# Real-Time Path Planning Based on Hybrid-VANET-Enhanced Transportation System 

Miao Wang, Hangguan Shan, Member, IEEE, Rongxing Lu, Member, IEEE, Ran Zhang, Xuemin (Sherman) Shen, Fellow, IEEE, and Fan Bai


#### Abstract

Real-time path planning can efficiently relieve traffic congestion in urban scenarios. However, how to design an efficient path-planning algorithm to achieve a globally optimal vehicletraffic control still remains a challenging problem, particularly when we take drivers' individual preferences into consideration. In this paper, we first establish a hybrid intelligent transportation system (ITS), i.e., a hybrid-VANET-enhanced ITS, which utilizes both vehicular ad hoc networks (VANETs) and cellular systems of the public transportation system to enable real-time communications among vehicles, roadside units (RSUs), and a vehicle-traffic server in an efficient way. Then, we propose a real-time path-planning algorithm, which not only improves the overall spatial utilization of a road network but reduces average vehicle travel cost for avoiding vehicles from getting stuck in congestion as well. A stochastic Lyapunov optimization technique is exploited to address the globally optimal path-planning problem. Finally, the transmission delay of the hybrid-VANET-enhanced ITS is evaluated in VISSIM to show the timeliness of the proposed communication framework. Moreover, system-level simulations conducted in Java demonstrate that the proposed path-planning algorithm outperforms the traditional distributed path planning in terms of balancing the spatial utilization and drivers' travel cost.


Index Terms-Hybrid VANETs, path planning, spatial utilization, travel cost.

## I. Introduction

TRAFFIC congestion, as an important societal problem, has received considerable attention. The 2007 Urban Mobility Report [1] stated that traffic congestion causes nearly 4.2 billion hours of extra travel every year in U.S.; the extra travel almost accounts for 2.9 billion extra gallons of gasoline. Although many existing advanced personal navigation devices have functionalities of providing an optimal end-to-end path [2], [3],

[^0]traffic congestion problems in intelligent transportation systems (ITSs) have not been fully resolved; on the contrary, conventional approaches still face a number of technical challenges. For example, Google Maps involve existing networks (e.g., Global Position System, Wi-Fi, cellular networks, etc.) for individual path planning to avoid the traffic congestion. However, the provided services are very costly, and more importantly, they cannot make quick response to an emergency caused by an accident/incident. The essential reason for this imperfection lies in lack of real-time traffic information. Thus, to enhance the adaptability of path planning, it is indispensable to study how to efficiently collect and further exploit the real-time traffic information for path planning and traffic congestion avoidance.

First, to collect the real-time traffic information, the emerging vehicular ad hoc networks (VANETs) can provide an ITS system with enhanced communication capabilities for cost effective and real-time traffic information delivery [4]. Both vehicle-to-vehicle $\left(\mathrm{V} 2 \mathrm{~V}^{1}\right)$ and vehicle-to-roadside-unit (V2R) communications [6] are supported in VANETs to efficiently collect/report traffic updates from/to vehicles as well as roadside units (RSUs) [7]. As a result, the collected real-time traffic information can be utilized for freeway-traffic-flow management [8], individualized vehicle path planning [9], and vehicle localization [10]. However, most of the related works assume that the incorporated VANETs have sufficiently small delivery delay for real-time information collection. As VANETs rely on short-range multihop communications, the end-to-end transmission delay cannot be neglected in some scenarios. Therefore, evaluations should be conducted to study how the end-to-end transmission performance of vehicular communications affects the performance of path planning in different scenarios and how to design the transmission mechanisms to reduce the delay when delay cannot be neglected.

Second, to exploit the obtained real-time traffic information, many algorithms are designed to discover optimal paths for individual vehicles [11], [12]. However, individual path planning may lead to new congestion if performed uncoordinatedly. To smooth the overall network flow, many works plan optimal paths from a global perspective for a group of vehicles simultaneously [13], [14]. However, most existing globally optimal path-planning algorithms focus on the network-side performance improvement and neglect the drivers' preferences (e.g., shorter travel length or time). Since the replanning decisions

[^1]are made to avoid congestion and balance the traffic rather than discover optimal paths for individuals, some vehicles may pay additional cost (e.g., a longer traveling length). Therefore, algorithms should be designed to jointly consider the balance of the network traffic and the reduction of average vehicle travel cost.

