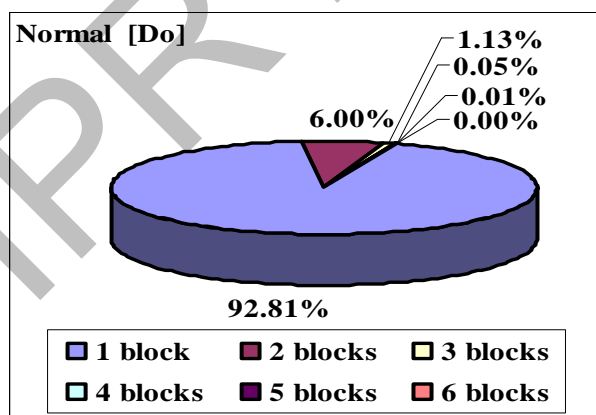
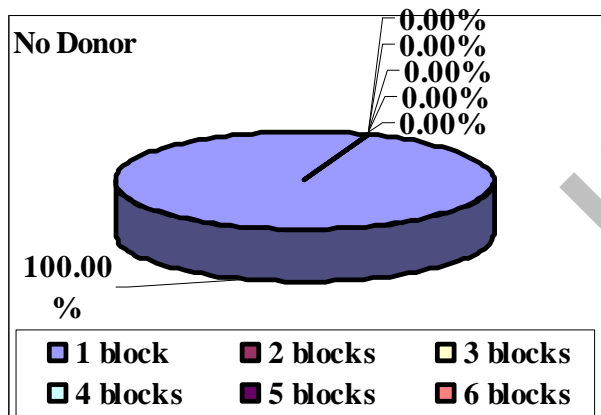
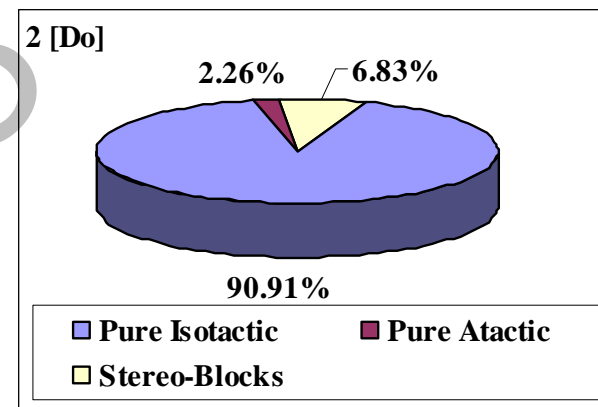
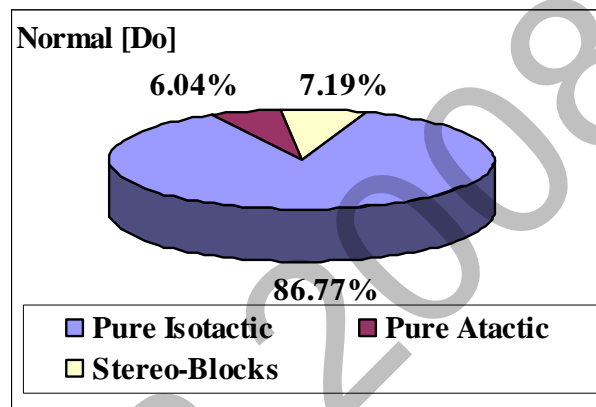
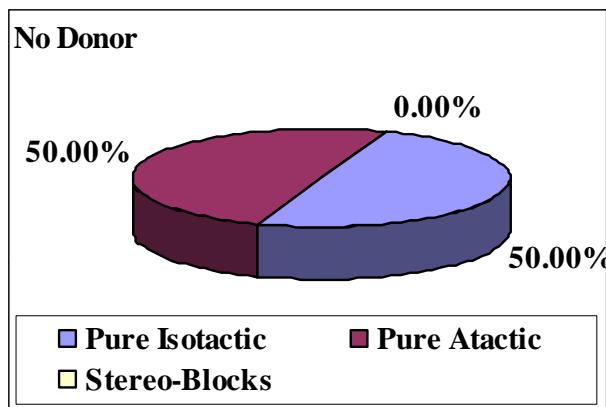


Single Site

Steady State Simulation Results

Steady State Solution for One Site Type:
 $R_{P1}/R_{P2} = 1$, $R_{P1}/R_{T1} = 1364$, $R_{P2}/R_{T2} = 1364$

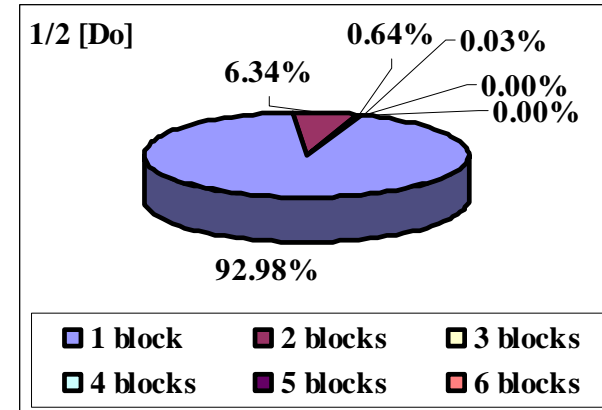
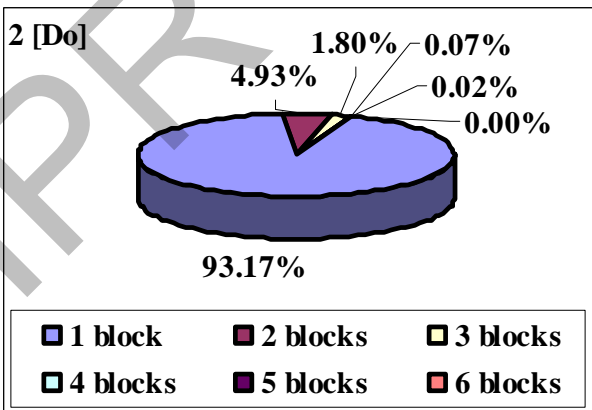
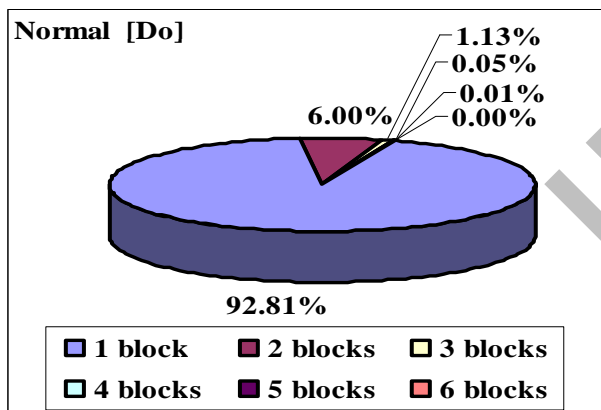
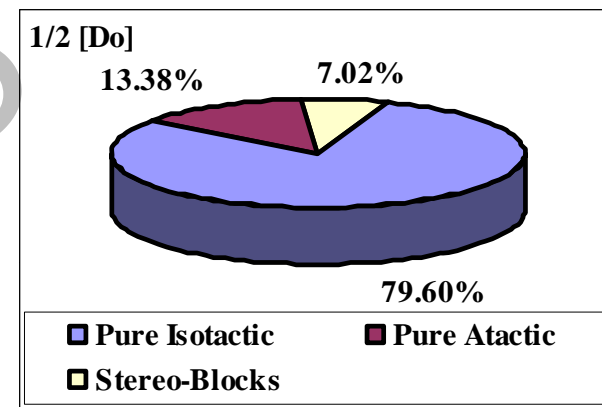
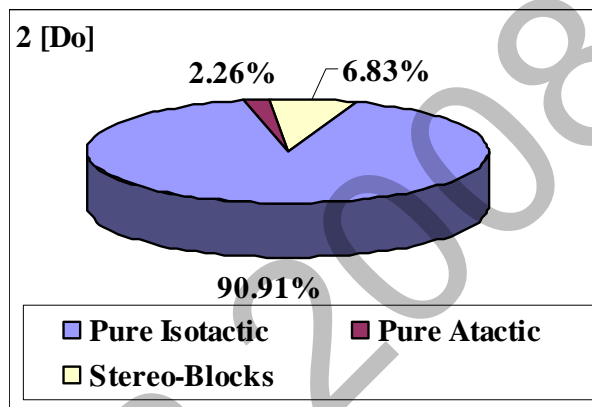
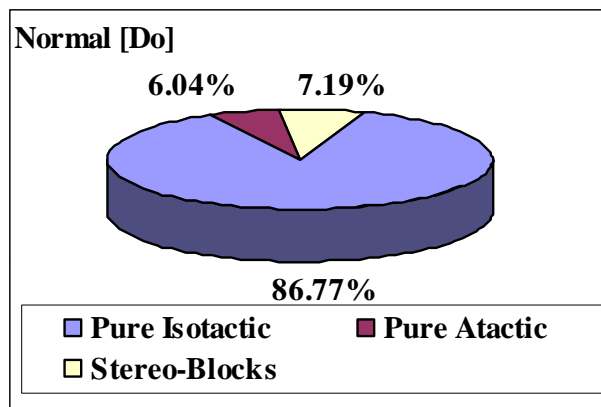
Effect of Changing the Electron Donor Concentration 1/2



