Energy-Efficient Actuator Design Principles for Robotic Leg Prostheses and Exoskeletons: A Review of Series Elasticity and Backdrivability

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17 ABSTRACT

18 Robotic leg prostheses and exoskeletons have traditionally been designed using highly-geared motor-19 transmission systems that minimally exploit the passive dynamics of human locomotion, resulting in 20 inefficient actuators that require significant energy consumption and thus provide limited battery-powered 21 operation or require large onboard batteries. Here we review two of the leading energy-efficient actuator 22 design principles for legged and wearable robotic systems: series elasticity and backdrivability. As shown by 23 inverse dynamic simulations of walking, there are periods of negative joint mechanical work that can be used 24 to increase efficiency by recycling some of the otherwise dissipated energy using series elastic actuators 25 and/or backdriveable actuators with energy regeneration. Series elastic actuators can improve shock 26 tolerance during foot-ground impacts and reduce the peak power and energy consumption of the electric 27 motor via mechanical energy storage and return. However, actuators with series elasticity tend to have lower 28 output torque, increased mass and architecture complexity due to the added physical spring, and limited force 29 and torque control bandwidth. High torque density motors with low-ratio transmissions, known as quasi-30 direct drives, can likewise achieve low output impedance and high backdrivability, allowing for safe and 31 compliant human-robot physical interactions, in addition to energy regeneration. However, torque-dense 32 motors tend to have higher Joule heating losses, greater motor mass and inertia, and require specialized 33 motor drivers for real-time control. While each actuator design has advantages and drawbacks, designers 34 should consider the energy-efficiency of robotic leg prostheses and exoskeletons beyond steady-state level-35 ground walking.

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37 Keywords: Actuators, Legged Locomotion, Prosthetics, Exoskeletons, Wearable Robotics, Energy-Efficiency

39 1. INTRODUCTION

40 Robotic leg prostheses and exoskeletons can replace the propulsive function of 41 amputated or impaired biological muscles and allow persons with mobility impairments to 42 perform daily locomotor activities that require positive power generation via motorized 43 hip, knee, and/or ankle joints [1-4]. These wearable robotic systems feature biomimetic 44 design principles, whereby the actuators and mechanical structure mimic the human 45 musculoskeletal system, the sensors and controller mimic the peripheral and central 46 nervous systems, respectively, and the batteries mimic the metabolic power sources. 47 Although early device designs used actuators like hydraulic systems tethered to off-board 48 fluid pumps [5-7], the field has largely shifted towards using electromagnetic actuators for 49 onboard power generation, specifically brushed and brushless direct current (DC) motors 50 [1-4]. Electric motors tend to be most efficient at low torques and high speeds, with torque 51 and power densities around 15 Nm/kg and 200 W/kg, respectively, with an efficiency of 52 ~90% [8]. For comparison, human muscles have torque and power densities around 20 53 Nm/kg and 50 W/kg, respectively, with an efficiency of ~30% during concentric 54 contractions [8].

High-speed motors are often coupled with a high-ratio transmission (e.g., ballscrew mechanism or harmonic gearing) to increase the motor torque output to that needed for legged locomotion. This design causes the robotic actuator to have high output impedance (i.e., mechanically stiff), which allows for precision position control [9]. For example, commercial powered lower-limb exoskeletons use stiff actuators to rigidly track predefined kinematic trajectories, which can benefit those with limited ability to physically

interact with and control the robotic device (e.g., persons with complete paralysis) [4].
However, these highly-geared motor-transmission systems minimally exploit the passive
dynamics of human locomotion and/or other energy storage and return mechanisms [2,
9].

65 Traditional rigid actuators used in robotics tend to be energy inefficient, which can 66 increase the energy consumption and thus decrease the battery-powered operating times 67 or require larger onboard batteries [3-4]. For example, [10] reported that robotic knee prostheses under research and development weigh 2-5 kg and provide only 3 ± 2 hours of 68 69 maximum battery-powered operation. Similarly, most robotic lower-limb exoskeletons 70 provide only 1-5 hours of operating time [4]. Onboard portable power has often been 71 considered one of the leading challenges to developing robotic exoskeletons for real-world 72 environments [3-4]. Increased device mass and inertia could require more effort by the 73 human musculoskeletal system during swing phase, therein reducing locomotor efficiency 74 via higher metabolic power consumption [11]. For socket-suspended prostheses, 75 increased mass could also cause pain and discomfort due to greater tensile forces on the 76 human-prosthesis interface [12-13]. Highly-geared motor-transmission systems also 1) 77 introduce nonlinearities like friction and backlash, which make torque prediction from the 78 motor current more challenging, 2) introduce compliance, which can cause resonance 79 issues, 3) generate higher acoustic noise from meshing gears, and 4) increase wear and the 80 need for maintenance [14].

81 Motivated by these limitations and building on our previous review on regenerative
82 braking [15], here we review two of the leading energy-efficient actuator design principles

83 for legged and wearable robotic systems: series elasticity and backdrivability. The goal of 84 this review is to inform next-generation designers of robotic leg prostheses and 85 exoskeletons of the state-of-the-art in energy-efficient systems for human-robot 86 locomotion. Here the terms robotic and powered are used synonymously such that both 87 systems can generate positive mechanical power. Accordingly, we did not focus on purely 88 passive designs (e.g., the C-Leg prosthesis by Ottobock) or semi-powered systems (e.g., the 89 Proprio Foot prosthesis by Össur). Furthermore, while some systems have used parallel 90 elastic elements [16-18], these designs are less prevalent compared to series elasticity and 91 thus were not the main focus of our review. We organized the paper into the following 92 sections: 1) the mechanical energetics of legged locomotion with an emphasis on human 93 walking, 2) the design of series elastic actuators and examples of devices that include 94 mechanical energy storage and return, and 3) the design of backdriveable actuators with 95 low impedance transmissions and examples of devices that include energy regeneration, 96 including biomechanical energy harvesting.

97 2. ENERGY-EFFICIENT ACTUATION

98 Designers of robotic leg prostheses and exoskeletons are increasingly moving 99 towards using more efficient actuators that exploit the mechanical energetics of human 100 locomotion, including series elastic actuators and/or backdriveable actuators with energy 101 regeneration, as subsequently reviewed. However, given that the biomechanics of walking 102 is fundamental to the design of wearable robotic systems, the mechanical energetics of 103 human locomotion are first discussed.

104 2.1 Energetics of Human Locomotion

105 Here joint mechanical power is defined as the product of the net joint torque and 106 angular velocity, and joint mechanical work is the cumulative time-integral of the joint 107 mechanical power. During energy generation, the net joint torque and angular velocity 108 have the same sign direction and positive mechanical work is done (e.g., a concentric 109 contraction wherein the biological muscles shorten under tension). During energy 110 absorption, the net joint torque and angular velocity have opposite polarities and negative 111 mechanical work is done (e.g., an eccentric contraction wherein the biological muscles 112 lengthen under tension). This assumes that the joint torque generators are independent 113 of adjacent joints such that biarticulating muscles spanning multiple joints are ignored. The 114 net rate of energy generation and absorption by all muscles crossing the joint is the joint 115 mechanical power. During walking, some mechanical energy can be recycled by 116 conservative forces (e.g., the elastic storage and return of muscle-tendon units or the 117 pendular dynamics of swinging limbs) and transferred between adjacent segments [19]. 118 Most models of human locomotion ignore the elastic potential energy of deformable segments since the amount of deformation is relatively small and difficult to measure [19-119 120 21].

