

Modelling insights into the nitroxide-mediated radical polymerization of styrene

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Reaction Mechanism and Moments

Description	Step
Chemical initiation	$I \xrightarrow{k_d} 2R_{in}^\bullet$
Nitroxyl ether decomposition	$NO_E \xrightleftharpoons[k_{d2}]{k_{a2}} R_{in}^\bullet + NO_x^\bullet$
Mayo dimerization	$M + M \xrightarrow{k_{dim}} D$
Thermal initiation	$M + D \xrightarrow{k_{ia}} D^\bullet + M^\bullet$
First propagation (primary radicals)	$R_{in}^\bullet + M \xrightarrow{k_p} R_1^\bullet$
First propagation (monomeric radicals)	$M^\bullet + M \xrightarrow{k_p} R_1^\bullet$
First propagation (dimeric radicals)	$D^\bullet + M \xrightarrow{k_p} R_1^\bullet$
Propagation	$R_r^\bullet + M \xrightarrow{k_p} R_{r+1}^\bullet$

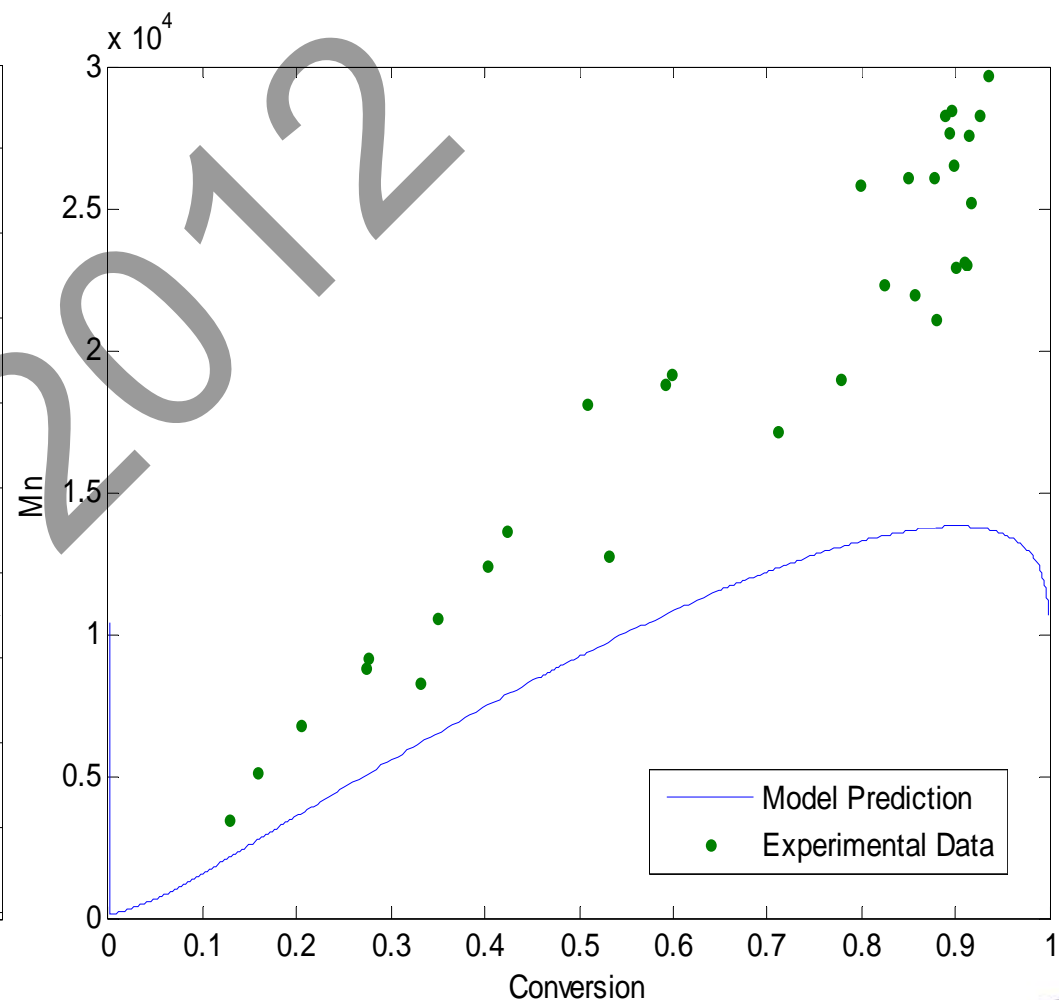
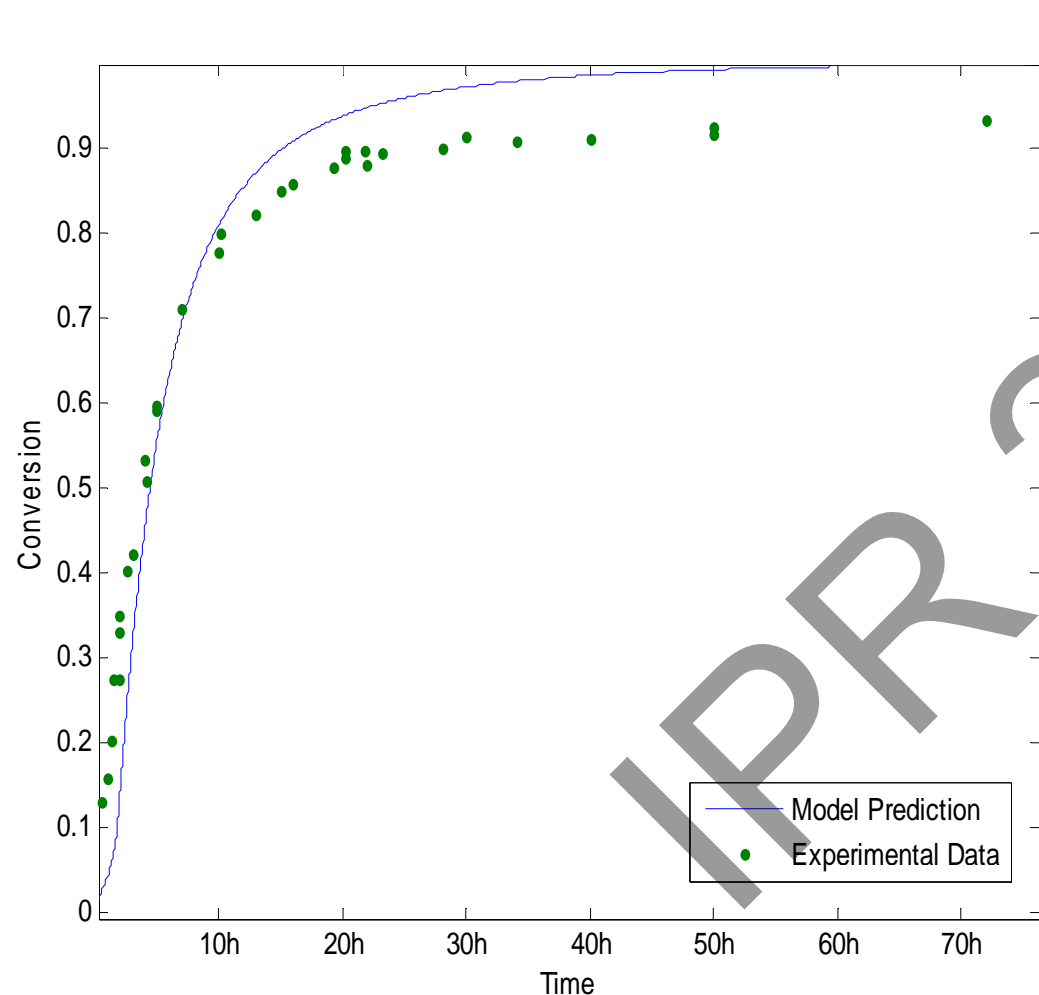
Dormant living exchange (monomeric alkoxyamine)	$M^\bullet + NO_x^\bullet \xrightleftharpoons[k_{da}]{k_a} MNO_x$
Dormant living exchange (polymeric alkoxyamine)	$R_r^\bullet + NO_x^\bullet \xrightleftharpoons[k_{da}]{k_a} R_rNO_x$
Alkoxyamine decomposition	$MNO_x \xrightarrow{k_{decomp}} M + HNO_x$
Rate enhancement reaction	$D + NO_x^\bullet \xrightarrow{k_{h3}} D^\bullet + HNO_x$
Termination by combination	$R_r^\bullet + R_s^\bullet \xrightarrow{k_{tc}} P_{r+s}$
Termination by disproportionation	$R_r^\bullet + R_s^\bullet \xrightarrow{k_{td}} P_r + P_s$
Transfer to monomer	$R_r^\bullet + M \xrightarrow{k_{fM}} P_r + M^\bullet$
Transfer to dimer	$R_r^\bullet + D \xrightarrow{k_{fD}} P_r + D^\bullet$