| | | | |
|---------------|---------|---------|---------|
| M_n (g/mol) | 57,000 | 57,000 | 57,000 |
| M_w (g/mol) | 114,000 | 114,000 | 114,000 |
| PDI | 2.00 | 2.00 | 2.00 |

Steady State Solution for One Site Type:
 $R_{P1}/R_{P2} = 1$, $R_{P1}/R_{T1} = 1364$, $R_{P2}/R_{T2} = 1364$

Effect of Changing the Electron Donor Concentration 2/2



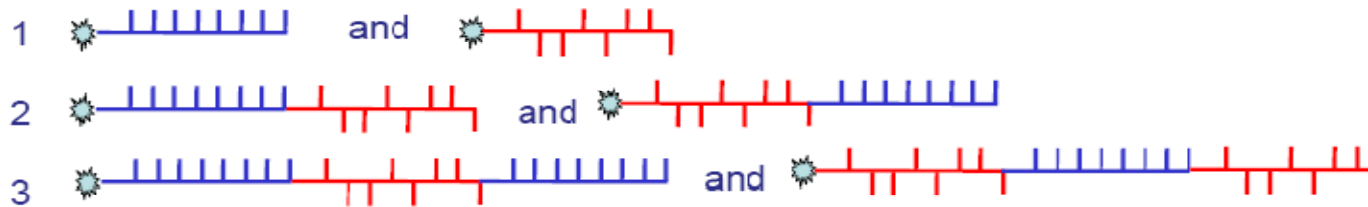
| | | | |
|---------------|---------|---------|---------|
| M_n (g/mol) | 57,000 | 57,000 | 57,000 |
| M_w (g/mol) | 114,000 | 114,000 | 114,000 |
| PDI | 2.00 | 2.00 | 2.00 |

Steady State Solution for One Site Type

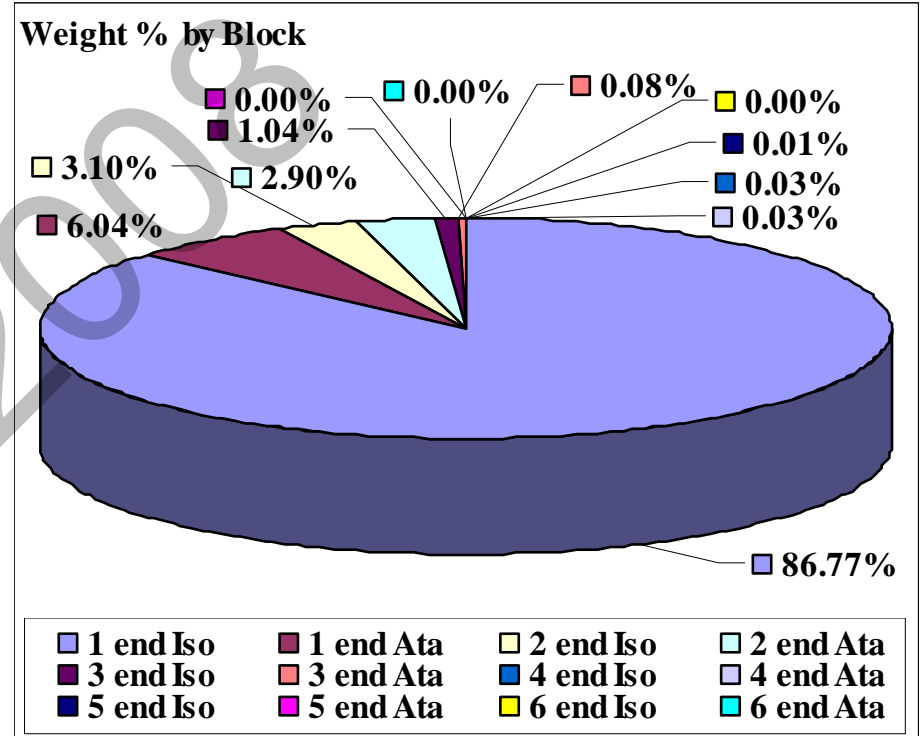
Block's Properties and Their Weight Distribution

| <i>i</i> | End Iso | | | End Ata | | |
|----------|---------|---------|------|---------|---------|------|
| | Mn | Mw | PD | Mn | Mw | PD |
| 1 | 56,000 | 112,000 | 2.00 | 46,000 | 92,000 | 2.00 |
| 2 | 102,000 | 153,000 | 1.50 | 102,000 | 153,000 | 1.50 |
| 3 | 158,000 | 211,000 | 1.34 | 148,000 | 198,000 | 1.34 |
| 4 | 204,000 | 256,000 | 1.25 | 204,000 | 256,000 | 1.25 |
| 5 | 260,000 | 313,000 | 1.20 | 250,000 | 301,000 | 1.20 |
| 6 | 307,000 | 358,000 | 1.17 | 307,000 | 358,000 | 1.17 |