The energetics of human walking can be modelled by the mechanical work and power done on the total body system, as shown by Donelan and colleagues [22-24]. During single support, the stance leg resembles an inverted pendulum such that no net mechanical work is needed to move the center of mass (COM) and energy is conserved. During step-to-step transitions, however, external mechanical work by ground reaction forces is needed to redirect the body's COM velocity from one pendulum arc to another,

127	which is a major determinant of the metabolic cost of human locomotion [24]. To maintain
128	steady-state level-ground walking, the leading leg performs negative mechanical work to
129	redirect the COM velocity at foot-ground contact, while the trailing leg simultaneously
130	performs positive mechanical work during push-off to restore the lost energy [22-23]. For
131	example, when walking at 1.25 m/s, 15.4 \pm 2.6 J of positive external mechanical work is
132	done by the trailing leg and 12.4 \pm 3.1 J of negative external mechanical work is done by
133	the leading leg [24]. In theory, the net mechanical work during level-ground walking at
134	constant speed should be nearly zero since there is no net change in the gravitational
135	potential energy or translational kinetic energy of the total body system. However,
136	compared to external mechanical work done on the center of mass, joint mechanical work
137	can more accurately model the human musculotendon work [25] and can be used to study
138	the distribution of energy generation and absorption throughout the lower-limbs [26-27].
139	Gregg and colleagues recently studied the joint mechanical power during walking
140	using inverse dynamics [28] (Fig. 1). They developed an open-source biomechanics dataset
141	to aid the development of biomechanical models of human locomotion and the design and
142	control of wearable robotic systems. The dataset includes, among other variables, the hip,
143	knee, and ankle joint mechanical power of ten (n=10) able-bodied subjects (age: 30 \pm 15
144	years, height: 1.73 \pm 0.94 m, weight: 74.6 \pm 9.7 kg) walking at variable speeds and slopes.
145	3D-kinematics and ground reaction forces were measured using an optical motion capture
146	system and an instrumented split-belt treadmill, respectively. The joint mechanical power
147	$\left(P_{j} ight)$ in the sagittal plane was calculated from rigid-body inverse dynamics (i.e., the dot
148	product of the net joint torque (au_j) and angular velocity $(\dot{ heta}_j)$) $\{P_j = au_j \dot{ heta}_j\}$. The joint

149 mechanical power (W/kg) was normalized to total body mass and percent stride (0-100%) 150 to allow for between and within subject averaging, and interpolated heel-strike to heel-151 strike to have the same length. It is important to mention that muscle work, not necessarily 152 joint work, is related to the metabolic energetics of human movement. Accordingly, the 153 design and control of an actuation system based on only joint mechanical work and power 154 could bring about a metabolic penalty such that the net joint work is negative but some 155 muscles crossing the joint could be doing positive work. This knowledge of the 156 musculoskeletal system is especially pertinent to exoskeleton systems, which operate in 157 parallel with human muscles.

158 As shown in Fig. 1, the knee joint generally behaves like a damper mechanism 159 during walking, performing net negative mechanical work with four main power phases: 1) 160 negative mechanical power absorption at weight acceptance wherein the knee flexes 161 under the control of an extensor moment, 2) positive mechanical power generation by the 162 knee extensors during mid-stance such that the product of the extensor moment and 163 angular velocity is positive, 3) negative mechanical power absorption by the extensors as 164 the knee flexes during early swing, and 4) negative mechanical power absorption by the 165 knee flexors during late swing to decelerate leg extension prior to heel-strike. In contrast, 166 the ankle joint generally behaves like an actuating motor, performing net positive 167 mechanical work with two main power phases: 1) negative mechanical power absorption 168 at weight acceptance wherein the product of the plantarflexor moment and dorsiflexor 169 velocity is negative, and 2) a significant positive mechanical power burst by the 170 plantarflexors during push-off. The hip joint power is relatively small and irregular. The

171 joint mechanical power can be integrated over time to estimate the joint mechanical 172 energy generated and absorbed during walking. These periods of negative joint mechanical 173 work present an opportunity to improve actuator efficiency of robotic leg prostheses and 174 exoskeletons by recycling some of the otherwise dissipated energy using series elastic 175 actuators and/or backdriveable actuators with energy regeneration.

176 2.2 Series Elastic Actuators

177 Elasticity is a mechanical principle that can promote safe and efficient physical 178 interactions, which is important for wearable robotics. One popular engineering design, 179 pioneered by Pratt and Williamson [29], is to connect a passive elastic element (e.g., 180 mechanical spring) in series between the actuator and external load, known as a series 181 elastic actuator (Fig. 1). Compared to traditional rigid motor-transmission systems used in 182 robotics, series elastic actuators have lower output impedance, greater shock tolerance 183 and efficiency during foot-ground impacts, higher backdrivability via lower reflected 184 inertia, and can store and return elastic energy during periods of negative and positive 185 mechanical work, respectively [29]. Energy recycling via series compliance can improve 186 actuator efficiency by reducing the peak power and energy consumption of the electric 187 motor, the quantity of which is dependent on the elastic element design (i.e., the spring-188 mass system dynamics ideally matches the external load, thus requiring only a reactionary 189 torque by the motor) [11, 16]. This actuator design is bioinspired such that the elastic 190 element stores and returns mechanical energy similar to human muscle-tendon units as 191 characterized by Hill muscle models with both active contractile and series elastic elements 192 [21].

193 Since series elasticity can reduce the mechanical power and torque requirements 194 of the electric motor, this can further improve locomotor efficiency by reducing the size 195 and weight of the onboard motors and batteries. Energy efficiency in legged locomotion can be quantified using cost of transport $\left\{COT = \frac{E}{Mgd}\right\}$, where E is the energy consumed 196 197 by a system of mass (M) to travel distance (d) [11]. For example, the Cassie bipedal robot, 198 designed based on passive dynamics and series elastic actuation, has a cost of transport of 199 \sim 0.7 such that the 30 kg robot consumes 200 W of electrical power while walking at 1 m/s 200 [11]. In comparison, humans have a cost of transport of around 0.2. The hydraulically-201 actuated Big Dog quadrupedal robot has a cost of transport of ~15 [11].

202 Series elastic actuators have also been applied to robotic leg prostheses and 203 exoskeletons (Fig. 2). For example, [30] published on modelling and optimal control of an 204 energy-recycling actuator with an electroadhesive clutch and spring arranged in parallel 205 with the electric motor. Their simulations showed that including parallel elasticity in the 206 actuator design reduced the electrical power consumption by ~57%. In another example, 207 Gregg and colleagues used non-parametric convex optimization to optimize the stiffness 208 of the elastic element to minimize peak power and energy consumption for arbitrary 209 reference trajectories while satisfying actuator constraints [31-34]. Adding their optimized 210 spring element to a robotic ankle prosthesis reduced the peak power and energy 211 consumption during walking from 450 W to 132 W and from 33 J to 25 J per stride, 212 respectively [34]. Other examples of wearable robotics using series elastic actuators 213 include [17-18, 35-40].

214 Herr and colleagues developed several generations of robotic knee prostheses with 215 series elasticity [41-47]. One prototype included a continuously variable transmission 216 between the motor and elastic element to operate the motor at optimal torque-speed 217 regimes with highest efficiency by continuously varying the transmission ratio [44]. 218 Another prototype included a clutchable series elastic actuator, whereby an 219 electromagnetic clutch arranged in parallel with the series elastic actuator supplied a 220 reactionary torque when the task dynamics were elastically conservative and mechanical 221 energy was recycled by the spring element [41, 46]. The clutchable series elastic actuator 222 consumed ~70% less electrical energy during walking compared to a series elastic actuator 223 without the clutch mechanism [41]. Despite these performance benefits, actuators with 224 series elasticity tend to have lower output torque, increased mass and architecture 225 complexity due to the added physical spring, and limited force and torque control 226 bandwidth [1].

227 2.3 Regenerative Actuators

228 2.3.1 Backdrivability

In recent years, torque-dense motors with low-ratio transmissions (<20:1), known as quasidirect drives, have been used to likewise achieve low output impedance and high backdrivability and efficiency [48]. The use of low transmission ratios in legged and wearable robotic systems has been growing due to advances in torque-dense "pancake" motors [49] largely driven by the drone industry. These actuators generate high output torque by increasing the motor torque density (torque per unit mass) rather than the transmission ratio, therein circumventing the negative effects of high gearing (e.g.,

236 increased damping, backlash, acoustic noise, and reflected inertia, which scales with the 237 transmission ratio squared) [9]. Gears also have torque-dependent friction that further 238 increase impedance and reduce backdrivability and efficiency [8]. For wearable robotics 239 with high output impedance, the external loads experienced during daily locomotor 240 activities might be insufficient to overcome the impedance to backdrive the actuator. 241 These characteristics of highly-geared motor-transmission systems can impede dynamic 242 physical interactions between the human and robot and between the robot and 243 environment, which can especially encumber persons with partial motor control function 244 (e.g., elderly and/or those with osteoarthritis or poststroke) who may benefit from the 245 ability to backdrive the joints and actively participate in locomotion. Here backdrive torque 246 is defined as the minimum torque needed to overcome the actuator impedance (i.e., 247 reflected inertia and friction) to backdrive the motor through its transmission.

