

**Use of CFD for Exploring  
the Effect of Mixing  
on MMA Solution Polymerization  
in a CSTR**

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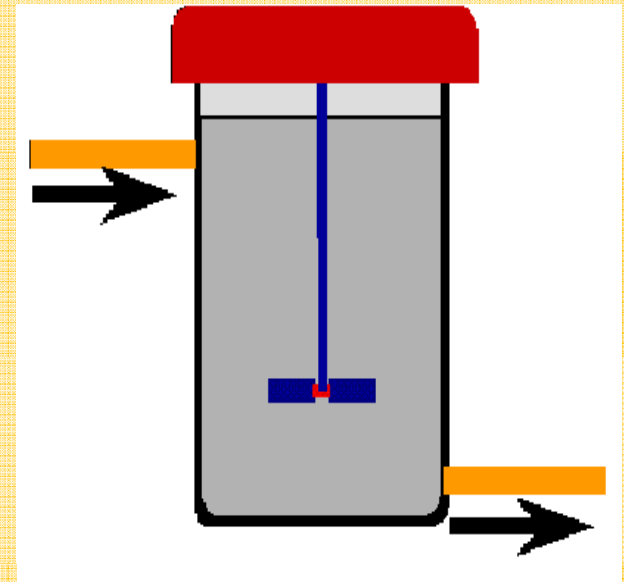
# Outline

- Introduction
- Objectives
- Reactor Specifications
- CFD Model
- Results and Discussion
- Concluding Remarks

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## Considerations:

- Good Mixing ?
- No Effect of Mixing in Conventional Kinetic models (rarely)
- Conversion/ $M_w$  Dependent on Mixing?
- Influence of Dead Zones



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## **Computer Simulation Tool involves:**

- Transport phenomena (Reaction)**
- Flow pattern**
- Trial and error analysis (Time/Cost)**
- CFD modeling → Improve reactor performance, Safety issues**

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- Patel et al. (2010) investigated the CFD modeling of styrene bulk polymerization in a CSTR.
- Shi and Luo (2010) studied the effects of velocity and solid particle size on the CFD modeling of Propylene Polymerization in a tubular loop.
- Cherbanski et al. (2007) used CFD to study the effect of process parameters on temperature behaviour in suspension polymerization .
- Serra et al. (2007) investigated the styrene free radical polymerization in a T-junction micro reactor and calculated conversion.
- Heath and Koh (2003) applied CFD modeling to calculate aggregation and breakage of solid polymer particles in a tubular pipe.
- Maschio & Moutier (1989) studied the effect of solvent fraction on polymer chain mobility in batch and CSTR reactors

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**Study the effects of solvent content, impeller speed and residence time, on MMA conversion in a CSTR using CFD**

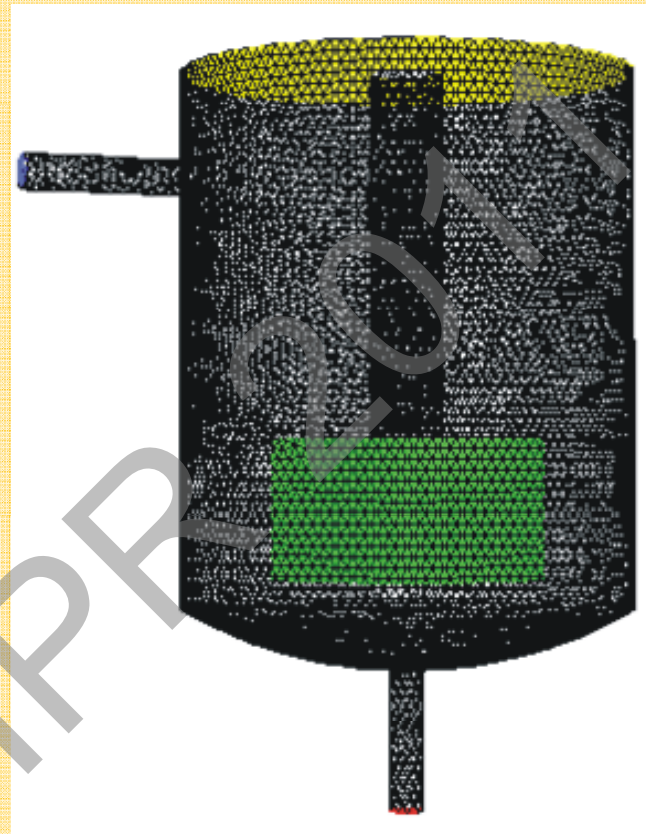
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## Geometry Grid