Moments used for MW estimation:

$$\lambda_i = \sum_r r^i R_r \quad \delta_i = \sum_r r^i R_r ON_x \quad \mu_i = \sum_r r^i P_r$$

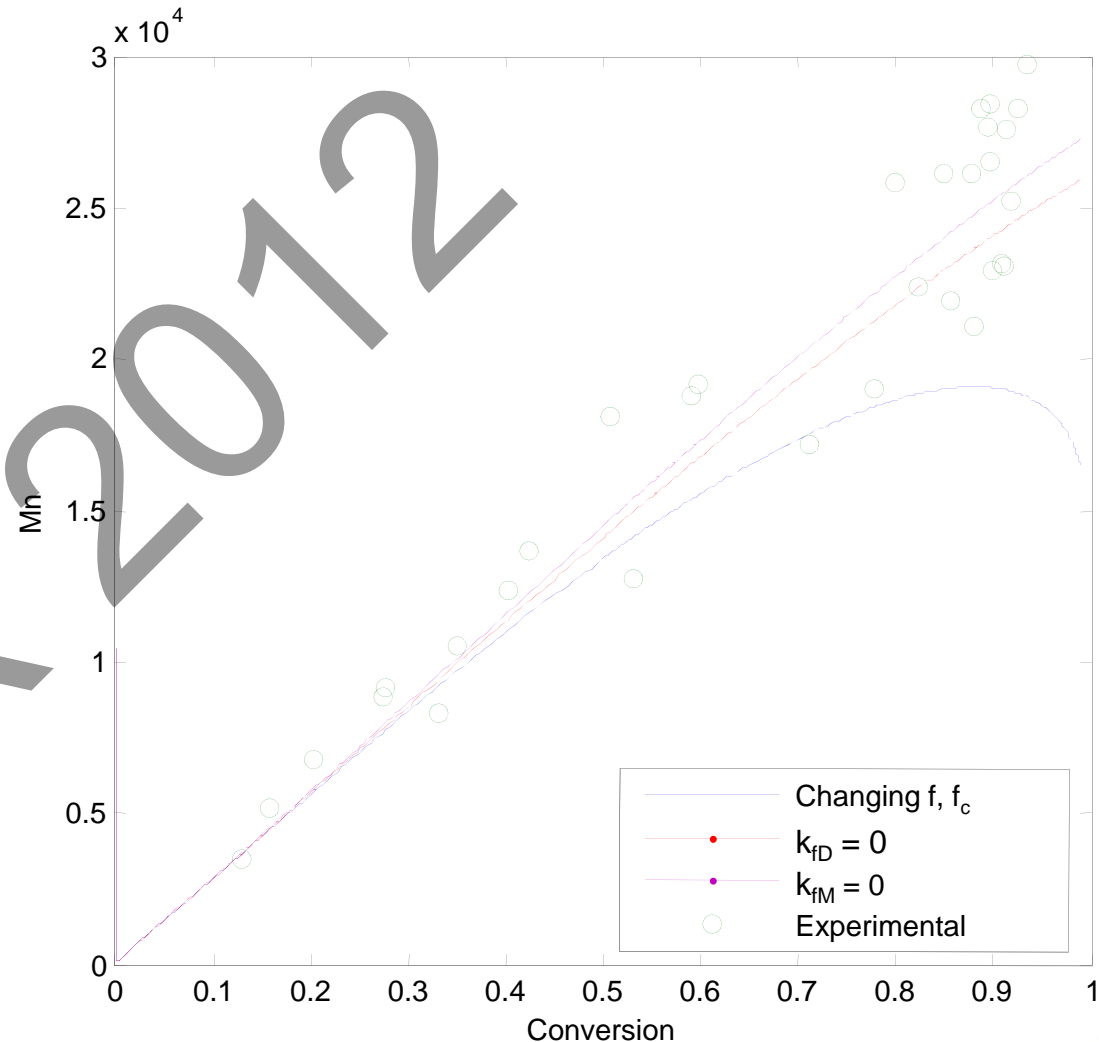
Fully Mechanistic Model (FMM)