248 Compared to traditional rigid actuators used in robotics, backdriveable actuators with low 249 impedance transmissions have many benefits for control and efficiency, including: 1) free-250 swinging dynamic leg motion similar to passive prosthesis, which can simplify the control 251 during swing phase and allow for more natural, energy-efficient locomotion, 2) compliant 252 foot-ground impacts, 3) negligible unmodeled actuator dynamics, which can further 253 simplify the control, 4) intrinsic backdriveability comparable to series elastic actuators 254 without their design and manufacturing complexities and low bandwidth, and 5) energy 255 regeneration [48]. Energy regeneration is the process of converting some of the otherwise 256 dissipated energy during periods of negative mechanical work into electrical energy via 257 backdriving the actuator (Fig. 1). In other words, when backdriven by an external load, the

258 motor can provide a braking torque to decelerate the load (e.g., motion control during 259 swing phase) while concurrently generating electricity [15, 50-51]. This is similar to 260 regenerative braking in electric and hybrid electric vehicles.

During standard forward operation, an electric motor converts electrical power (P_e) into 261 mechanical power (P_m) such that the mechanical power output $\{P_m = \tau_j \dot{\theta}_j\}$ is the product 262 of the joint torque (τ_j) and angular speed $(\dot{\theta}_j)$ and the electrical power input $\{P_e = i_m v_M\}$ 263 is the product of the motor winding current (i_m) and voltage (v_m) . When backdriven by 264 265 an external load, the motor can operate like a generator, converting mechanical power into electrical power. The actuator efficiency (η_a) during forward operation is the ratio of 266 electrical-to-mechanical power conversion $\left\{\eta_a = \frac{1}{T} \left(\frac{\int \tau_j \dot{\theta}_j dt}{\int i_m v_m dt} \right) \times 100\% \right\}$ and vice-versa for 267 268 energy regeneration when backdriven. Assuming a sufficient motor driver to control 269 bidirectional power flow during motoring and braking operations, the regenerated energy 270 could be used for battery recharging and/or transferred to other joints to support positive 271 power generation. Backdriveable actuators with energy regeneration can thus help extend 272 the battery-powered autonomy and/or decrease the weight of the onboard batteries.

The MIT Cheetah was one of the first legged robots to use backdriveable actuators with energy regeneration [48, 52-55]. The robot was designed with torque-dense motors, low gearing, regenerative motor drivers, and low leg mass and inertia. The motor torque density was increased by increasing the gap radius, which is the radius of the gap between the stator windings and permanent magnets on the rotor. The low-ratio transmission (6:1) allowed for efficient bidirectional power flow between the motor and end effector. The forward and backdrive directional efficiencies of the transmission were 98% and 96%,

280 respectively, the differences of which were attributed to asymmetric friction and viscous 281 damping losses [52]. The actuator backdrive efficiency was ~63% [48]. The MIT Cheetah 282 achieved a cost of transport of ~0.5 such that the 33-kg robot can run at 6 m/s while 283 consuming 973 W of electrical power [48]. Approximately 76% of the power losses (P_{loss}) were attributed to Joule heating, which is expressed by $\{P_{loss} = i_m^2 R_m\}$, where R_m is the 284 285 resistance of the motor windings. To improve accessibility of these high-performance 286 actuators for legged locomotion, [56] recently proposed an open-source, 3D-printed 287 design.

288 Taking inspiration from the MIT Cheetah, [57-63] applied similar design principles 289 to wearable robotics to achieve a low impedance, high backdriveable interface between 290 the human and robot. They designed pancake-style brushless DC motors with 291 encapsulated windings for high torque-density. The large diameter of the motor allowed 292 for a low-ratio transmission (7:1) to be integrated inside the stator for a low form factor 293 [58]. Benchtop and human walking experiments with a robotic exoskeleton showed that 294 the actuator could generate 20-24 Nm of peak output torque and 1-3 Nm of backdrive 295 torque [57-60, 63], thus providing a high torque output during stance phase and a low 296 backdrive torque during swing phase. Their backdriveable actuators also allowed for 297 energy regeneration and sharing between joints for improved locomotor efficiency [61]. 298 To date, these wearable robotic systems are some of the few to demonstrate both power 299 generation and regeneration during walking. Other examples of robotic leg prostheses and 300 exoskeletons using backdriveable actuators include [64-68].

301 One of the biggest limitations to energy regeneration is the relatively low efficiency 302 of most motor-transmission systems [11]. Two of the leading sources of energy losses are 303 Joule heating in the motor windings and friction in the transmission [8-9]. High 304 transmission ratios can reduce the motor torque needed for legged locomotion, thus 305 decreasing the motor current and the associated Joule heating losses. However, high 306 gearing can also increase weight, friction, and reflected inertia, which increases impedance 307 and reduces backdrivability and the potential for energy regeneration [9]. Alternatively, 308 high torque-density motors can decrease the needed transmission ratios by generating 309 high output torque, thereby circumventing the inefficiencies of high gearing, although at 310 the expense of more winding current and thus higher Joule heating losses [8]. An open 311 challenge for the research community is to optimize the tradeoff between the actuator 312 output torque and backdrive torque. Many system design parameters can affect this 313 tradeoff (e.g., transmission ratio and efficiency, motor terminal resistance, and motor 314 torque and speed constants) [8]. Given the complex interactions between these different 315 parameters, determining the optimal actuator design via experimental trial-and-error can 316 be difficult. Modelling and simulation can be used to co-optimize the motor and 317 transmission system design parameters to optimize bidirectional efficiency (including 318 energy regeneration) and the actuator dynamics [69-70].

Despite the benefits of backdriveability via quasi-direct drives, high-torque motors tend to 1) require specialized motor drivers for real-time commutation and control, 2) have problems with thermal overheating due to difficulty evacuating heat, and 3) have higher motor mass and inertia due to the larger diameter [14].

323 2.3.2 Energy Regeneration

324 While the aforementioned robotic systems focused on backdrivability, a byproduct of 325 which is improved efficiency and the potential for energy regeneration, other systems have 326 been designed specifically for regenerative braking, as reviewed in our previous work [15]. 327 For example, the knee exoskeleton by Donelan and colleagues [71–75] was designed to 328 convert human biomechanical power into electrical power without requiring significant 329 metabolic effort. They used a 113:1 geared transmission and brushless DC generator to 330 harvest energy during late swing knee extension such that the motor assisted the muscles 331 to decelerate the swing leg prior to heel strike, therein minimizing the metabolic cost of 332 operating the muscles as biological brakes, while concurrently generating electricity. The 333 mechanical-to-electrical power conversion efficiency of the actuator was ~63% [74]. The 334 system performance was evaluated using cost of harvesting (COH), which is the additional metabolic effort needed to generate electrical power $\left\{COH = \frac{\Delta metabolic \ power}{\Delta electrical \ power}\right\}$. When 335 336 walking at 1.5 m/s, users were able to generate 4.8 \pm 0.8 W of electricity with a 5 \pm 21 W 337 increase in metabolic power consumption compared to walking with the system but not 338 generating electricity, therein yielding a cost of harvesting of 0.7 ± 4.4 W [74]. This knee 339 exoskeleton could be worn on the unaffected limb of persons with unilateral impairments 340 to help recharge a robotic leg prosthesis or exoskeleton worn on the contralateral affected 341 limb.

More recently, a collaborative research group [76-90] published a series of studies on modeling, optimization, and control of robotic and prosthetic systems with energy regeneration. They used biogeography-based optimization to search for the optimal design

345 and control parameters that maximized both energy regeneration and reference tracking 346 motion control. A Pareto front was used to evaluate the trade-off between the two 347 objective functions such that a higher impedance system tends to yield more accurate 348 motion tracking but less energy regeneration. For example, their multi-objective 349 optimization in [83] resulted in 0.9° of root mean square tracking error relative to 350 reference joint kinematics while regenerating ~53 J of electrical energy over 5-second 351 computer simulations of human-prosthesis walking. The energy regeneration efficiency 352 was 30%. A unique feature of their research was the use of ultracapacitors for storing the 353 regenerated energy.