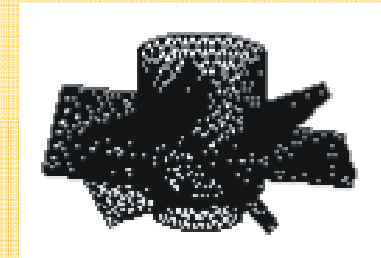
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- Gambit 2.4
- Tetrahedral,
- Triangular Faces
- ~280,000 cells
- MRF
- 1 Litre Reactor
- Six 45° pitched bladed Impeller

Inlet



Outlet



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Parameter	Value	Parameter	Value
Tank diameter	4 inches	Impeller diameter	2 inches
Liquid level	5.3 inches	Blade width	0.55 inches
Outlet diameter	0.25 inches	Blade thickness	0.8 inches
Inlet diameter	0.25 inches	Inlet wall length	1.5 inches
Impeller type	45° six pitched blade	Outlet wall length	1.5 inches

Fluid	Density (kg/m <sup>3</sup> )	Viscosity (Pa. s)	Molecular Weight (g/mole)
Methyl Methacrylate (MMA)	895	0.00037	100.12
Azobisisobutyronitrile (AIBN)	1100	0.000278	164
Toluene (Solvent)	866	0.000586	92.07



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- Transport Equations**
- Polymerization Source Equations**
- Physical Properties**

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## Transport equations

$$\frac{\partial \rho}{\partial t} + (\nabla \cdot \rho \vec{v}) = 0$$

$$\frac{\partial}{\partial t} (\rho \vec{v}) + \nabla \cdot (\rho \vec{v} \vec{v}) = -\nabla P + (\nabla \cdot \vec{\tau}) + \rho g + \vec{F}$$

$$\vec{\tau} = \mu \left[ ((\nabla \vec{v}) + (\nabla \vec{v})^T) - \frac{2}{3} \nabla \cdot \vec{v} \right]$$

$$\frac{\partial}{\partial t} (\rho W_j) + \nabla \cdot (\rho \vec{v} W_j) = -\nabla \cdot \vec{J}_j + R_j + S_j$$

$$\vec{J}_j = -\rho D \nabla W_j$$

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## Polymerization Source

### Assumptions:

- Steady-state condition**
- Termination: Combination reaction only**
- No gel effect**

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## Polymerization Source

$$[R \cdot] = \sqrt{\frac{2 f K_d [I]}{K_{tc}}}$$

$$R_p = -K_p [M] \sqrt{\frac{2 f K_d [I]}{K_{tc}}}$$

$$S_{monomer} = R_p \times M_{w,monomer}$$

$$S_{initiator} = R_p \times M_{w,initiator}$$

$$K = A \exp(-E / R_g T)$$

Parameter	Values <sup>1</sup>	Parameter	Values <sup>1</sup>
$A_d$	$1.33 \cdot 10^{15} \text{ m}^3/\text{s}$	$E_d$	<b>30700 cal/mol</b>
$A_p$	$4.41 \cdot 10^5 \text{ m}^3/\text{kmol s}$	$E_p$	<b>4350 cal/mol</b>
$A_{tc}$	$6.5 \cdot 10^7 \text{ m}^3/\text{kmol s}$	$E_{tc}$	<b>700 cal/mol</b>
$f$	<b>0.4</b>		