i = Block #

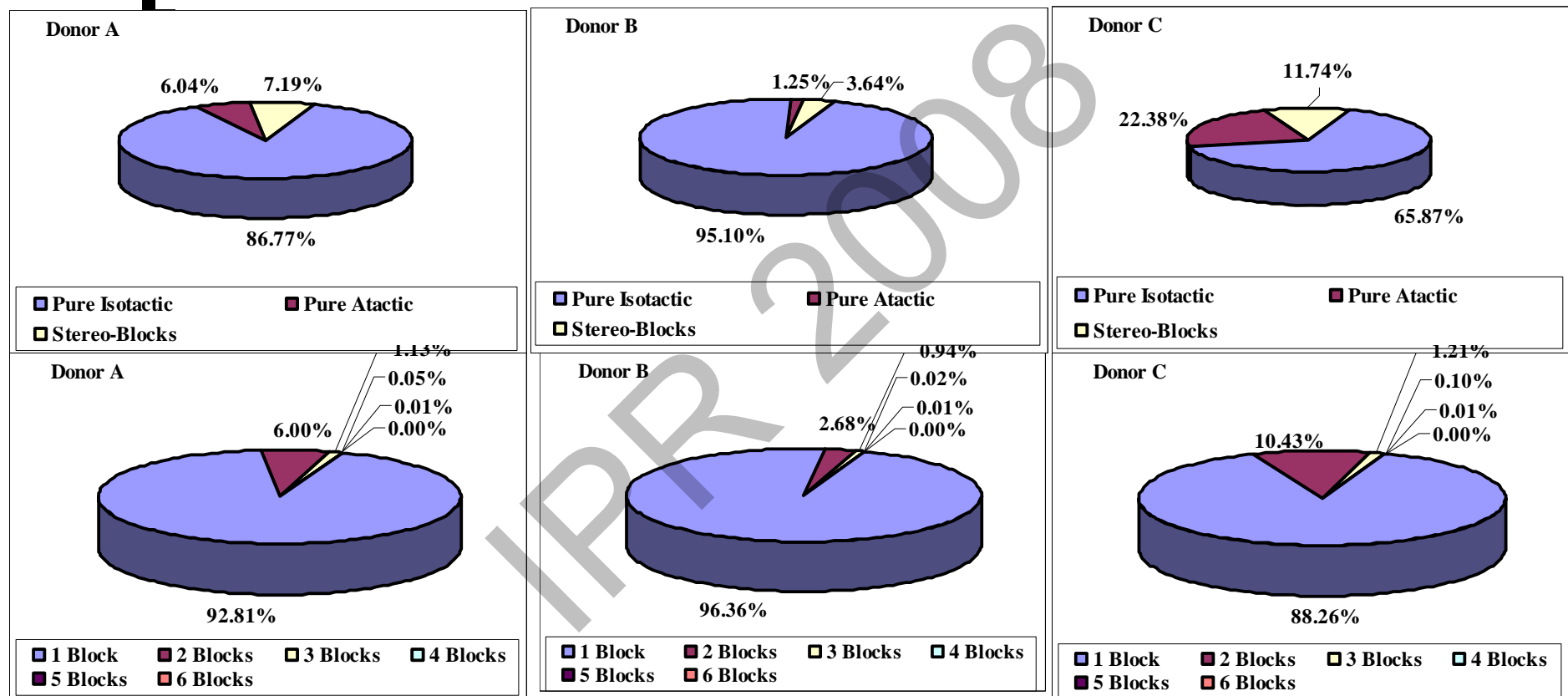


etc.



Steady State Solution for One Site Type

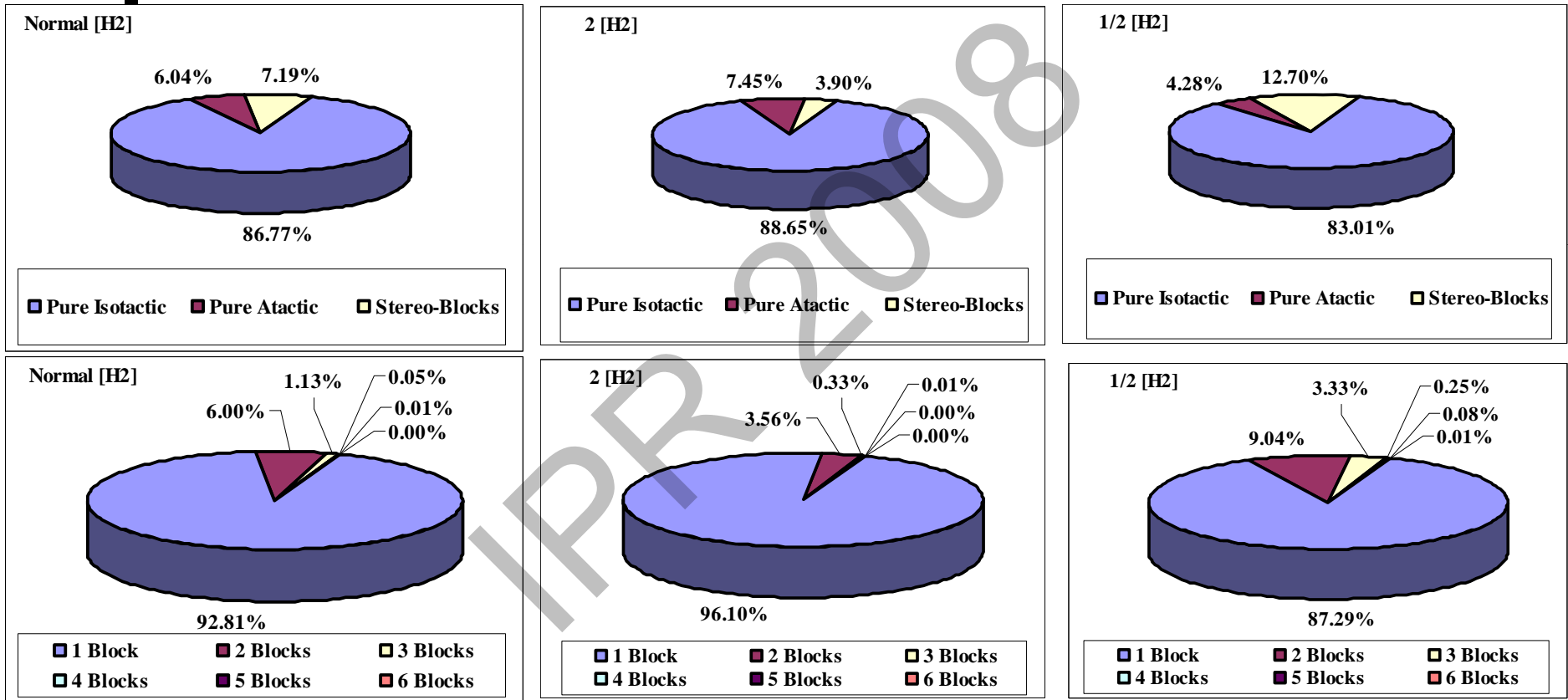
Effect of Changing the Donor Type



| | | | |
|---------------|---------|---------|---------|
| K^+ / K_A^+ | 1 | 2 | 0.5 |
| K^- / K_A^- | 1 | 0.5 | 2 |
| M_n g/mol | 57,000 | 57,000 | 57,000 |
| M_w g/mol | 114,000 | 114,000 | 114,000 |
| PDI | 2.00 | 2.00 | 2.00 |

Steady State Solution for One Site Type

Effect of Changing the Hydrogen Concentration



$$R_{P1}/R_{T1} = 1364, R_{P2}/R_{T2} = 1364$$

$$R_{P1}/R_{T1} = 682, R_{P2}/R_{T2} = 682$$

$$R_{P1}/R_{T1} = 2727, R_{P2}/R_{T2} = 2727$$

| | | | |
|-------------|---------|--------|---------|
| M_n g/mol | 57,000 | 29,000 | 114,000 |
| M_w g/mol | 114,000 | 58,000 | 228,000 |
| PDI | 2.00 | 2.00 | 2.00 |