354 Most robotic leg prostheses and exoskeletons are powered by lithium-polymer or lithium-355 ion batteries [1, 4]. Batteries tend to have a high energy density (e.g., ~100 Wh/kg), which 356 allows for extended operation, but a low power density (e.g., 0.1-1 kW/kg), which yields 357 slow charge and discharge rates [91]. However, in many mechatronics applications, the 358 rate at which mechanical energy should be converted into electrical energy for 359 regenerative braking is higher than the rate at which most batteries can absorb energy 360 [79]. In other words, rechargeable batteries tend to have insufficient power densities. In 361 contrast, ultracapacitors have a high-power density (e.g., ~10 kW/kg) but low energy 362 density (e.g., 1-10 Wh/kg), can charge and discharge at high rates without damage, and 363 have almost infinite lifecycles [91]. Ultracapacitors bridge the gap between conventional 364 capacitors [92–94] and batteries. Although the total energy stored per unit mass in 365 ultracapacitors is typically much smaller than batteries, recent breakthroughs in nanotechnology are enabling the fabrication of graphene-based ultracapacitors, which 366

have reached energy densities of ~64 Wh/kg [81]. Regenerative systems for robotic leg
prostheses and exoskeletons could include an ultracapacitor, for fast charging and
discharging, and a rechargeable battery, for extended operation.

370 **2.4** Applications

371 Despite these developments in energy-efficient actuators for wearable robotics, 372 previous studies have focused on steady-state level-ground walking - e.g., energy 373 regeneration [34, 71-74, 76, 79, 82-87, 89, 95-100] and mechanical energy storage and 374 return [17-18, 31, 34, 38-43, 45-46]. In real-world community mobility, however, steady-375 state locomotion is generally short lived and separated by frequent transitions between 376 different states (e.g., ~40% of walking bouts are less than 12 consecutive steps) [101]. This 377 observation is supported by [102-103], which recently showed that a relatively small 378 percentage (~8%) of real-world walking environments consist of continuous level-ground 379 terrain. Targeted users of wearable robotic systems (i.e., older adults and/or persons with 380 physical disabilities) also tend to walk slower and take fewer steps per day. For example, 381 self-selected walking speed and daily step count have been shown to decrease by 24% 382 from 25 to 75 years age and by 75% from 60 to 85 years age, respectively [104].

These differences, especially in walking speed, can have implications for energy recycling. Studies of robotic leg prostheses and exoskeletons with regenerative actuators have shown a positive correlation between walking speed and both energy regeneration and efficiency (i.e., faster walking generates more electricity and more efficiently) [61, 73-75, 89, 95-96, 105]. For a given back electromotive force (EMF) constant, an electric motor generates a voltage proportional to its rotational speed. Slower walking would backdrive

389 the actuator with lower speeds and thus generate less electricity. Motors are also generally 390 less efficient when generating torques at low speeds due to Joule heating. A recent study 391 by [61] showed that increasing walking speed with a robotic knee-ankle prosthesis from 392 0.9 m/s to 1.6 m/s increased the actuator power conversion efficiency from 40% to 59%. 393 [105] also showed that the ratio of regenerated energy to total power consumption using 394 a robotic ankle prosthesis increased from 27% to 35% when walking speed increased from 395 0.7 m/s to 1.3 m/s. Although several studies have recently simulated energy regeneration 396 in human-exoskeleton systems during stand-to-sit movements [106-107] and walking on 397 variable slopes and speeds [108], these studies were limited by model assumptions and 398 lacked experimental validation. Moving forward, designers should consider energy 399 regeneration, as well as mechanical energy storage and return, during locomotor activities 400 of daily living besides steady-state level-ground walking.

401 **3. CONCLUSION**

402 In this study, we reviewed two of the leading energy-efficient actuator design 403 principles for legged and wearable robotic systems: series elasticity and backdrivability. 404 Our goal is to inform next-generation designers of robotic leg prostheses and exoskeletons 405 of the state-of-the-art in energy-efficient actuators for human-robot locomotion. As shown 406 by inverse dynamic simulations of walking, there are periods of negative joint mechanical 407 power and work that can be used to improve efficiency by recycling some of the otherwise 408 dissipated mechanical energy using series elastic actuators and/or backdriveable actuators 409 with energy regeneration. Compared to traditional highly-geared motor-transmission 410 systems used in robotics, series elastic actuators can improve shock tolerance during foot-

411 ground impacts and reduce the peak power and energy consumption of the electric motor 412 via mechanical energy storage and return using a passive elastic element, the performance 413 of which is dependent on the spring design. However, actuators with series elasticity tend 414 to have lower output torque, increased mass and architecture complexity due to the added 415 physical spring, and limited force and torque control bandwidth.

416 High-torque density motors with low-ratio transmissions, known as quasi-direct 417 drives, can likewise achieve low output impedance and high backdrivability, therein 418 allowing for dynamic physical interactions, in addition to energy regeneration (i.e., the 419 conversion of mechanical energy into electrical energy via backdriving the motor). 420 However, torque-dense motors tend to have higher Joule heating losses due to higher 421 current draw, greater motor mass and inertia, and require specialized motor drivers for 422 real-time commutation and control. Quasi-direct drives are also typically more expensive 423 than traditional motor-transmission systems.

424 Although energy-efficient actuators can help extend the battery-powered 425 autonomy and/or decrease the weight of the onboard batteries, most robotic leg 426 prostheses and exoskeletons that have been designed for efficiency have been limited to 427 steady-state level-ground walking. However, targeted users of these wearable robotic 428 systems (e.g., older adults and/or persons with physical disabilities) often walk slower and 429 take fewer steps per day. Moving forward, designers should consider energy regeneration, and mechanical energy storage and return, during locomotor activities of daily living 430 431 besides continuous level-ground walking. In addition to robotic leg prostheses and

- 432 exoskeletons, these energy-efficient actuator design principles can also be applied to
- 433 humanoids and autonomous walking robots.

434 FUNDING

- 435 We want to thank the Natural Sciences and Engineering Research Council of Canada
- 436 (NSERC), the Waterloo Engineering Excellence PhD Fellowship program, and the Canada
- 437 Research Chairs (CRC) program for funding this research. This paper is dedicated to the
- 438 people of Ukraine in response to the 2022 Russian invasion and war.

440 **REFERENCES**

441

442 [1] Voloshina, A. S., and Collins, S. H., 2020, "Lower Limb Active Prosthetic Systems 443 Overview," Wearable Robotics: Systems and Applications, pp. 469–486. DOI:
444 10.1016/B978-0-12-814659-0.00023-0.

445

[2] Pieringer, D. S., Grimmer, M., Russold, M. F., and Riener, R., 2017, "Review of the
Actuators of Active Knee Prostheses and their Target Design Outputs for Activities of Daily
Living," 2017 International Conference on Rehabilitation Robotics (ICORR), London, pp.
1246–1253. DOI: 10.1109/ICORR.2017.8009420.

450

[3] Dollar, A. M., and Herr, H., 2008, "Lower Extremity Exoskeletons and Active Orthoses:
Challenges and State-of-the-Art," IEEE Trans. Robot., 24(1), pp. 144–158, DOI:
10.1109/TRO.2008.915453.

454

[4] Young, A. J., and Ferris, D. P., 2017, "State of the Art and Future Directions for Lower
Limb Robotic Exoskeletons," IEEE Trans. Neural Syst. Rehabil. Eng., 25(2), pp. 171–182,
DOI: 10.1109/TNSRE.2016.2521160.

458

459 [5] Kazerooni, H., and Steger, R., 2006, "The Berkeley Lower Extremity Exoskeleton," ASME460 J. Dyn. Syst. Meas. Control, 128, DOI: 10.1115/1.2168164.

461

[6] Zoss, A., and Kazerooni, H., 2005, "Architecture and Hydraulics of a Lower Extremity
Exoskeleton," in ASME 2005 International Mechanical Engineering Congress and
Exposition, Orlando, USA, pp. 1447–1455. DOI: 10.1115/IMECE2005-80129.

465

466 [7] Flowers, W, C., and Mann, R, W., 1977, "An Electrohydraulic Knee-Torque Controller
467 for a Prosthesis Simulator," ASME J. Biomech. Eng., 99(1), pp. 3–8, DOI:
468 10.1115/1.3426266.

469

[8] Hollerbach, J., Hunter, I., and Ballantyne, J., 1992, "A Comparative Analysis of Actuator
Technologies for Robotics," The Robotics Review 2, pp. 299–342.

472

473 [9] García, P. L., Crispel, S., Saerens, E., Verstraten, V., and Lefeber, D., 2020 "Compact
474 Gearboxes for Modern Robotics: A Review," Front. Robot. AI, 7, p. 103, DOI:
475 10.3389/frobt.2020.00103.

