## PMath 441/641 – Spring 2024

## Algebraic Number Theory Detailed Course Outline

The third column contains the section in the course notes corresponding to the topic to be covered that day in lecture, described in the fourth column.

| Date    | Day       | Notes    | Topic                                 |                        |
|---------|-----------|----------|---------------------------------------|------------------------|
| 6 May   | Monday    | 1        | What is an algebraic integer?         |                        |
| 8 May   | Wednesday | 13       | Modules                               |                        |
| 10 May  | Friday    | 2        | The ring of algebraic integers        |                        |
| 13 May  | Monday    | 3        | Norm and trace                        |                        |
| 15 May  | Wednesday | 3        | Additive structure of $\mathcal{O}_K$ | Homework 1 due         |
| 17 May  | Friday    | 3        | Dedekind domains                      | Quiz 1                 |
| 20 May  | Monday    |          | Victoria Day holiday                  |                        |
| 21 May  | Tuesday   | 4        | Geometry of numbers                   |                        |
| 22 May  | Wednesday | 4        | Minkowski space                       | Homework 2 due         |
| 24 May  | Friday    | 4        | More geometry of numbers              | Quiz 2                 |
| 27 May  | Monday    | 5        | Discriminants                         |                        |
| 29 May  | Wednesday | 5        | Norm and trace                        | Homework 3 due         |
| 31 May  | Friday    | 5        | Norm of an ideal                      | Quiz 3                 |
| 3 June  | Monday    | 5        | Norms and discriminants               |                        |
| 5 June  | Wednesday | 6        | Ideals of $\mathcal{O}_K$             | Homework 4 due         |
| 7 June  | Friday    | 16       | Finite rings                          | Quiz 4                 |
| 10 June | Monday    | 6        | Factoring ideals                      |                        |
| 12 June | Wednesday | 6        | More factoring                        | Homework 5 due         |
| 14 June | Friday    | 7        | More factoring of ideals              | $\operatorname{Quiz}5$ |
| 17 June | Monday    | 7        | Fractional ideals                     |                        |
| 19 June | Wednesday | 7        | Fractional ideals                     | Homework 6 due         |
| 21 June | Friday    | 7        | Dividing by ideals                    | Quiz 6                 |
| 24 June | Monday    | 18       | Local rings and DVRs                  |                        |
| 26 June | Wednesday | 18       | Local rings and DVRs                  | Homework 7 due         |
| 28 June | Friday    | 8        | Norm ideals are multiplicative        | Quiz 7                 |
| 1 July  | Monday    |          | Canada Day holiday                    |                        |
| 3 July  | Wednesday | 8        | Yet more ideal factoring              | Homework 8 due         |
| 5 July  | Friday    | 8        | Computing rings of integers           | Quiz 8                 |
| 8 July  | Monday    | 8        | Ramification and discriminants        |                        |
| 10 July | Wednesday | 9        | The class group                       |                        |
| 12 July | Friday    | $9,\!15$ | Computing the class group             |                        |
| 15 July | Monday    | 9-10,15  | More computing the class group        |                        |
| 17 July | Wednesday | 10       | Computing the class group             | Homework 9 due         |
| 19 July | Friday    | 10       | Still computing the class group       | Quiz 9                 |
| 22 July | Monday    | 11       | Units of $\mathcal{O}_K$              |                        |
| 24 July | Wednesday | 11,15    | Dirichlet's Unit Theorem              |                        |
| 26 July | Friday    | 12       | Showing an ideal is not principal     |                        |
| 29 July | Monday    |          | Review                                | Quiz 10 & Hmwk 10 due  |
|         |           |          |                                       |                        |