To this end, we propose a real-time global path-planning algorithm that exploits VANET communication capabilities to avoid vehicles from congestion in an urban environment. Both the network spatial utilization and vehicle travel cost are considered to optimally balance the overall network smoothness and the drivers' preferences. Specifically, the contributions of this paper are threefold.

- First, to facilitate the application of real-time path planning, we propose a hybrid-VANET-enhanced ITS framework, exploiting both the VANETs and the public transportation system. Based on the proposed hybrid ITS framework, a multihop message forwarding mechanism is designed to collect the real-time traffic information or the emergent warning messages, which usually have strict delay bounds. A theoretical analysis on the end-toend transmission delay performance of the mechanism is presented as well.
- Second, we design a real-time global path-planning algorithm to not only improve network spatial utilization but also reduce average vehicle travel cost per trip. A lowcomplexity algorithm is developed based on Lyapunov optimization to make real-time path planning decisions. With the proposed path-planning algorithm, the tradeoff between the overall network spatial utilization and drivers' preferences can be well balanced.
- Finally, the transmission performance of the hybrid VANETs is first evaluated under different vehicle densities via VISSIM, and then, extensive simulations validate the effectiveness and efficiency of the proposed path-planning algorithm. The results confirm that our proposed pathplanning algorithm is able to find alternative paths for vehicles to bypass congestion areas while reducing the average travel cost in an efficient, timely, and coordinated way.
The remainder of this paper is organized as follows. Section II provides related works on path planning. The system model is discussed in Section III. Section IV presents the transmission mechanism in the proposed architecture and the corresponding performance analysis. A real-time path planning problem is formulated in Section V, followed by algorithm design in Section VI. Section VII demonstrates the performance of our proposed path-planning algorithm by simulations. Finally, Section VIII concludes this paper.


## II. Related Works

Traffic congestion, caused by unbalanced traffic flow or a sudden accident/incident, can cause late arrivals and additional cost for drivers and becomes a major problem in the transportation. However, this cost due to traffic congestion can be reduced by route navigation or path planning with congestion avoidance. For example, the paths of vehicles can be replanned with the shortest-path-based GPS navigation [15], the accident
duration prediction [16], and the route reservation in advance [17]. However, these approaches cannot make quick response to an emergency or congestion due to a sudden accident since a timely update on the traffic condition is lacking. Thus, the realtime traffic information becomes indispensable to support the vehicular real-time path-planning algorithm.

To collect time-varying traffic-condition information, most existing works in conventional ITS usually rely on cellular systems or loop detectors. In [18]-[21], cellphones or mobile sensors with cellular access have been investigated to collect real-time traffic information for traffic forecast or reconstruction in experimental research. In [8], a traffic management system with loop detectors for continuous traffic measurement and monitoring along arterials is introduced. However, inevitable drawbacks cast a shadow on the application of cellular systems and loop detectors. For cellular systems, as they are not dedicated for traffic data collection, the collection services can be highly costly, and the high volume of traffic data may also cause congestion for other cellular services. For the loop detectors, the deployment expense can also be very high. Moreover, the inaccuracy of position measurement becomes a problem for short-distance transmissions particularly in dense networks, which will degrade the performance of path planning [22], [23].

Due to VANETs, V2V and V2R communications can make real-time message delivery much quicker, cheaper, and more efficient than the existing systems, even for short-distance transmissions in dense networks [24], [25]. More importantly, RSUs in VANETs can greatly enhance the timeliness of data collection and dissemination [26], which makes it possible to perform coordinated path planning for a group of vehicles. To improve the quality of experience (QoE), a point-to-point-based vehicular network can be utilized to support the application of multimedia delivery [27], [28], which however may still experience large transmission delay. Hence, in this paper, to reduce the end-to-end transmission delay, taxis or buses are considered as super relays to help in delivering the information through the cellular network of public transportation system. On the other hand, in [27] and [28], media service applications, introducing heavy load to the involved cellular networks, are studied; however, in this paper, the delivered information composes limited small-size packets, leading to a different transmission scenario with smaller data traffic load.