476

477 [10] Laschowski, B., and Andrysek, J., 2018, "Electromechanical Design of Robotic
478 Transfemoral Prostheses," ASME 2018 International Design Engineering Technical
479 Conferences & Computers and Information in Engineering Conference (IDETC/CIE),
480 Quebec City, Quebec, Canada, p. V05AT07A054. DOI: 10.1115/DETC2018-85234.

481

482 [11] Kashiri, N., et al., 2018, "An Overview on Principles for Energy Efficient Robot
483 Locomotion," Front. Robot. AI, 5, p. 129, DOI: 10.3389/frobt.2018.00129.

484 485 [12] Farina, D., et al., 2021 "Toward Higher-Performance Bionic Limbs for Wider Clinical 486 Use," Nat. Biomed. Eng., DOI: 10.1038/s41551-021-00732-x. 487 488 [13] Maryniak, A., Laschowski, B., and Andrysek, J., 2018, "Technical Overview of 489 Osseointegrated Transfemoral Prostheses: Orthopedic Surgery and Implant Design 490 Centered," ASME J. Eng. Sci. Med. Diagn. Ther., 1(2), p. 020801, DOI: 10.1115/1.4039105. 491 492 [14] Lopez Garcia, P., Saerens, E., Crispel, S., Varadharajan, A., Lefeber, D., and Verstraten, 493 T., 2022, "Factors Influencing Actuator's Backdrivability in Human-Centered Robotics," 494 MATEC Web Conf., 366, p. 01002, DOI: 10.1051/matecconf/202236601002. 495 496 [15] Laschowski, B., McPhee, J., and Andrysek, J., 2019, "Lower-Limb Prostheses and 497 Exoskeletons with Energy Regeneration: Mechatronic Design and Optimization Review," 498 ASME J. Mech. Robot., 11(4), p. 040801, DOI: 10.1115/1.4043460. 499 500 [16] Verstraten, T., Beckerle, P., Furnémont, R., Mathijssen, G., Vanderborght, B., and 501 Lefeber, D., 2016, "Series and Parallel Elastic Actuation: Impact of Natural Dynamics on 502 Power and Energy Consumption," Mech. Mach. Theory, 102, pp. 232–246, DOI: 503 10.1016/j.mechmachtheory.2016.04.004. 504 505 [17] Verstraten, T., Geeroms, J., Mathijssen, G., Convens, B., Vanderborght, B., and Lefeber, 506 D., 2017, "Optimizing the Power and Energy Consumption of Powered Prosthetic Ankles 507 with Series and Parallel Elasticity," Mech. Mach. Theory, 116, pp. 419–432, DOI: 508 10.1016/j.mechmachtheory.2017.06.004. 509 510 [18] Verstraten, T., Flynn, L., Geeroms, J., Vanderborght, B., and Lefeber, D., 2018, "On the 511 Electrical Energy Consumption of Active Ankle Prostheses with Series and Parallel Elastic 512 Elements," in 2018 7th IEEE International Conference on Biomedical Robotics and 513 Biomechatronics (Biorob), Enschede, pp. 720–725. DOI: 10.1109/BIOROB.2018.8487656. 514 515 [19] Winter, D. A., 1991, The Biomechanics and Motor Control of Human Gait: Normal, 516 Elderly and Pathological, 2nd Edition. Waterloo, Canada: Waterloo Biomechanics. 517 [20] Winter, D. A., 1983, "Energy Generation and Absorption at the Ankle and Knee during 518 519 Fast, Natural, and Slow Cadences," Clin. Orthop., 175, pp. 147–154, DOI: 520 10.1097/00003086-198305000-00021. 521 522 [21] Winter, D. A., 2009, Biomechanics and Motor Control of Human Movement, 4th ed. 523 Hoboken, N.J: Wiley. 524 525 [22] Donelan, J. M., Kram, R., and Kuo, A. D., 2002, "Mechanical Work for Step-to-Step 526 Transitions is a Major Determinant of the Metabolic Cost of Human Walking," J. Exp. Biol.,

527 205, pp. 3717–3727, DOI: 10.1242/jeb.205.23.3717.

528

[23] Donelan, J. M., Kram, R., and Kuo, A. D., 2002, "Simultaneous Positive and Negative 529 530 External Mechanical Work in Human Walking," J. Biomech., 35(1), pp. 117–124, DOI: 531 10.1016/S0021-9290(01)00169-5. 532 533 [24] Kuo, A. D., Donelan, J. M., and Ruina, A., 2005, "Energetic Consequences of Walking 534 Like an Inverted Pendulum: Step-to-Step Transitions," Exerc. Sport Sci. Rev., 33(2), pp. 88-535 97, DOI: 10.1097/00003677-200504000-00006. 536 537 [25] Sasaki, K., Neptune, R. R., and Kautz, S. A., 2009, "The Relationships Between Muscle, 538 External, Internal and Joint Mechanical Work during Normal Walking," J. Exp. Biol., 212(5), 539 pp. 738–744, DOI: 10.1242/jeb.023267. 540

[26] Farris, D. J., and Sawicki, G. S., 2012, "The Mechanics and Energetics of Human Walking
and Running: A Joint Level Perspective," J. R. Soc. Interface, 9(66), pp. 110–118, DOI:
10.1098/rsif.2011.0182.

544

- [27] Nuckols, R. W., Takahashi, K. Z., Farris, D. J., Mizrachi, S., Riemer, R., and Sawicki, G. S.,
 2020, "Mechanics of Walking and Running Up and Downhill: A Joint-Level Perspective to
 Guide Design of Lower-Limb Exoskeletons," PLOS ONE, 15(8), p. e0231996, DOI:
 10.1371/journal.pone.0231996.
- 549

[28] Reznick, E., Embry, K. R., Neuman, R., Bolívar-Nieto, E., Fey, N. P., and Gregg, R. D.,
2021 "Lower-Limb Kinematics and Kinetics during Continuously Varying Human
Locomotion," Sci. Data, 8(1), p. 282, DOI: 10.1038/s41597-021-01057-9.

553

[29] Pratt, G. A., and Williamson, M. M., 1995, "Series Elastic Actuators," in Proceedings
1995 IEEE/RSJ International Conference on Intelligent Robots and Systems. Human Robot
Interaction and Cooperative Robots, Pittsburgh, PA, USA, 1, pp. 399–406. DOI:
10.1109/IROS.1995.525827.

558

[30] Krimsky, E., and Collins, S. H., 2020 "Optimal Control of an Energy-Recycling Actuator
for Mobile Robotics Applications," in 2020 IEEE International Conference on Robotics and
Automation (ICRA), Paris, France, pp. 3559–3565. DOI:
10.1109/ICRA40945.2020.9196870.

563

[31] Bolivar, E., Rezazadeh, S., Summers, T., and Gregg, R. D., 2019, "Robust Optimal Design
of Energy Efficient Series Elastic Actuators: Application to a Powered Prosthetic Ankle," in
2019 IEEE 16th International Conference on Rehabilitation Robotics (ICORR), Toronto, ON,
Canada, pp. 740–747. DOI: 10.1109/ICORR.2019.8779446.

568

569 [32] Bolivar Nieto, E. A., Rezazadeh, S., and Gregg, R. D., 2019, "Minimizing Energy 570 Consumption and Peak Power of Series Elastic Actuators: A Convex Optimization 571 Framework for Elastic Element Design," IEEEASME Trans. Mechatron., 24(3), pp. 1334–
572 1345, DOI: 10.1109/TMECH.2019.2906887.

573

574 [33] Bolívar-Nieto, E. A., Thomas, G. C., Rouse, E., and Gregg, R. D., 2021, "Convex 575 Optimization for Spring Design in Series Elastic Actuators: From Theory to Practice," in 576 International Conference on Intelligent Robots and Systems (IROS), Prague, Czech 577 Republic, p. 6, DOI: 10.1109/IROS51168.2021.9636427.

578

[34] Bolívar, E., Rezazadeh, S., and Gregg, R., 2017, "A General Framework for Minimizing
Energy Consumption of Series Elastic Actuators with Regeneration," in ASME 2017
Dynamic Systems and Control Conference, Tysons, Virginia, USA, p. V001T36A005. DOI:
10.1115/DSCC2017-5373.

583

[35] Rouse, E. J., Mooney, L. M., and Hargrove, L. J., 2016, "The Design of a Lightweight,
Low Cost Robotic Knee Prosthesis with Selectable Series Elasticity," in 2016 6th IEEE
International Conference on Biomedical Robotics and Biomechatronics (BioRob),
Singapore, Singapore, pp. 1055–1055. DOI: 10.1109/BIOROB.2016.7523770.