Prior state of the art



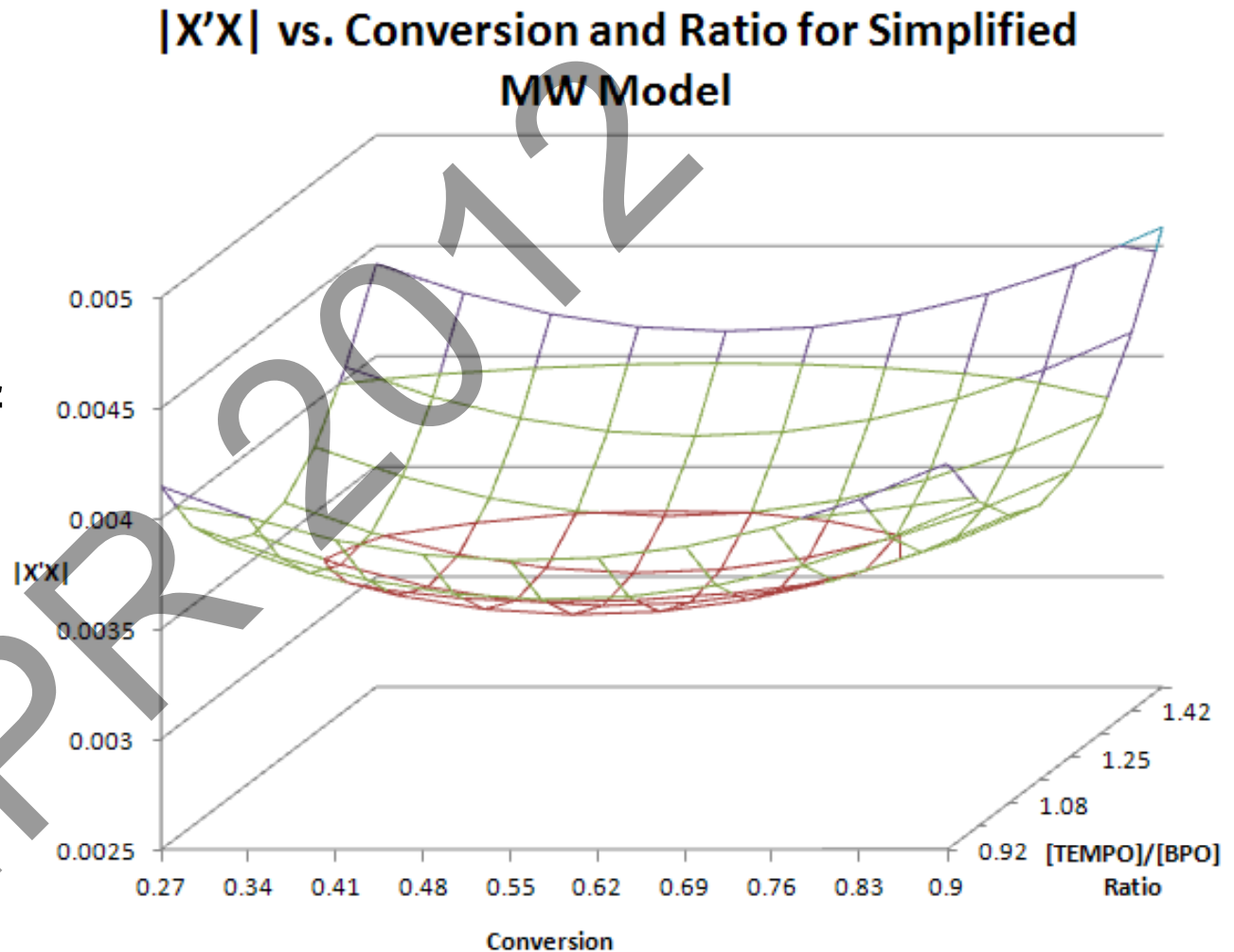
FMM Updates and Improvements

- Added controller efficiency f_c , allowed for f and f_c to change with conversion
- Removal of chain transfer to dimer and then monomer reactions
- These changes led to improved agreement with experimental data



D-Optimal Design Applications

- The D-optimality criterion (i.e., maximization of the determinant of $X'X$) can be used to select the next best experiments to be run for a process



Model and Design Applications

- Based on prior experimental trials

Level	T (°C)	[I] ₀ (M)	[N] ₀ (M)
Low	120	0.036	0.058
High	130	0.072	0.086

- Previous Bayesian approach compared with D-optimality results (with decoded [N]₀/[I]₀ Ratio)

Experiment	Bayesian Design				D-Optimal Design				
		T	[I]	[N]	Ratio	T	[I]	[N]	Ratio
First Sequence of Two Runs	1	-1	1	-1	0.81	-1	1	-1	0.81
	2	1	1	-1	0.81	1	1	-1	0.81
Second Sequence of Two Runs	3	-1	1	1	1.19	-0.6	1	1	1.19
	4	1	1	1	1.19	0.2	0.6	0.4	1.19