Multiple Sites

Steady State Simulation Results

Summary Results for a 4-Site Model of Propylene Polymerization

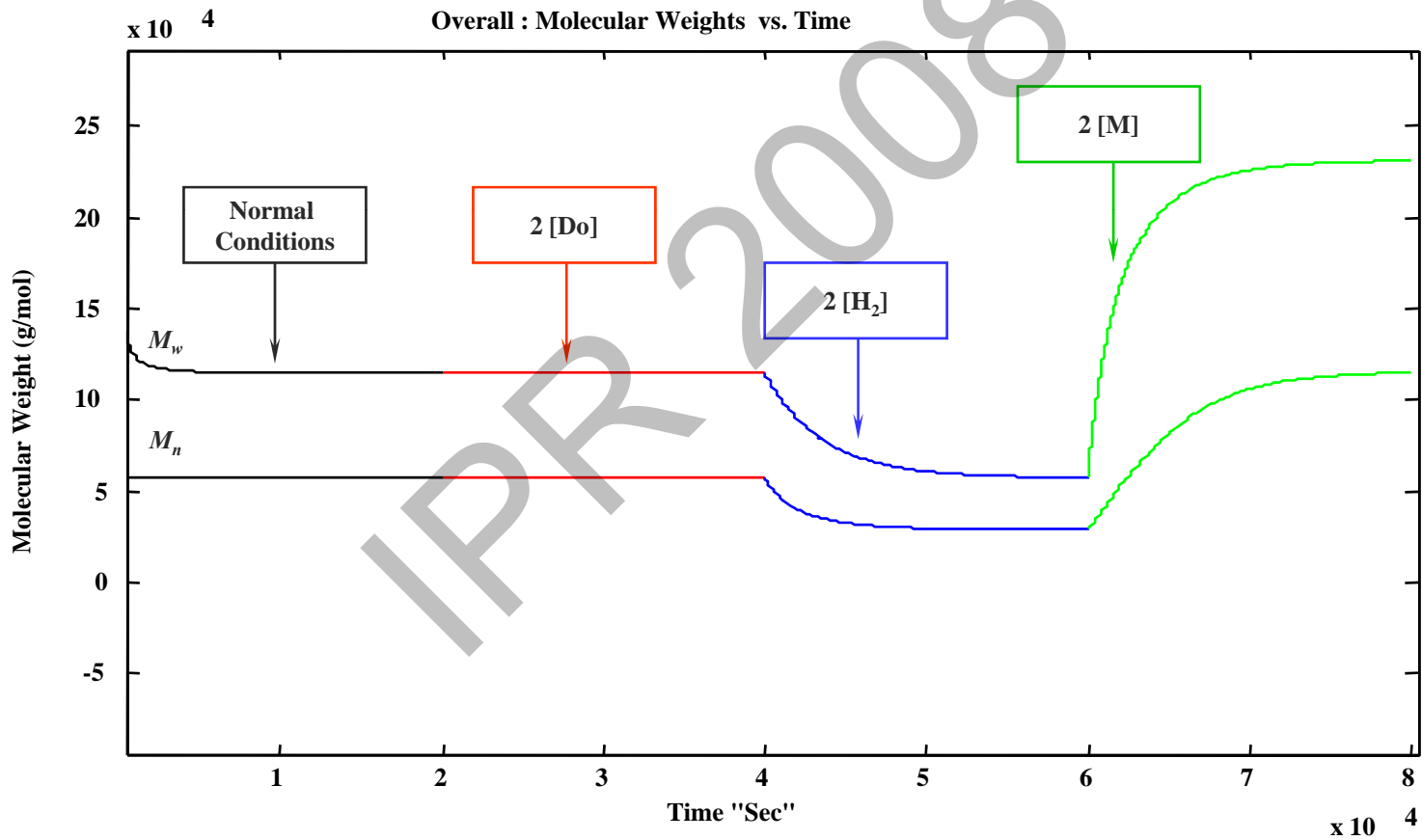
| Site | Overall | 1 | 2 | 3 | 4 |
|-----------------|-------------|-----------------------------------|-------------|-----------------|-------------|
| | Mass % | Mass % | Mass % | Mass % | Mass % |
| Pure Isotactic | 98.22% | 100 % | 100 % | 93.40% | 86.47% |
| Pure Atactic | 0.30% | 0.0 % | 0.0 % | 2.84% | 0.88% |
| Stereo-Blocks | 1.48% | 0.0 % | 0.0 % | 3.76% | 12.64% |
| Block weight %: | | Single-state stereospecific sites | | Two-state sites | |
| 1 block | 97.98% | 100 % | 100 % | 96.24% | 87.35% |
| 2 blocks | 1.44% | 0.0 % | 0.0 % | 3.24% | 7.89% |
| 3 blocks | 0.52% | 0.0 % | 0.0 % | 0.50% | 4.25% |
| 4 blocks | 0.04% | 0.0 % | 0.0 % | 0.01% | 0.35% |
| 5 blocks | 0.01% | 0.0 % | 0.0 % | 0.00% | 0.14% |
| 6 blocks | 0.00% | 0.0 % | 0.0 % | 0.00% | 0.01% |
| M_n (g/mol) | 52,081 | 62,957 | 167,316 | 7,902 | 191,523 |
| M_w (g/mol) | 231,513 | 125,890 | 334,595 | 16,013 | 398,055 |
| PDI | 4.45 | 2.00 | 2.00 | 2.03 | 2.08 |
| R_{P1}/R_{P2} | | | | 2.50 | 6.67 |
| R_{P1}/R_{T1} | | 1500 | 4000 | 194 | 5000 |
| R_{P2}/R_{T2} | | 0 | 0 | 97 | 1071 |