588

[36] Kang, I., Peterson, R. R., Herrin, K. R., Mazumdar, A., and Young, A. J., 2022, "Design and Validation of a Torque-Controllable Series Elastic Actuator-Based Hip Exoskeleton for
Dynamic Locomotion," ASME J. Mech. Robot., p. 13, DOI: 10.1115/1.4054724.

592

593 [37] Vantilt, J., et al., 2019, "Model-Based Control for Exoskeletons with Series Elastic
594 Actuators Evaluated on Sit-to-Stand Movements," J. NeuroEngineering Rehabil., 16(1), p.
595 65, DOI: 10.1186/s12984-019-0526-8.

596

[38] Zhang, T., and Huang, H., 2019, "Design and Control of a Series Elastic Actuator with
Clutch for Hip Exoskeleton for Precise Assistive Magnitude and Timing Control and
Improved Mechanical Safety," IEEEASME Trans. Mechatron., 24(5), pp. 2215–2226, DOI:
10.1109/TMECH.2019.2932312.

601

[39] Dong, D., Ge, W., Convens, B., Sun, Y., Verstraten, T., and Vanderborght, B., 2020,
"Design, Optimization and Energetic Evaluation of an Efficient Fully Powered Ankle-Foot
Prosthesis with a Series Elastic Actuator," IEEE Access, 8, pp. 61491–61503, DOI:
10.1109/ACCESS.2020.2983518.

606

607 [40] Convens, B., et al., 2019, "Modeling, Design and Test-Bench Validation of a Semi608 Active Propulsive Ankle Prosthesis with a Clutched Series Elastic Actuator," IEEE Robot.
609 Autom. Lett., 4(2), pp. 1823–1830, DOI: 10.1109/LRA.2019.2897993.

610

611 [41] Rouse, E. J., Mooney, L. M., and Herr, H. M., 2014, "Clutchable Series-Elastic Actuator:

Implications for Prosthetic Knee Design," Int. J. Robot. Res., 33(13), pp. 1611–1625, DOI:

61310.1177/0278364914545673.

615 [42] Martinez-Villalpando, E. C., and Herr, H., 2009, "Agonist-Antagonist Active Knee
616 Prosthesis: A Preliminary Study in Level-Ground Walking," J. Rehabil. Res. Dev., 46(3), pp.
617 361–374, DOI: 10.1682/JRRD.2008.09.0131.

618

619 [43] Martinez-Villalpando, E. C., Mooney, L., Elliott, G., and Herr, H., 2011, "Antagonistic 620 Active Knee Prosthesis. A Metabolic Cost of Walking Comparison with a Variable-Damping 621 Prosthetic Knee," in 2011 Annual International Conference of the IEEE Engineering in 622 Society, Medicine and Biology Boston, MA, pp. 8519-8522. DOI: 623 10.1109/IEMBS.2011.6092102.

624

[44] Mooney, L., and Herr, H., 2013, "Continuously-Variable Series-Elastic Actuator," in
2013 IEEE 13th International Conference on Rehabilitation Robotics (ICORR), Seattle, WA,
pp. 1–6. DOI: 10.1109/ICORR.2013.6650402.

628

[45] Carney, M. E., Shu, T., Stolyarov, R., Duval, J. F., and Herr, H. M., 2021, "Design and
Preliminary Results of a Reaction Force Series Elastic Actuator for Bionic Knee and Ankle
Prostheses," IEEE Trans. Med. Robot. Bionics, 3(3), pp. 542–553, DOI:
10.1109/TMRB.2021.3098921.

633

[46] Rouse, E. J., Mooney, L. M., Martinez-Villalpando, E. C., and Herr, H. M., 2013,
"Clutchable Series-Elastic Actuator: Design of a Robotic Knee Prosthesis for Minimum
Energy Consumption," in 2013 IEEE 13th International Conference on Rehabilitation
Robotics (ICORR), Seattle, WA, pp. 1–6. DOI: 10.1109/ICORR.2013.6650383.

638

[47] Martinez- Villalpando, E. C., Weber, J., Elliott, G., and Herr, H., 2008, "Design of an
Agonist-Antagonist Active Knee Prosthesis," in 2008 2nd IEEE RAS & EMBS International
Conference on Biomedical Robotics and Biomechatronics, Scottsdale, AZ, USA, pp. 529–
534. DOI: 10.1109/BIOROB.2008.4762919.

643

[48] Seok, S., et al., 2015, "Design Principles for Energy-Efficient Legged Locomotion and
Implementation on the MIT Cheetah Robot," IEEEASME Trans. Mechatron., 20(3), pp.
1117–1129, DOI: 10.1109/TMECH.2014.2339013.

647

[49] Sensinger, J. W., Clark, S. D., and Schorsch, J. F., 2011, "Exterior vs. Interior Rotors in
Robotic Brushless Motors," in 2011 IEEE International Conference on Robotics and
Automation (ICRA), Shanghai, China, pp. 2764–2770. DOI: 10.1109/ICRA.2011.5979940.

651

654

652 [50] Seth, B., and Flowers, W. C., 1990, "Generalized Actuator Concept for the Study of the
653 Efficiency of Energetic Systems," ASME J. Dyn. Syst. Meas. Control, 112(2), pp. 233–238.

[51] Vailati, L, G., and Goldfarb, M., 2022, "On Using a Brushless Motor as a Passive TorqueControllable Brake," ASME J. Dyn. Syst. Meas. Control, 144(9), p. 091001, DOI:
10.1115/1.4054733.

[52] Wang, A., and Kim, S., 2015, "Directional Efficiency in Geared Transmissions:
Characterization of Backdrivability Towards Improved Proprioceptive Control," in 2015
IEEE International Conference on Robotics and Automation (ICRA), Seattle, WA, USA, pp.
1055–1062. DOI: 10.1109/ICRA.2015.7139307.

663

[53] Seok, S., Wang, A., Otten, D., and Kim, S., 2012, "Actuator Design for High Force
Proprioceptive Control in Fast Legged Locomotion," in 2012 IEEE/RSJ International
Conference on Intelligent Robots and Systems (IROS 2012), Vilamoura-Algarve, Portugal,
pp. 1970–1975. DOI: 10.1109/IROS.2012.6386252.

668

[54] Seok, S., Wang, A., Chuah, M. Y., Otten, D., Lang, J., and Kim, S., 2013, "Design
Principles for Highly Efficient Quadrupeds and Implementation on the MIT Cheetah
Robot," in 2013 IEEE International Conference on Robotics and Automation (ICRA),
Karlsruhe, Germany, pp. 3307–3312. DOI: 10.1109/ICRA.2013.6631038.

673

[55] Wensing, P. M., Wang, A., Seok, S., Otten, D., Lang, J., and Kim, S., 2017,
"Proprioceptive Actuator Design in the MIT Cheetah: Impact Mitigation and HighBandwidth Physical Interaction for Dynamic Legged Robots," IEEE Trans. Robot., 33(3), pp.
509–522, DOI: 10.1109/TRO.2016.2640183.

678

[56] Urs, K., Adu, C. E., Rouse, E. J., and Moore, T. Y., 2022, "Design and Characterization
of 3D Printed, Open-Source Actuators for Legged Locomotion," in 2022 IEEE/RSJ
International Conference on Intelligent Robots and Systems (IROS), Kyoto, Japan. DOI:
10.1109/IROS47612.2022.9981940.

683

[57] Zhu, H., Doan, J., Stence, C., Lv, G., Elery, T., and Gregg, R., 2017, "Design and
Validation of a Torque Dense, Highly Backdrivable Powered Knee-Ankle Orthosis," in 2017
IEEE International Conference on Robotics and Automation (ICRA), Singapore, Singapore,
pp. 504–510. DOI: 10.1109/ICRA.2017.7989063.

688

[58] Zhu, H., Nesler, C., Divekar, N., Peddinti, V., and Gregg, R., 2021, "Design Principles for
Compact, Backdrivable Actuation in Partial-Assist Powered Knee Orthoses," IEEE/ASME
Trans. Mechatron., DOI: 10.1109/TMECH.2021.3053226.

692

[59] Zhu, H., Nesler, C., Divekar, N., Ahmad, M. T., and Gregg, R. D., 2019, "Design and
Validation of a Partial-Assist Knee Orthosis with Compact, Backdrivable Actuation," in 2019
IEEE 16th International Conference on Rehabilitation Robotics (ICORR), Toronto, ON,
Canada, pp. 917–924. DOI: 10.1109/ICORR.2019.8779479.