<sup>1</sup> Maschio and Moutier, 1989

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## Physical Properties

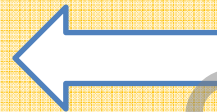
$$\log_{10} \mu = J_1 + \frac{J_2}{T} + J_3 T + J_4 T^2$$

$$J_1 = -7.7825$$

$$J_2 = 7.3478 \times 10^{-2}$$

$$J_3 = 1.0258 \times 10^{-2}$$

$$J_4 = -1.1343 \times 10^{-5}$$



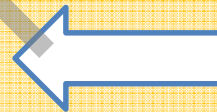
**Viscosity Correlation with Temperature <sup>1</sup>**

$$\log_{10} (\mu) = K' + a \log_{10} X_m + \log_{10} M_w^b$$

$$K' = -3.64 \times 10^1$$

$$a = 12.8$$

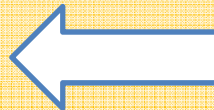
$$b = 3.4$$



**Viscosity Correlation with Conversion & Molecular Weight <sup>2</sup>**

$$\rho_m = 966.5 - 1.1(T - 273.15)$$

$$\rho_p = 1200 \text{ Kg} / \text{m}^3$$



**Density Correlation with Temperature <sup>3</sup>**

<sup>1</sup> Yaws, 1999

<sup>2</sup> Sangwai et al., 2006

<sup>3</sup> Baillagou & Soong, 1985

## Solving Procedure

- Space: 3D
- Time: Steady state
- BC on inlet → Velocity, Mass Fractions (M, S, I),  $T = 65^\circ \text{C}$
- UDF → Reaction Source
- HPCVL system → parallel with 24 CPUs

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## Effects of

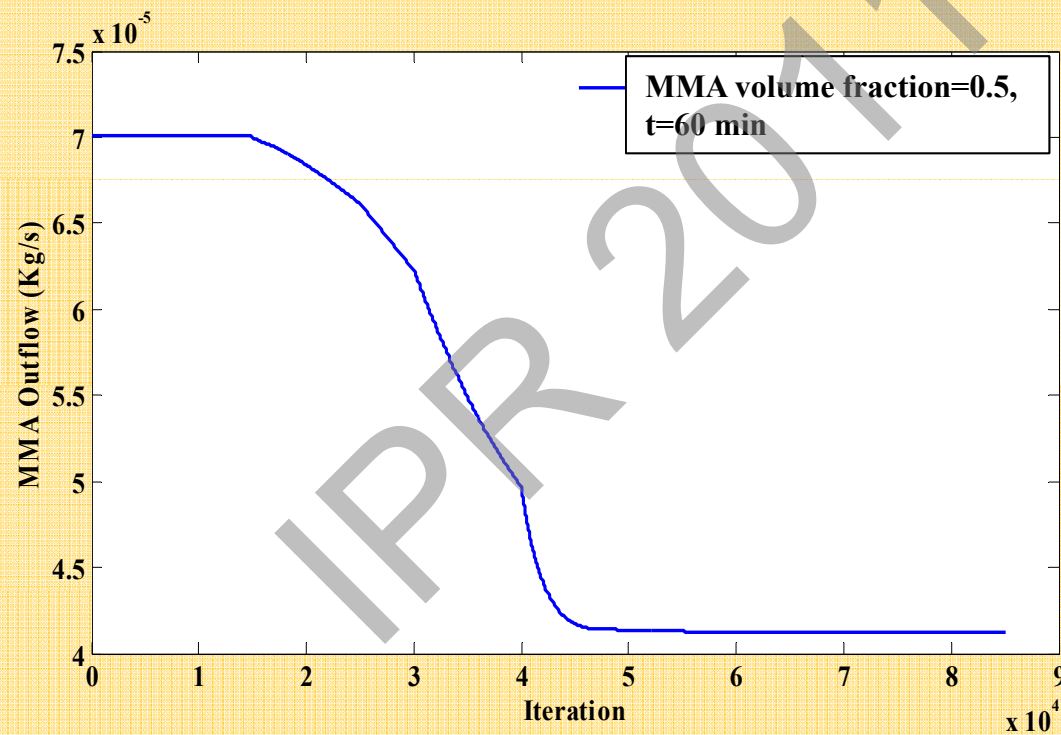
- Solvent Volume Fraction
- Residence Time
- Impeller Speed