Single Site

Dynamic Simulation Results

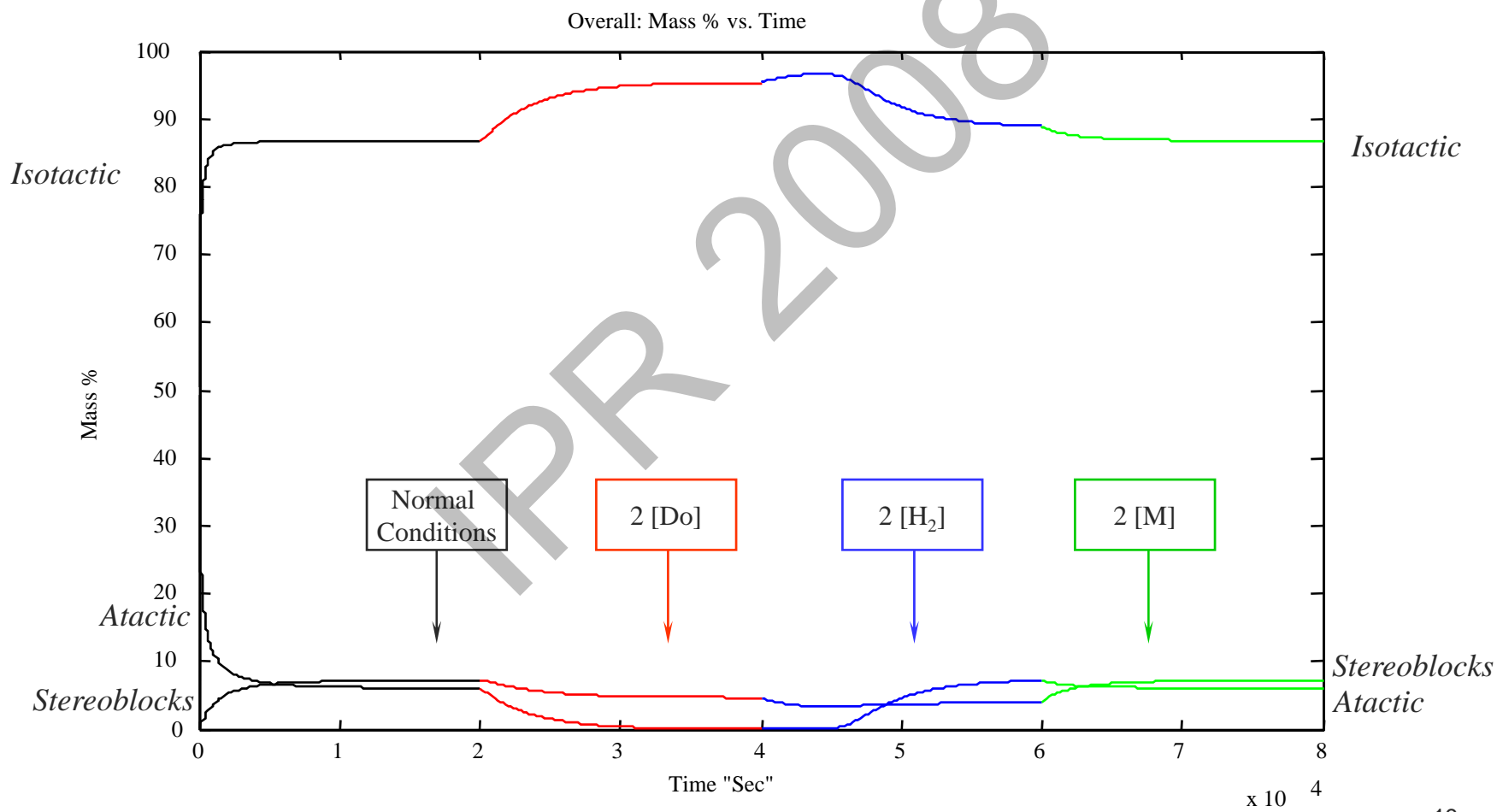
Dynamic Solution Simulation

Effect of Donor, Hydrogen, & Monomer Concentrations on Molecular Weight



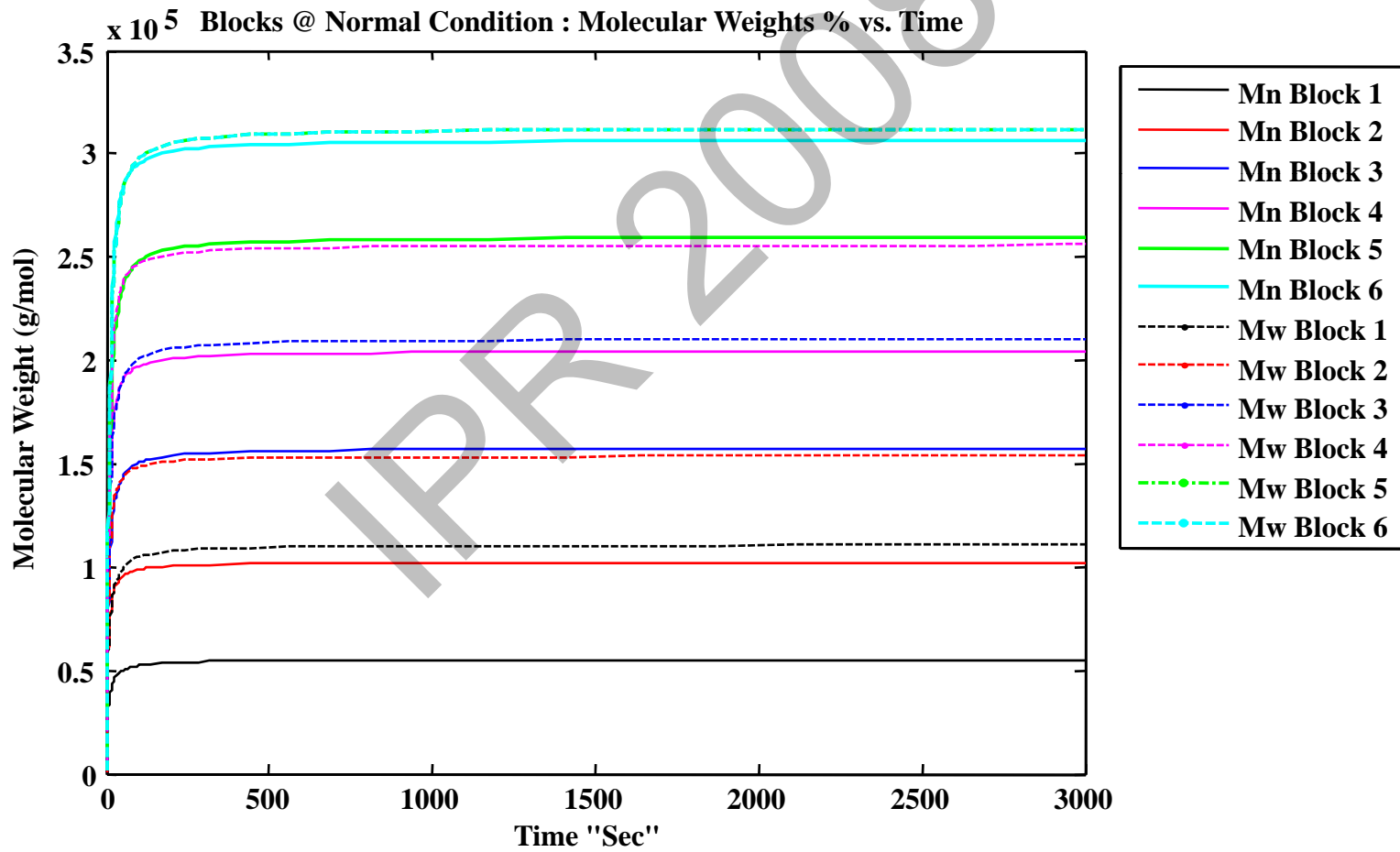
Dynamic Solution Simulation

Effect of Donor, Hydrogen, & Monomer Concentrations on Tacticity



Dynamic Solution Simulation

Molecular Weights by Block Number

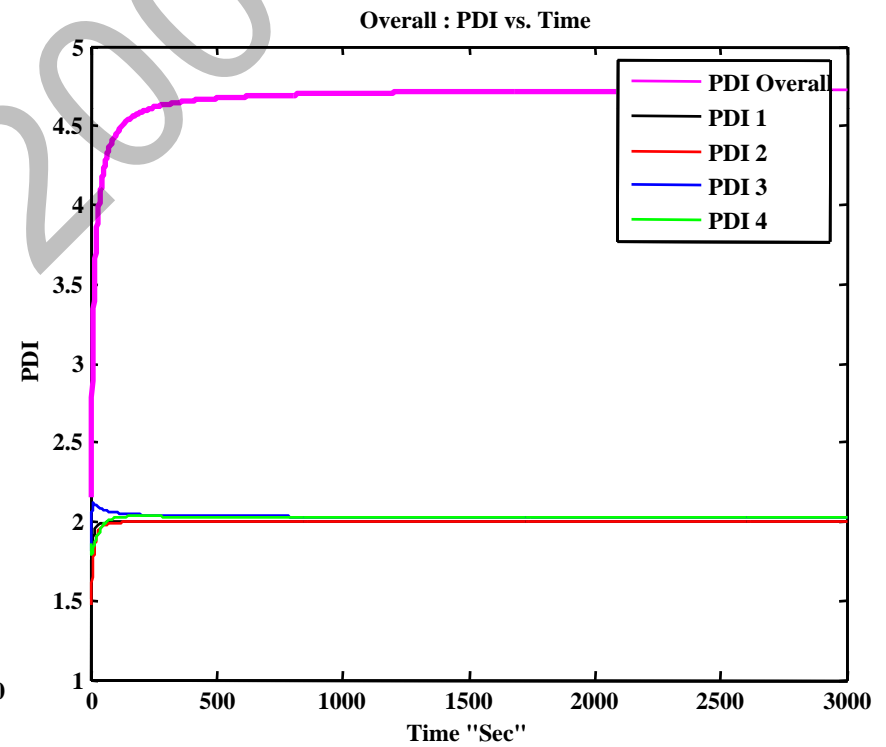
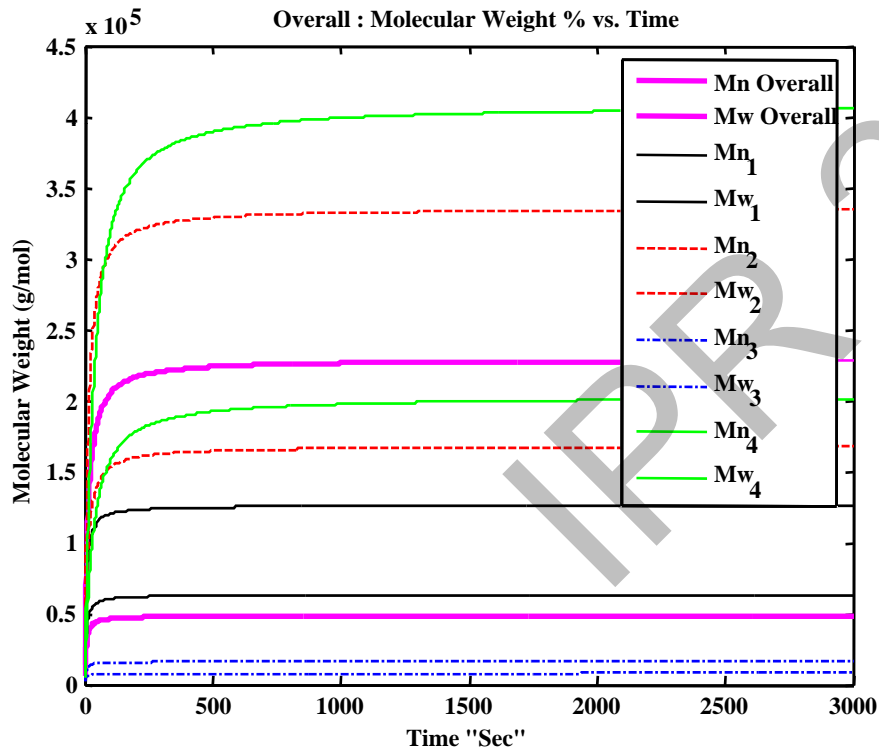


