## AMATH 731 Fall 2019 Tentative Schedule

| Lecture | Date | Lecture Notes | Contents |
| :---: | :---: | :---: | :---: |
| 01 | Sep 5 | Lecture 1 | Review Real Analysis |
| 02 | Sep 10 | Lecture 2 <br> Assignment 1 <br> A1 Solutions | Review Linear Algebra <br> Normed Linear Spaces: Definitions and Examples |
| 03 | Sep 12 | Lecture 3 | Cauchy Sequences and Banach Spaces |
| 04 | Sep 17 | Lecture 4 | Completeness of $\left(C[a, b],\\|\cdot\\|_{\infty}\right)$ and $\left(L_{p}[a, b],\\|\cdot\\|_{p}\right)($ Riesz-Fischer Theorem) |
| 05 | Sep 19 | Lecture 5 | Open and Closed Sets; Convexity; Banach Fixed-Point Theorem and the Iteration Method. |
| 06 | Sep 24 | Lecture 6 | Applications of Banach Fixed Point Theorem to ODEs and Integral Equations |
| 07 | Sep 26 | Lecture 7 <br> Assignment 2 <br> A2 Solutions | Continuity; Equivalent Norms; <br> Compactness in Finite Dimensional Normed Spaces |
| 08 | Oct 1 | Lecture 8 | Compactness in Infinite Dimensional Normed Spaces; Compact Operators |
| 09 | Oct 3 | Lecture 9 | Schauder Fixed Point Theorem and Applications to ODEs |
| 10 | Oct 8 | Lecture 10 | Bounded Linear Operators |
| 11 | Oct 10 | Lecture 11 | Bounded Linear Operators (cont'd); Dual Spaces; B(X,Y) |
|  | Oct 14-18 |  | Thanksgiving + Reading Week |
| 12 | Oct 22 | Lecture 12 <br> Assignment 3 <br> A3 Solutions | Infinite Series; Neumann Series; Fréchet Derivative |
| 13 | Oct 24 | Midterm <br> Solutions | Contents: Lectures 01 to 11 + Past Assignments |
| 14 | Oct 29 | Lecture 13 | Fréchet Derivative; Hahn-Banach Theorems |
| 15 | Oct 31 | Lecture 14 | Applications of Hahn-Banach Theorems; Inner Product Spaces |
| 16 | Nov 5 | Lecture 15 \& 16 | Hilbert Spaces and Examples; Projection Theorem |

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| 17 | Nov 7 | Lecture 15 \& 16 <br> Questions <br> Assignment 4 <br> A4 Solutions | Riesz Representation Theorem; Adjoint Operators <br> Potential Questions for Final Exam |
| 18 | Nov 12 | Lecture 17 | Lax Milgram Theorem; Nonlinear Lax Milgram Theorem; Stampacchia Theorem |
| 19 | Nov 14 | Lecture 18 | Nonlinear Lax Milgram Theorem (cont'd); Generalized Fourier Series |
| 20 | Nov 19 | Lecture 19 | Orthonormal Basis; Spectral Theory |
| 21 | Nov 21 | No Class |  |
| 22 | Nov 26 | Lecture 20 <br> Sturm-Liouville Theorem <br> Questions <br> Assignment 5 | Spectral Theory (cont'd) <br> Sturm-Liouville Theorem <br> Updated Potential Questions for Final Exam |
| 23 | Nov 28 | Lecture 21 | Sobolev Spaces (cont'd) |
| 24 | Dec 3 | Lecture 22 | Sobolev Spaces (cont'd) |
|  |  | All Lectures | Combined All Lectures in One |