## On

- Conversion of MMA Polymerization
- Contour of Monomer Mass Fraction
- Medium Viscosity

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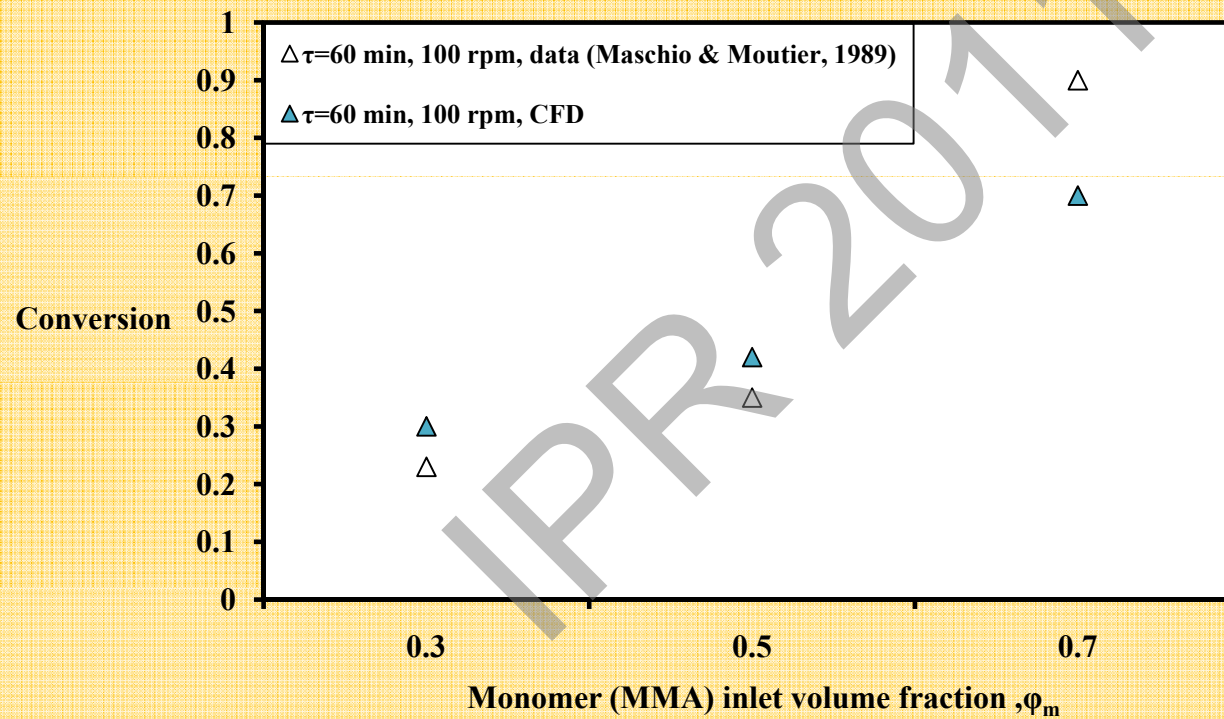
## Convergence Monitoring