Multiple Sites

Dynamic Simulation Results

Dynamic Solution Simulation for a 4-Site Model

Molecular Weight & Polydispersity Index



Monte Carlo Simulation



$$P_p = \frac{R_p}{R_p + R_{tr} + R_{tf}}$$

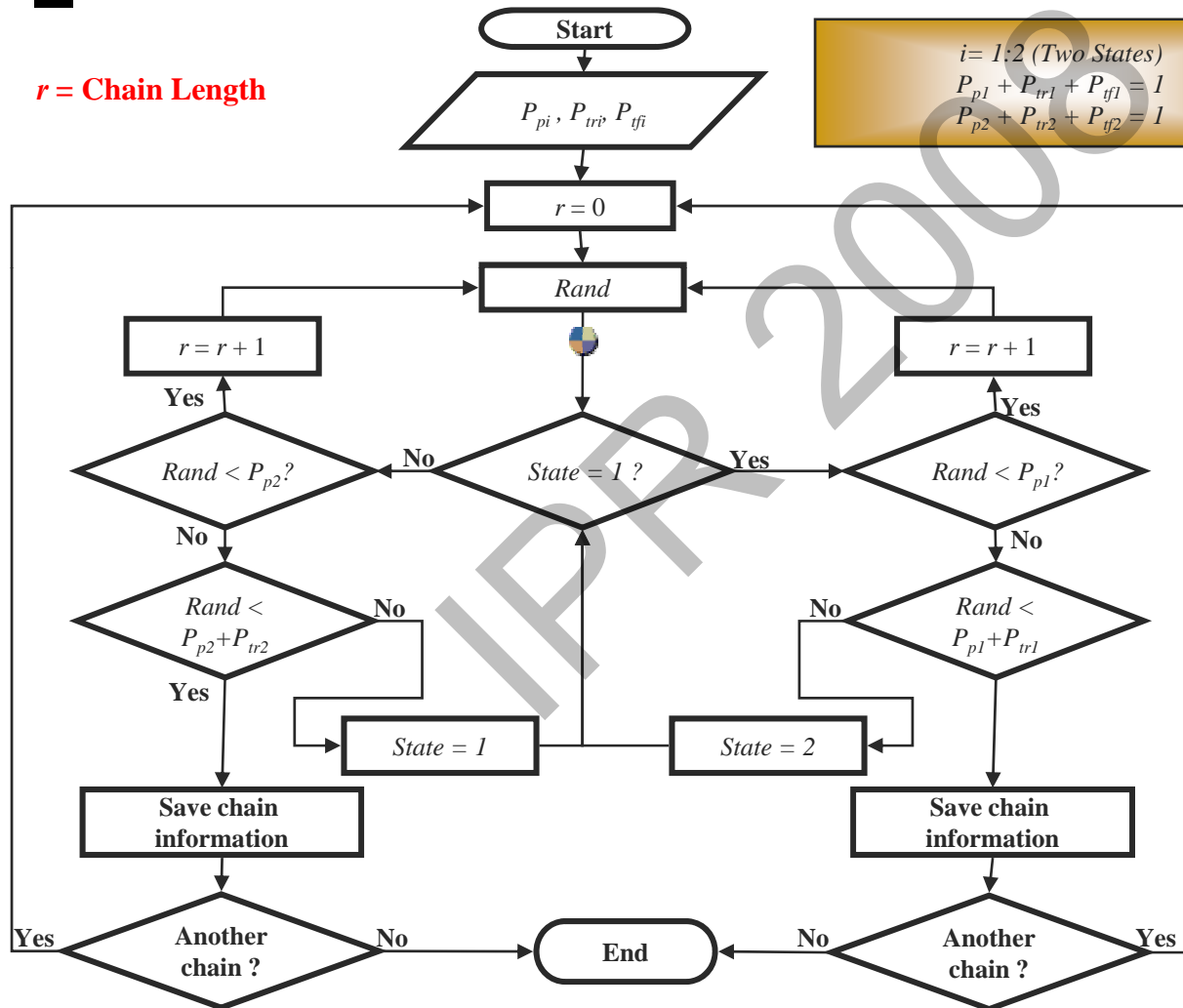
$$P_{tr} = \frac{R_{tr}}{R_p + R_{tr} + R_{tf}}$$

$$P_{tf} = \frac{R_{tf}}{R_p + R_{tr} + R_{tf}}$$

Can have the whole distribution

Monte Carlo Approach

$r = \text{Chain Length}$



$$\begin{aligned}
 & i = 1:2 \text{ (Two States)} \\
 & P_{p1} + P_{tr1} + P_{tf1} = 1 \\
 & P_{p2} + P_{tr2} + P_{tf2} = 1
 \end{aligned}$$



Monte Carlo Approach

■ Donor Effect:

$$\begin{aligned} P_{p1} + P_{tr1} + P_{tf1} &= 1 \\ P_{p2} + P_{tr2} + P_{tf2} &= 1 \end{aligned}$$

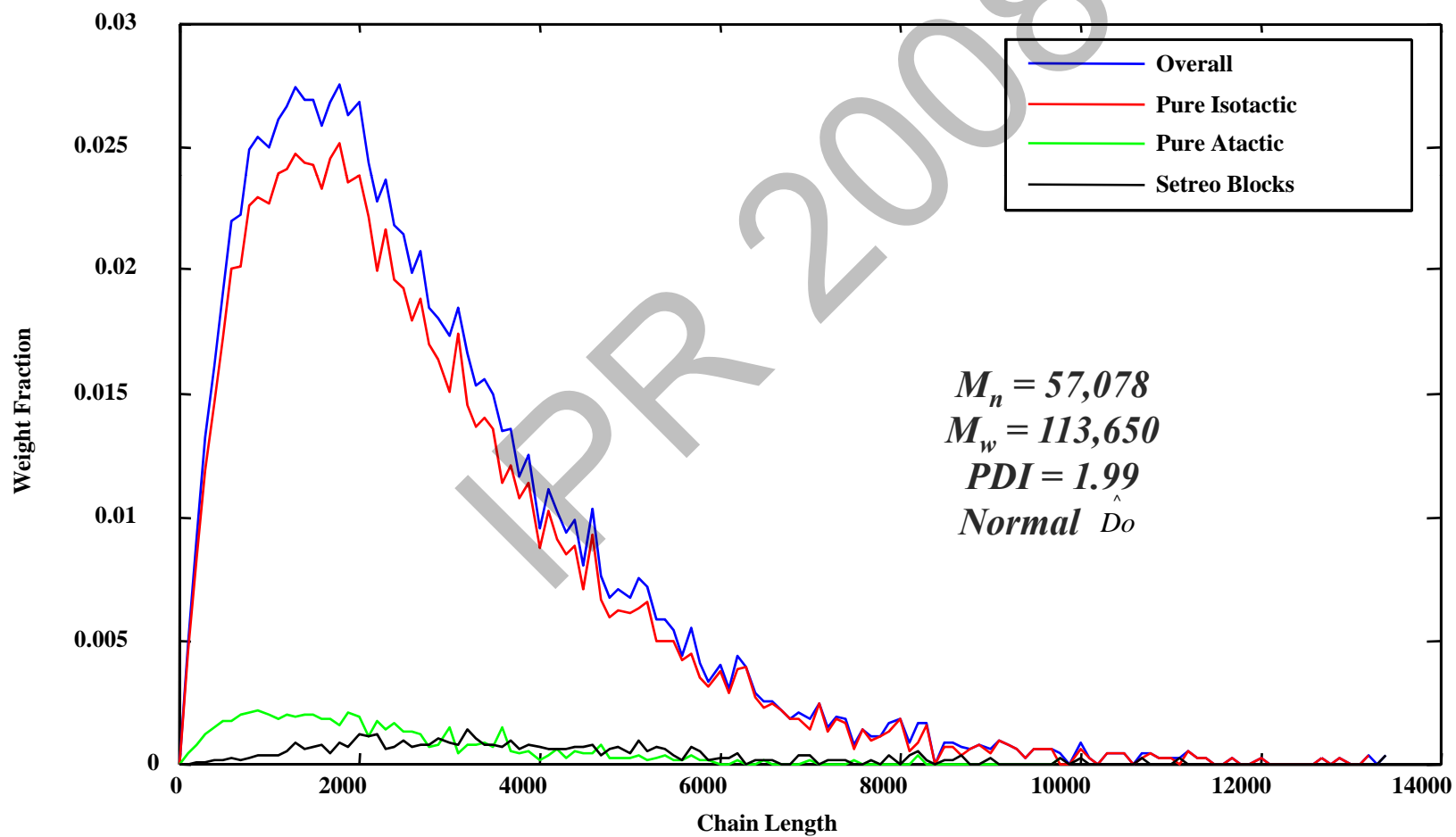
$$P_{tf} = \frac{R_{tf}}{R_p + R_{tr} + R_{tf}}$$