697

[60] Lv, G., Zhu, H., and Gregg, R. D., 2018, "On the Design and Control of Highly
Backdrivable Lower-Limb Exoskeletons: A Discussion of Past and Ongoing Work," IEEE
Control Syst., 38(6), pp. 88–113, DOI: 10.1109/MCS.2018.2866605.

[61] Elery, T., Rezazadeh, S., Nesler, C., and Gregg, R. D., 2020, "Design and Validation of a
Powered Knee–Ankle Prosthesis with High-Torque, Low-Impedance Actuators," IEEE Trans.
Robot., 36(6), pp. 1649–1668, DOI: 10.1109/TRO.2020.3005533.

705

[62] Elery, T., Rezazadeh, S., Nesler, C., Doan, J., Zhu, H., and Gregg, R. D., 2018, "Design and Benchtop Validation of a Powered Knee-Ankle Prosthesis with High-Torque, LowImpedance Actuators," in 2018 IEEE International Conference on Robotics and Automation (ICRA), Brisbane, QLD, pp. 2788–2795. DOI: 10.1109/ICRA.2018.8461259.

710

[63] Nesler, C., Thomas, G., Divekar, N., Rouse, E. J., and Gregg, R. D., 2022, "Enhancing
Voluntary Motion with Modular, Backdrivable, Powered Hip and Knee Orthoses," IEEE
Robot. Autom. Lett., DOI: 10.1109/LRA.2022.3145580.

714

[64] Huang, T. H., et al., 2022, "Modeling and Stiffness-Based Continuous Torque Control
of Lightweight Quasi-Direct-Drive Knee Exoskeletons for Versatile Walking Assistance,"
IEEE Trans. Robot., 38(3), pp. 1442–1459, DOI: 10.1109/TRO.2022.3170287.

718

[65] Wang, J., et al., 2018, "Comfort-Centered Design of a Lightweight and Backdrivable
Knee Exoskeleton," IEEE Robot. Autom. Lett., 3(4), pp. 4265–4272, DOI:
10.1109/LRA.2018.2864352.

722

[66] Yu, S., et al., 2019, "Design and Control of a High-Torque and Highly Backdrivable
Hybrid Soft Exoskeleton for Knee Injury Prevention During Squatting," IEEE Robot. Autom.
Lett., 4(4), pp. 4579–4586, DOI: 10.1109/LRA.2019.2931427.

726

[67] Yu, S., et al., 2020, "Quasi-Direct Drive Actuation for a Lightweight Hip Exoskeleton
with High Backdrivability and High Bandwidth," IEEEASME Trans. Mechatron., 25(4), pp.
1794–1802, DOI: 10.1109/TMECH.2020.2995134.

730

[68] Zhu, J., Jiao, C., Dominguez, I., Yu, S., and Su, H., 2022, "Design and Backdrivability
Modeling of a Portable High Torque Robotic Knee Prosthesis with Intrinsic Compliance for
Agile Activities," IEEEASME Trans. Mechatron., 27(4), pp. 1837–1845, DOI:
10.1109/TMECH.2022.3176255.

735

[69] Bartlett, H. L., Lawson, B. E., and Goldfarb, M., 2017, "Optimal Transmission Ratio
Selection for Electric Motor Driven Actuators with Known Output Torque and Motion
Trajectories," ASME J. Dyn. Syst. Meas. Control, 139(10), p. 101013, DOI:
10.1115/1.4036538.

740

[70] Rezazadeh, S., and Hurst, J. W., 2014, "On the Optimal Selection of Motors and
Transmissions for Electromechanical and Robotic Systems," in 2014 IEEE/RSJ International
Conference on Intelligent Robots and Systems, Chicago, USA, pp. 4605–4611, DOI:
10.1109/IROS.2014.6943215.

746 [71] Donelan, J. M., Li, Q., Naing, V., Hoffer, J. A., Weber, D. J., and Kuo, A. D., 2008, 747 "Biomechanical Energy Harvesting: Generating Electricity During Walking with Minimal 748 User Effort," Science, 319(5864), pp. 807–810, DOI: 10.1126/science.1149860. 749 750 [72] Donelan, J. M., Naing, V., and Li, Q., 2009, "Biomechanical Energy Harvesting," in 2009 751 Symposium, San Diego, CA, USA, p. 4. DOI: IEEE Radio and Wireless 752 10.1109/RWS.2009.4957269. 753 754 [73] Li, Q., Naing, V., Hoffer, J. A., Weber, D. J., Kuo, A. D., and Donelan, J. M., 2008, 755 "Biomechanical Energy Harvesting: Apparatus and Method," in 2008 IEEE International 756 Conference on Robotics and Automation (ICRA), Pasadena, CA, USA, pp. 3672–3677. DOI: 757 10.1109/ROBOT.2008.4543774. 758 759 [74] Li, Q., Naing, V., and Donelan, J. M., 2009, "Development of a Biomechanical Energy 760 Harvester," J. NeuroEngineering Rehabil., 6(1), p. 22, DOI: 10.1186/1743-0003-6-22. 761 762 [75] Selinger, J. C., and Donelan, J. M., 2016, "Myoelectric Control for Adaptable 763 Biomechanical Energy Harvesting," IEEE Trans. Neural Syst. Rehabil. Eng., 24(3), pp. 364– 764 373, DOI: 10.1109/TNSRE.2015.2510546. 765 766 [76] Barto, T., and Simon, D., 2017, "Neural Network Control of an Optimized Regenerative 767 Motor Drive for a Lower-Limb Prosthesis," in 2017 American Control Conference (ACC), 768 Seattle, WA, USA, pp. 5330–5335. DOI: 10.23919/ACC.2017.7963783. 769 770 [77] Ghorbanpour, A., and Richter, H., 2018, "Control with Optimal Energy Regeneration in 771 Robot Manipulators Driven by Brushless DC Motors," in ASME 2018 Dynamic Systems and 772 Control Conference, Atlanta, Georgia, USA, p. V001T04A003. DOI: 10.1115/DSCC2018-773 8972. 774 775 [78] Ghorbanpour, A., and Richter, H., 2020, "Energy-Optimal, Direct-Phase Control of 776 Brushless Motors for Robotic Drives," in ASME 2020 Dynamic Systems and Control 777 Conference, Virtual, Online, p. V001T05A006. DOI: 10.1115/DSCC2020-3200. 778 779 [79] Rarick, R., Richter, H., van den Bogert, A., Simon, D., Warner, H., and Barto, T., 2014, 780 "Optimal Design of a Transfemoral Prosthesis with Energy Storage and Regeneration," in 781 2014 American Control Conference (ACC), Portland, OR, USA, pp. 4108-4113. DOI: 782 10.1109/ACC.2014.6859051. 783 784 [80] Khalaf, P., and Richter, H., 2016, "Parametric Optimization of Stored Energy in Robots 785 with Regenerative Drive Systems," in 2016 IEEE International Conference on Advanced 786 Banff, AB, Canada, Intelligent Mechatronics (AIM), pp. 1424–1429. DOI: 787 10.1109/AIM.2016.7576970. 788