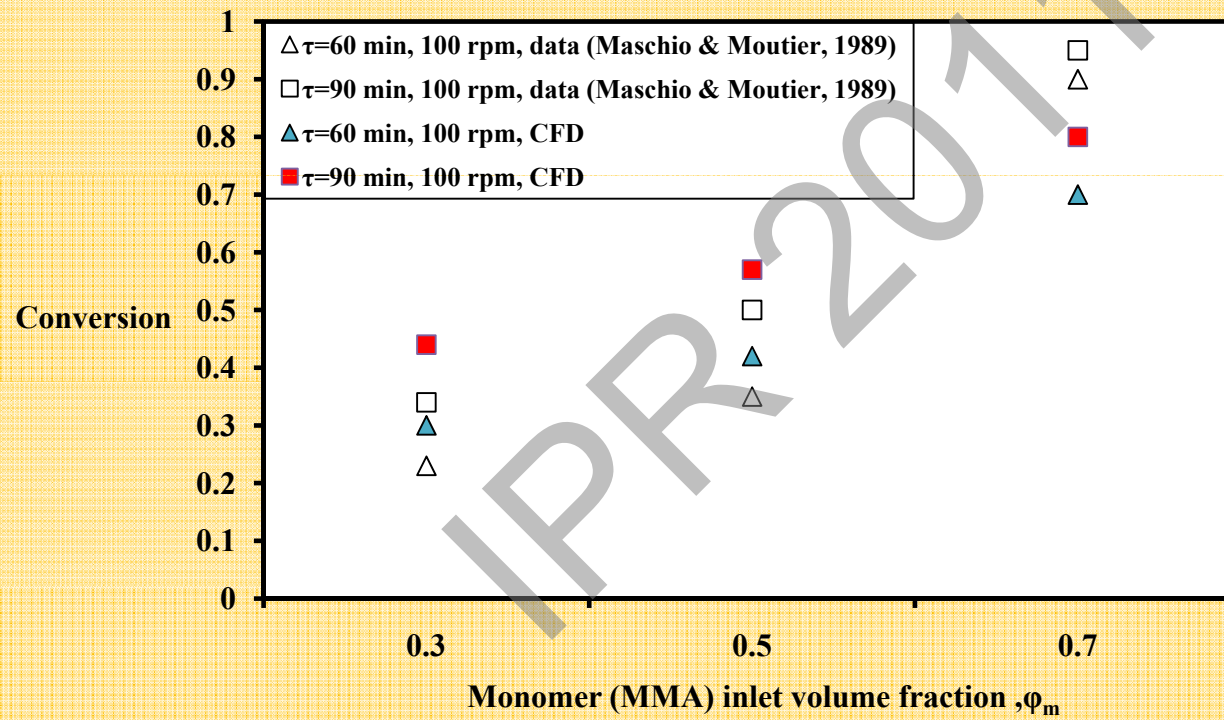
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## Effect of Solvent Fraction at 100 rpm