$$R_{tf} = k_{Do}^+ [P_r^{II}] [Do]$$

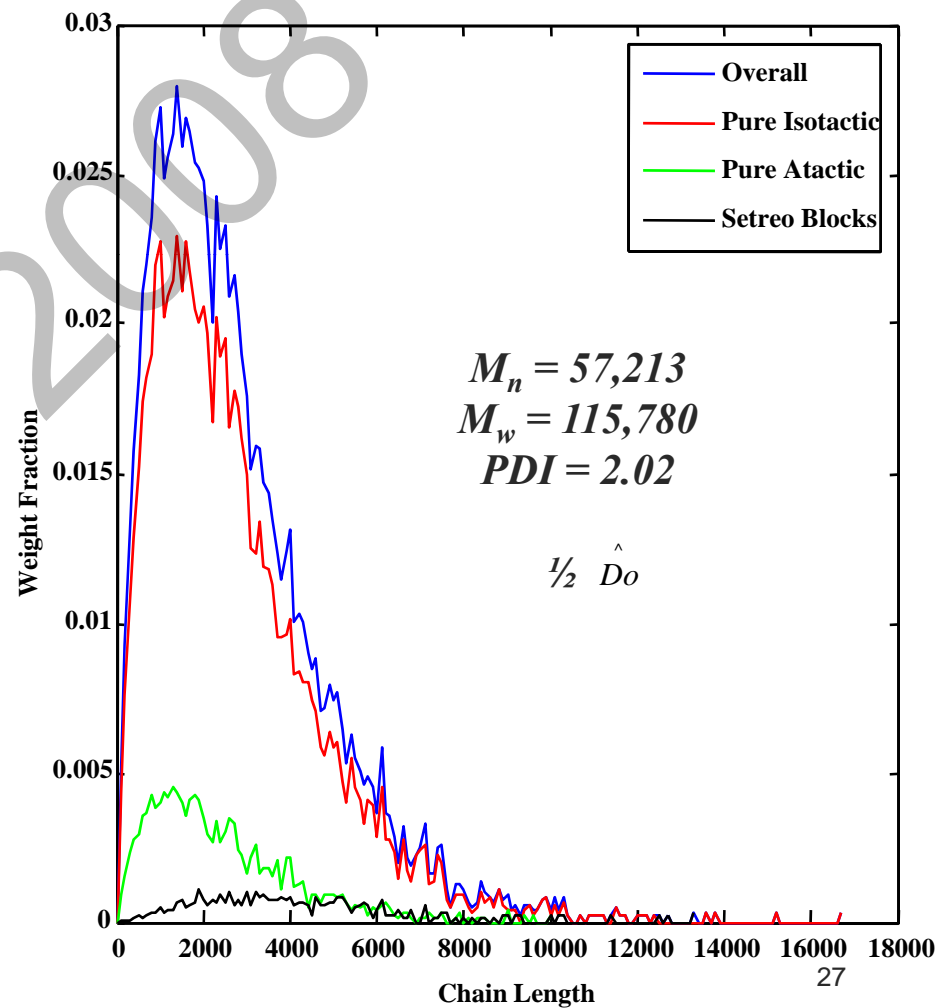
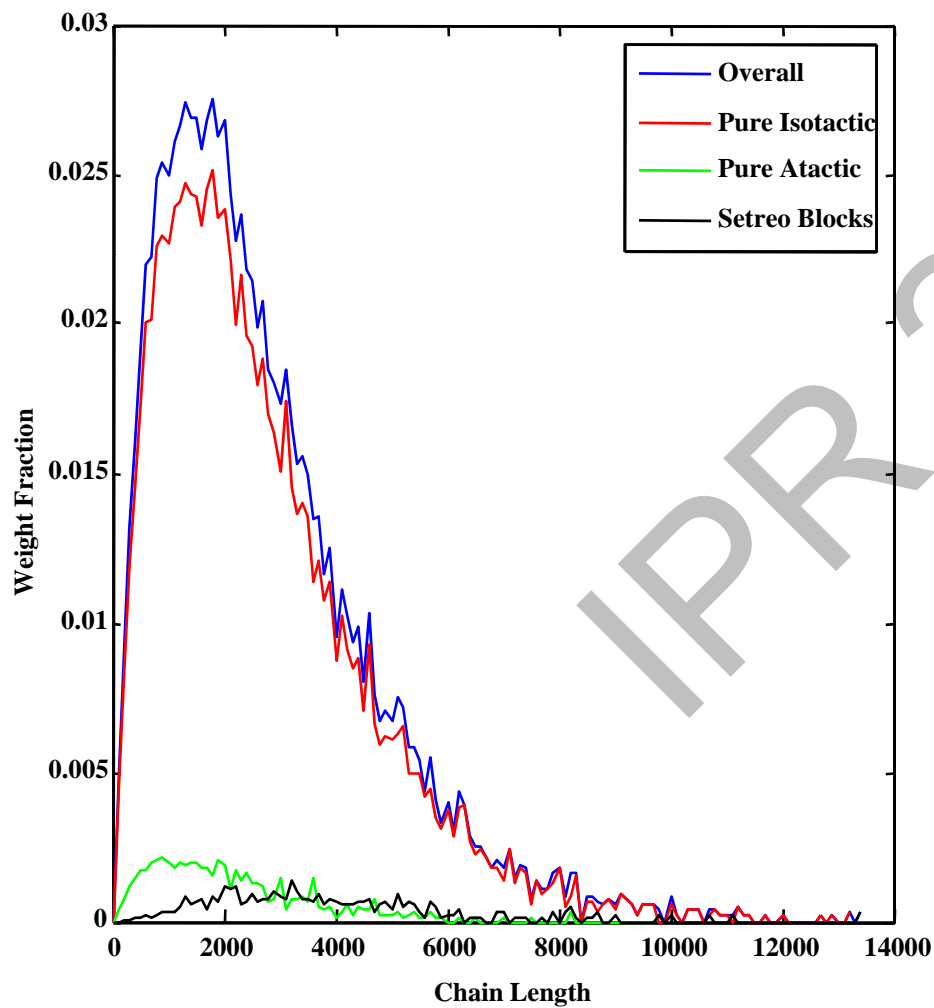
Donor Type