789 [81] Richter, H., 2015, "A Framework for Control of Robots with Energy Regeneration," 790 ASME J. Dyn. Syst. Meas. Control, 137(9), p. 091004, DOI: 10.1115/1.4030391. 791 792 [82] dos Santos, E. G., and Richter, H., 2018, "Modeling and Control of a Novel Variable-793 Stiffness Regenerative Actuator," in ASME 2018 Dynamic Systems and Control Conference, 794 Atlanta, Georgia, USA, p. V002T24A003. DOI: 10.1115/DSCC2018-9054. 795 796 [83] Khademi, G., Richter, H., and Simon, D., 2016, "Multi-Objective Optimization of 797 Tracking/Impedance Control for a Prosthetic Leg with Energy Regeneration," in 2016 IEEE 798 55th Conference on Decision and Control (CDC), Las Vegas, NV, USA, pp. 5322–5327. DOI: 799 10.1109/CDC.2016.7799085. 800 801 [84] Warner, H., Simon, D., and Richter, H., 2016, "Design Optimization and Control of a 802 Crank-Slider Actuator for a Lower-Limb Prosthesis with Energy Regeneration," in 2016 IEEE 803 International Conference on Advanced Intelligent Mechatronics (AIM), Banff, AB, Canada, 804 pp. 1430-1435. DOI: 10.1109/AIM.2016.7576971. 805 806 [85] Kim, B. H., and Richter, H., 2018, "Energy Regeneration-Based Hybrid Control for 807 Transfemoral Prosthetic Legs Using Four-Bar Mechanism," in IECON 2018 - 44th Annual 808 Conference of the IEEE Industrial Electronics Society, Washington, DC, USA, pp. 2516-809 2521. DOI: 10.1109/IECON.2018.8591399. 810 811 [86] Khademi, G., Mohammadi, H., Richter, H., and Simon, D., 2018, "Optimal Mixed 812 Tracking/Impedance Control with Application to Transfemoral Prostheses with Energy 813 Regeneration," IEEE Trans. Biomed. Eng., 65(4), pp. 894-910, DOI: 10.1109/TBME.2017.2725740. 814 815 816 [87] Rohani, F., Richter, H., and van den Bogert, A. J., 2017, "Optimal Design and Control of 817 an Electromechanical Transfemoral Prosthesis with Energy Regeneration," PLOS ONE, 818 12(11), p. e0188266, DOI: 10.1371/journal.pone.0188266. 819 820 [88] Khalaf, P., and Richter, H., 2018, "On Global, Closed-Form Solutions to Parametric 821 Optimization Problems for Robots with Energy Regeneration," ASME J. Dyn. Syst. Meas. 822 Control, 140(3), p. 031003, DOI: 10.1115/1.4037653. 823 824 [89] Khalaf, P., Warner, H., Hardin, E., Richter, H., and Simon, D., 2018, "Development and 825 Experimental Validation of an Energy Regenerative Prosthetic Knee Controller and 826 Prototype," in ASME 2018 Dynamic Systems and Control Conference, Atlanta, Georgia, 827 USA, p. V001T07A008. DOI: 10.1115/DSCC2018-9091. 828 829 [90] Ghorbanpour, A., and Richter, H., 2021, "A Novel Concept for Energy-Optimal, 830 Independent-Phase Control of Brushless Motor Drivers," ASME Lett. Dyn. Syst. Control, pp. 831 1–11, DOI: 10.1115/1.4052662.

833 834	[91] Burke, A. F., 2007, "Batteries and Ultracapacitors for Electric, Hybrid, and Fuel Cell Vehicles," Proc. IEEE, 95(4), pp. 806–820, DOI: 10.1109/JPROC.2007.892490.
835	
836	[92] Hunter, B., 1981, "Design of a Self-Contained, Active, Regenerative Computer
837 838	Controlled Above-Knee Prosthesis," PhD Thesis, Massachusetts Institute of Technology.
839	[93] Seth, B., 1987, "Energy Regeneration and Its Application to Active Above-Knee
840	Prostheses," PhD Thesis, Massachusetts Institute of Technology.
841	
842	[94] Tabor, K., 1988, "The Real-Time Digital Control of a Regenerative Above-Knee
843	Prosthesis," PhD Thesis, Massachusetts Institute of Technology.
844	
845	[95] Andrysek, J., and Chau, G., 2007, "An Electromechanical Swing-Phase-Controlled
846	Prosthetic Knee Joint for Conversion of Physiological Energy to Electrical Energy: Feasibility
847	Study," IEEE Trans. Biomed. Eng., 54(12), pp. 2276–2283, DOI:
848	10.1109/TBME.2007.908309.
849	
850	[96] Andrysek, J., Liang, T., and Steinnagel, B., 2009, "Evaluation of a Prosthetic Swing-
851	Phase Controller with Electrical Power Generation," IEEE Trans. Neural Syst. Rehabil. Eng.,
852	17(4), pp. 390–396, DOI: 10.1109/TNSRE.2009.2023292.
853	
854	[97] Tucker, M. R., and Fite, K. B., 2010, "Mechanical Damping with Electrical Regeneration
855	for a Powered Transfemoral Prosthesis," in 2010 IEEE/ASME International Conference on
856	Advanced Intelligent Mechatronics (AIM), Montreal, QC, Canada, pp. 13–18. DOI:
857	10.1109/AIM.2010.5695828.
858	
859	[98] Riemer, R., Nuckols, R. W., and Sawicki, G. S., 2021, "Extracting Electricity with Exosuit
860	Braking," Science, 372(6545), pp. 909–911, DOI: 10.1126/science.abh4007.
861	
862	[99] Schertzer, E., and Riemer, R., 2015, "Harvesting Biomechanical Energy or Carrying
863	Batteries? An Evaluation Method based on a Comparison of Metabolic Power," J.
864	NeuroEngineering Rehabil., 12(1), p. 30, DOI: 10.1186/s12984-015-0023-7.
865	
866	[100] Riemer, R., and Shapiro, A., 2011, "Biomechanical Energy Harvesting from Human
867	Motion: Theory, State of the Art, Design Guidelines, and Future Directions," J.
868	NeuroEngineering Rehabil., 8(1), p. 22, DOI: 10.1186/1743-0003-8-22.
869	
870	[101] Orendurff, M. S., Schoen, J., Bernatz, G., Segal, A., and Klute, G., 2008, "How Humans
871	Walk: Bout Duration, Steps per Bout, and Rest Duration," J. Rehabil. Res. Dev., 45(7), pp.
872	1077–1090, DOI: 10.1682/JRRD.2007.11.0197.
873	
874	[102] Laschowski, B., McNally, W., Wong, A., and McPhee, J., 2020, "ExoNet Database:
875	Wearable Camera Images of Human Locomotion Environments," Front. Robot. AI, 7, p.
876	562061, DOI: 10.3389/frobt.2020.562061.

877

- [103] Laschowski, B., McNally, W., Wong, A., and McPhee, J., 2022, "Environment
 Classification for Robotic Leg Prostheses and Exoskeletons using Deep Convolutional
 Neural Networks," Front. Neurorobotics, 15, p. 730965, DOI: 10.3389/fnbot.2021.730965.
- [104] Grimmer, M., Riener, R., Walsh, C. J., and Seyfarth, A., 2019, "Mobility Related
 Physical and Functional Losses due to Aging and Disease A Motivation for Lower Limb
 Exoskeletons," J. NeuroEngineering Rehabil., 16(1), p. 2, DOI: 10.1186/s12984-018-04588.
- 886

[105] Feng, Y., Mai, J., Agrawal, S. K., and Wang, Q., 2020, "Energy Regeneration From
Electromagnetic Induction by Human Dynamics for Lower Extremity Robotic Prostheses,"
IEEE Trans. Robot., 36(5), pp. 1442–1451, DOI: 10.1109/TRO.2020.2991969.

- 890
- [106] Laschowski, B., Razavian, R. S., and McPhee, J., 2021, "Simulation of Stand-to-Sit
 Biomechanics for Robotic Exoskeletons and Prostheses with Energy Regeneration," IEEE
 Trans. Med. Robot. Bionics, 3(2), pp. 455–462, DOI: 10.1109/TMRB.2021.3058323.
- 894
- [107] Laschowski, B., 2021, "Energy Regeneration and Environment Sensing for Robotic
 Leg Prostheses and Exoskeletons," PhD Thesis, University of Waterloo.
- 897

[108] Laschowski, B., Inkol, K. A., Mihailidis, A., and McPhee, J., 2022, "Simulation of Energy
 Regeneration in Human Locomotion for Efficient Exoskeleton Actuation," in 2022 9th IEEE
 RAS/EMBS International Conference for Biomedical Robotics and Biomechatronics
 (BiaBab) Securit Republic of Karao, DOI: 10.1100/BiaBab52680.2022.0025240

901 (BioRob), Seoul, Republic of Korea. DOI: 10.1109/BioRob52689.2022.9925349.

902 Figure Captions List

- 903
- Fig. 1 The average hip, knee, and ankle joint mechanical power (W/kg) per stride in healthy young adults (n=10) walking at 1 m/s on level-ground and normalized to total body mass (top left). The positive and negative values represent joint power generation and absorption, respectively. Data were calculated from [28], the trajectories of which begin and end with heelstrike (top right). These joint mechanical energetics have implications on the energy-efficient actuation of robotic leg prostheses and exoskeletons (bottom left); the nomenclature are described in the text.
- Fig. 2 Examples of robotic leg prostheses and exoskeletons with series elastic actuators (two images on the left) and backdriveable actuators with low impendence transmissions (two images on the right). The photographs (left to right) were provided by Tom Verstraten [39], Elliot Rouse [41], and Robert Gregg [61, 63].



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