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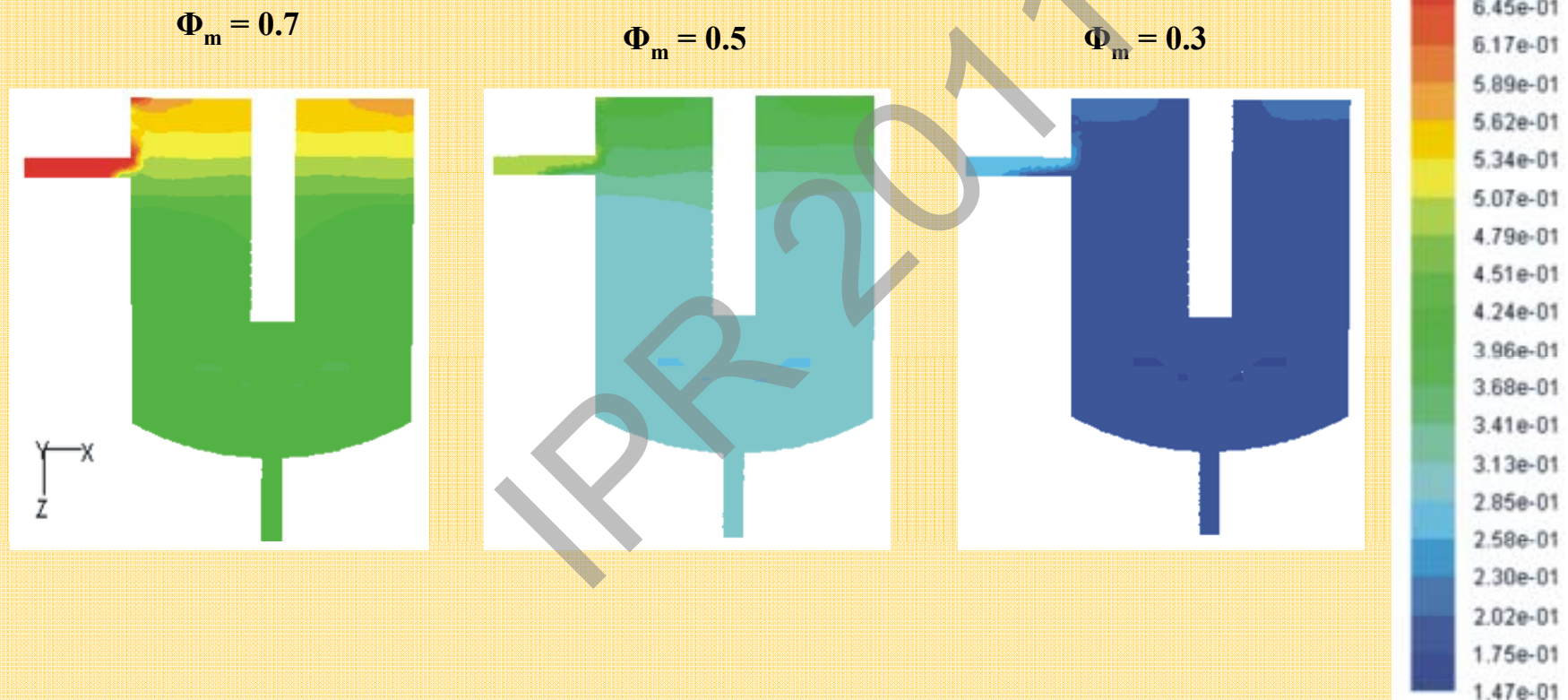
## Effect of Solvent Fraction at 100 rpm



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## Monomer Mass Fraction Contour

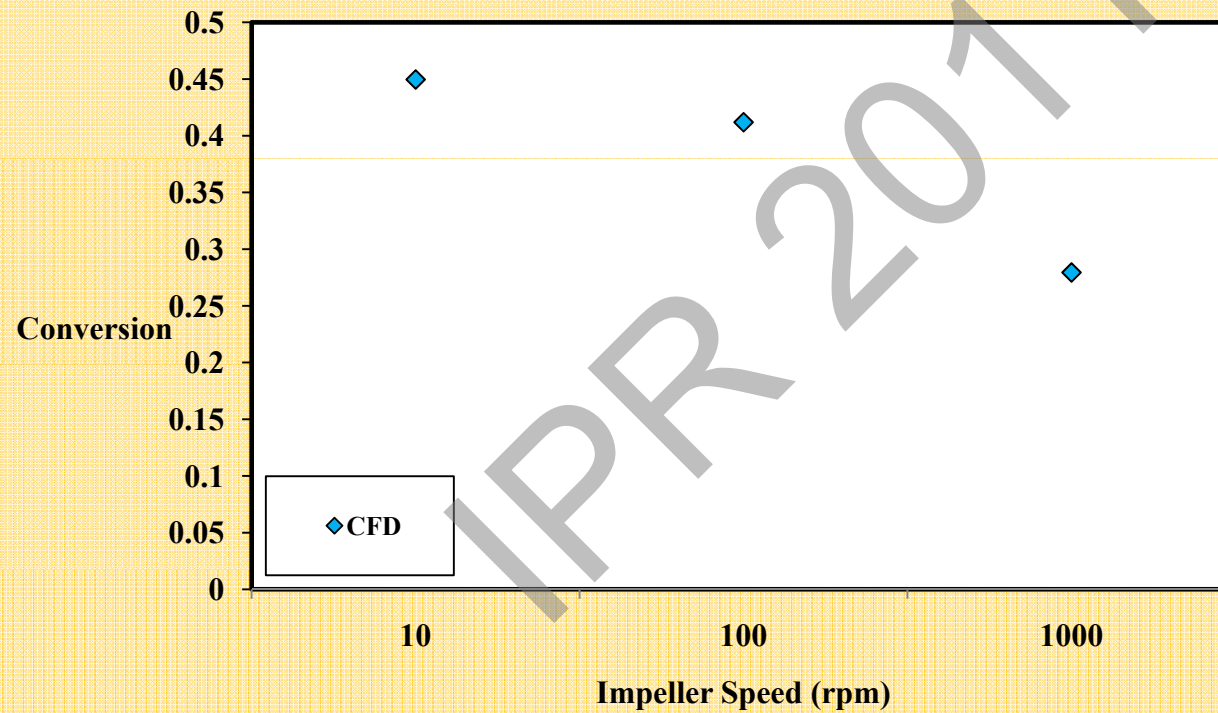
Impeller Speed = 100 rpm,  $\tau = 60$  min