Donor Concentration

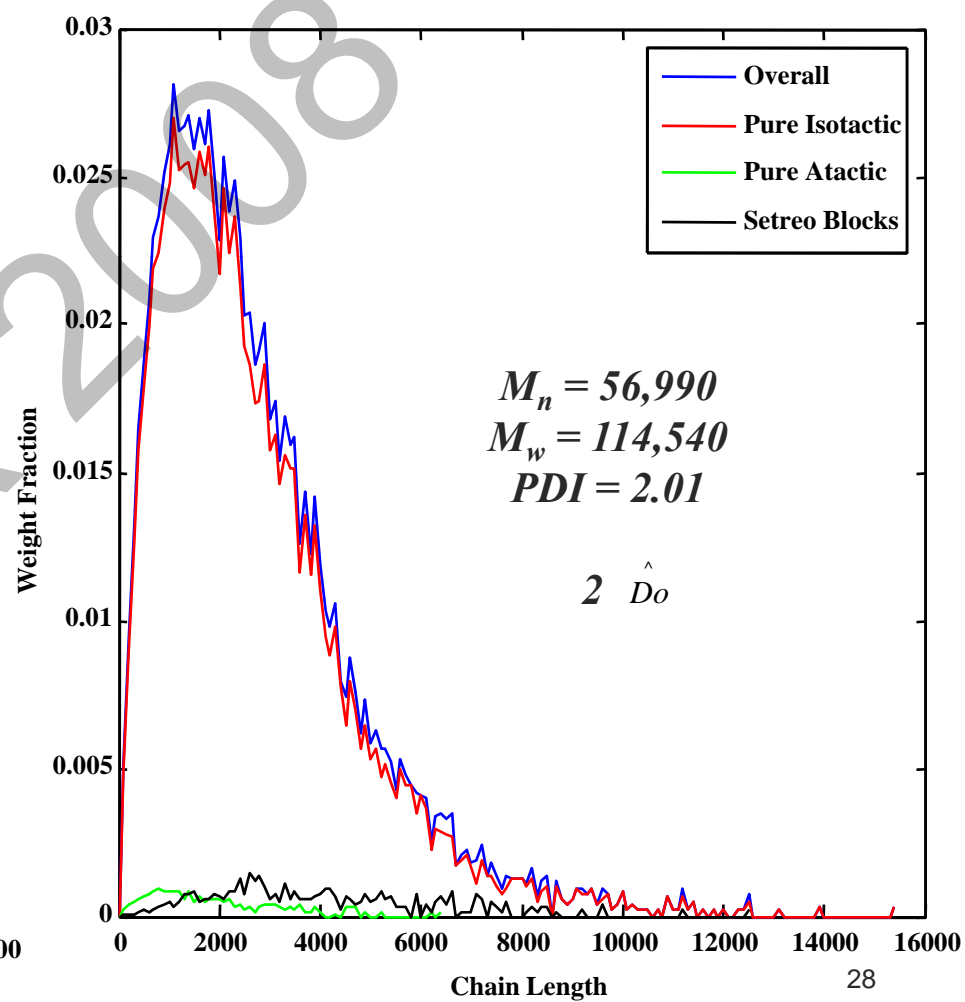
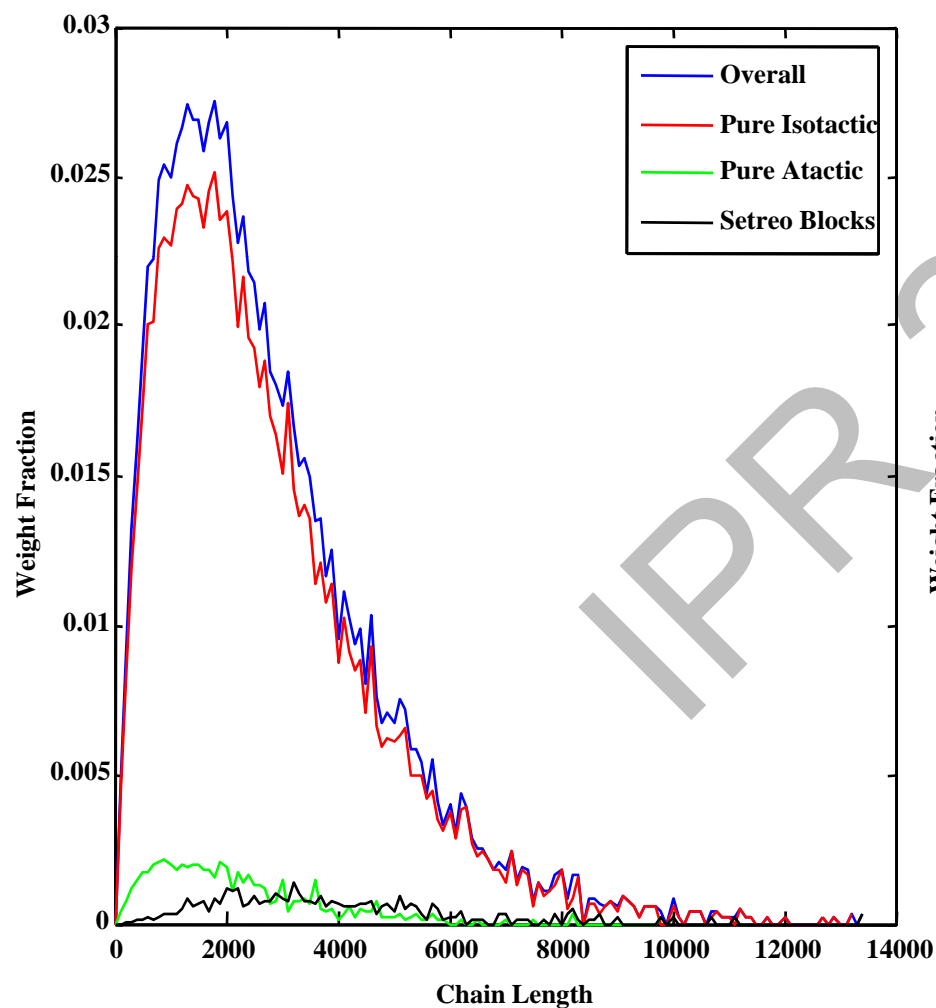
Chain Length vs. Weight Fraction @ Normal [Do]



Chain Length vs. Weight Fraction @ 1/2 [Do]



Chain Length vs. Weight Fraction @ 2 [Do]



[CURRENT & FUTURE WORK]

- Add additional features to the Monte Carlo code such as number of defects per chain and end group determination
- Use the microstructural information obtained by simulation to predict polypropylene fractionation with the temperature rising elution fractionation (TREF) and the nuclear magnetic resonance (^{13}C NMR)
- Plan for the parameter estimation for some known commercial catalyst / donor systems.

CONCLUSION

- The model is able to predict the polypropylene properties taking in consideration site transformation in the presence of the electron donor.
- The model is able to predict the tacticity during propylene polymerization which could enhance and used as a tool for the process control.
- The model will be used for parameter estimation for some commercial catalyst /electron donor systems.
- The microstructural information obtained by simulation can be used to predict polypropylene fractionation with the temperature rising elution fractionation (TREF).

[THE END]

**THANK
YOU**

Steady State vs. Dynamic Solution Simulations

| Mass % | Steady State | Dynamic | Error % |
|--------------------|--------------|---------|---------|
| Pure Isotactic | 86.73% | 86.68% | -0.1% |
| Pure Atactic | 6.07% | 6.10% | 0.5% |
| Stereo-Blocks | 7.20% | 7.22% | 0.2% |
| By Block %: | | | |
| 1 block | 92.81% | 92.81% | 0.0% |
| 2 blocks | 6.00% | 6.00% | 0.0% |
| 3 blocks | 1.13% | 1.13% | 0.0% |
| 4 blocks | 0.05% | 0.05% | 0.0% |
| 5 blocks | 0.01% | 0.01% | 0.0% |
| 6 blocks | 0.00% | 0.00% | 0.0% |
| M_n (g/mol) | 57,270 | 57,270 | 0.00% |
| M_w (g/mol) | 114,497 | 114,500 | 0.00% |
| <i>PDI</i> | 2.00 | 2.00 | 0.00% |

Steady State vs. Dynamic Solution Simulations

| i | <u>Steady State</u> | | | <u>Dynamic</u> | | | <u>Error %</u> | | |
|---|---------------------|-----------|------|----------------|-----------|------|----------------|-----------|-------|
| | <i>Mn</i> | <i>Mw</i> | PD | <i>Mn</i> | <i>Mw</i> | PD | <i>Mn</i> | <i>Mw</i> | PD |
| 1 | 55,246 | 110,695 | 2.00 | 55,245 | 110,690 | 2.00 | 0.00% | 0.00% | 0.00% |
| 2 | 102,229 | 153,807 | 1.50 | 102,230 | 153,810 | 1.50 | 0.00% | 0.00% | 0.00% |
| 3 | 157,432 | 210,382 | 1.34 | 157,430 | 210,380 | 1.34 | 0.00% | 0.00% | 0.00% |
| 4 | 204,416 | 256,004 | 1.25 | 204,420 | 256,010 | 1.25 | 0.00% | 0.00% | 0.00% |
| 5 | 259,619 | 312,037 | 1.20 | 259,620 | 312,040 | 1.20 | 0.00% | 0.00% | 0.00% |
| 6 | 306,603 | 358,194 | 1.17 | 306,610 | 358,200 | 1.17 | 0.00% | 0.00% | 0.00% |

| | <u>Steady State</u> | | | <u>Dynamic</u> | | | <u>Error %</u> | | |
|----------------|---------------------|-----------|------|----------------|-----------|------|----------------|-----------|--------|
| | <i>Mn</i> | <i>Mw</i> | PD | <i>Mn</i> | <i>Mw</i> | PD | <i>Mn</i> | <i>Mw</i> | PD |
| Iso-Segments | 56,008 | 111,939 | 2.00 | 56,002 | 111,960 | 2.00 | 0.01% | -0.02% | -0.03% |
| Ata-Segments | 46,274 | 92,507 | 2.00 | 46,271 | 92,500 | 2.00 | 0.01% | 0.01% | 0.00% |
| Total Segments | 55,058 | 110,377 | 2.00 | 55,112 | 110,470 | 2.00 | -0.10% | -0.08% | 0.01% |