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## Effect of Impeller Speed

$$\Phi_m = 0.5, \tau = 60 \text{ min}$$

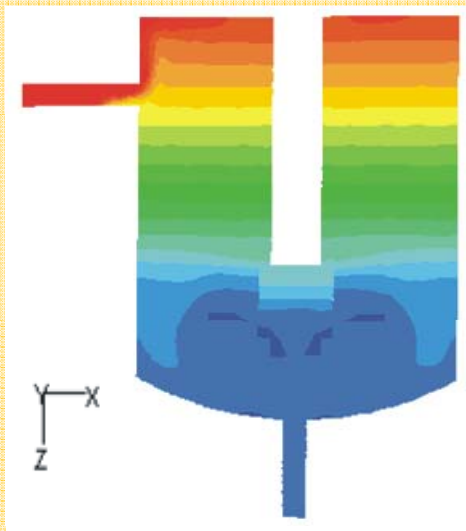


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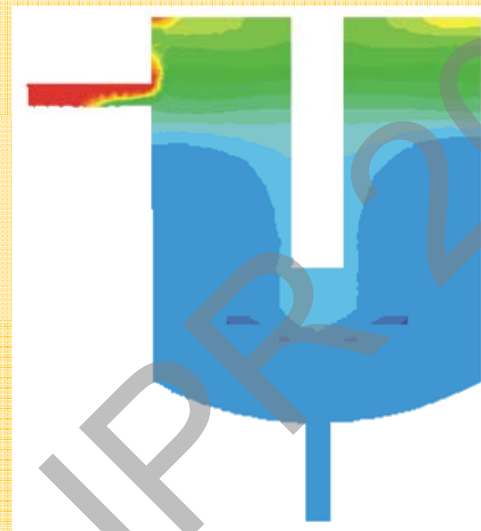
## Effect of Impeller Speed on homogeneity

$$\Phi_m = 0.5, \tau = 60 \text{ min}$$

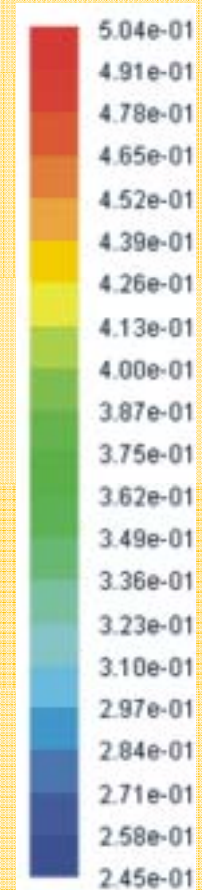
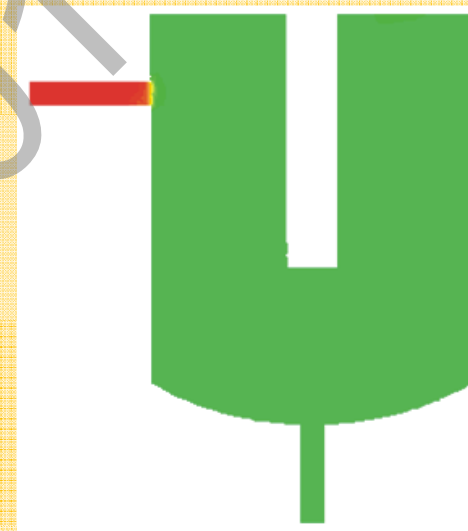
10 rpm



100 rpm



1000 rpm

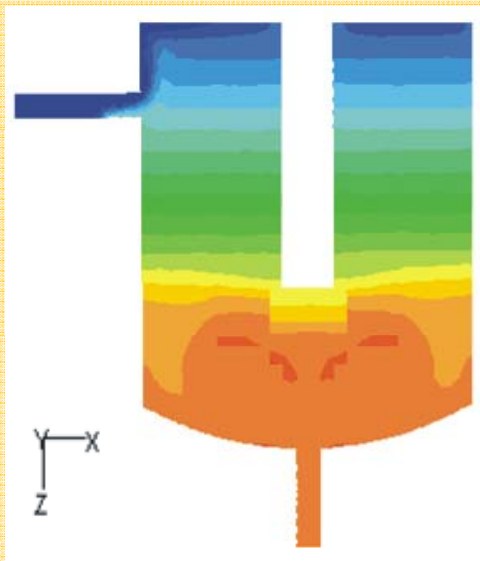


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## Effect of Impeller Speed on Viscosity

$$\Phi_m = 0.5, \tau = 60 \text{ min}$$

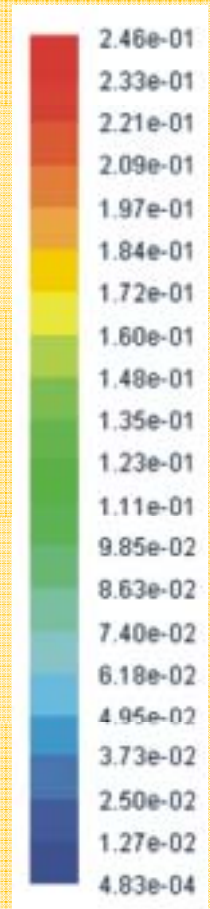
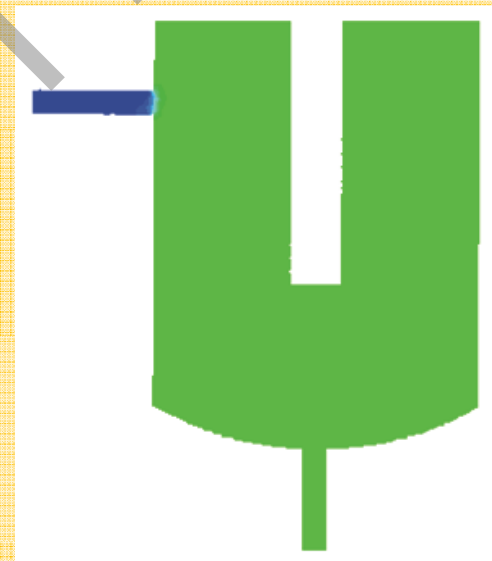
10 rpm



100 rpm



1000 rpm



Pa. Second

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- CFD gave good prediction for conversion at different solvent fractions and different residence times**
- CFD showed decrease in conversion with increase in impeller speed at fixed solvent fraction and residence time**
- Homogeneity of medium was improved at higher impeller speeds**

## **Acknowledgements:**

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- Supervisors: Dr. Ein-Mozaffari and Dr. Dhib**

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**Thanks for your attention**

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