Many works have studied real-time vehicle path planning with the assist of VANETs. A distributed path planning method to avoid congestion is put forward in [11] using real-time traffic data collected from VANETs, with the increased traffic flow. Aiming to save gasoline for individual vehicle, a navigation system is designed in [12] to avoid congestion. However, the individual-user-optimal schemes may introduce additional traffic congestion due to human uncoordinated selfish behaviors. Thus, the paths of different vehicles should be jointly planned to balance the network traffic. The works in [13] and [14] consider multivehicle path planning, but the average travel cost or the drivers' preference is not considered. Moreover, how communications in VANETs can impact on the path-planning algorithm is still not clear.

Therefore, in this paper, a globally optimal path-planning algorithm is proposed for vehicles to avoid traffic congestion

TABLE I
Summary of the Important Mathematical Notations

| Symbol | Description |
| :---: | :---: |
| V | The set of vehicles in the network |
| II | The set of all intersections |
| $\Gamma$ | The set of all the roads in the network |
| $\mathbb{R}$ | The set of RSUs in the network |
| $\lambda_{i j}(t)$ | The inflow rate of road segment $(i, j)$ in time slot $t$ |
| $\mu_{i j}(t)$ | The outflow rate of road segment (i,j) in time slot $t$ |
| $c_{i j}(t)$ | The maximum number of outflow vehicles of road segment $(i, j)$ in time slot $t$ |
| $\delta\left(I_{i j}\right)$ | A congestion indicator of a warning message of congestion $I$ on road segment $(i, j)$ |
| $Q_{i}^{d}(T)$ | A virtual queue of intersection $i$ to represent the buffered vehicles destined to destination $d$ |
| $w_{m}$ | The capability of flexible turning for the vehicle $m$ |
| $T_{L}$ | A global message lifetime |
| $T_{\text {on }}$ | "on" period of a vehicle |
| $T_{\text {off }}$ | "off" period of a vehicle |
| $U_{\text {on }}$ | The travel distances within an "on" period |
| $U_{\text {off }}$ | The travel distances within an "off" period |
| $R$ | The transmission range of a vehicle or an RSU |
| M | The average number of hops of an end-to-end transmission in pure VANETs |
| $M^{\prime}$ | The average number of hops of an end-to-end transmission in hybrid VANET-enhanced networks |
| $\psi$ | The average transmission delay of a multi-hop transmission path in pure VANETs |
| $\psi^{\prime}$ | The average transmission delay of a multi-hop transmission path in hybrid ITS |
| $L_{r_{i j}}^{m_{d}}$ | The changed path for vehicle $m$ at intersection $i$, routing from intersection $i$ to $j$ |
| $L_{S_{i}}^{m_{d}}$ | The original path for vehicle $m$ at intersection $i$ |
| $p_{r_{i j}}^{m_{d}}$ | The cost of vehicle $m$ for a turning decision $r_{i j}$ towards destination $d$ |
| $p_{i J_{i}}(T)$ | The average cost factor for vehicles at intersection $i$ |

(including those caused by accidents) in a suburban scenario. With the real-time traffic information collection and decision delivery enabled by a hybrid-VANET-enhanced network, the road network resources are fully utilized, and the average travel cost of vehicles is significantly reduced. In addition, the impacts of VANETs on the path-planning algorithm are further discussed.

## III. System Model

Aiming at providing real-time planned paths for vehicles from a global perspective, we first introduce the following network architecture. The traffic flow model is then elaborated upon, followed by the vehicle categorization and mobility model. A summary of the important mathematical notations used in this paper is given in Table I.

## A. Hybrid-VANET-Enhanced Transportation System

Fig. 1 shows the architecture of the considered hybrid-VANET-enhanced transportation system, consisting of vehicles, RSUs, cellular base stations (BSs), and a vehicle-traffic server.
Vehicles are equipped with the onboard units that enable multihop V2V communication used in delivering the periodic vehicle information (e.g., vehicle velocity, density, and location). When vehicles sense accident-related congestion, the warning message can be generated to alert the emergent accident information and then be shared not only among ve-
hicles but with the nearest RSU via V2R communications as well. Moreover, pure VANETs, cellular communications, e.g., a GSM system which is set up for the functions such as mobile telemonitoring and management systems for intercity public transportation [29], are also involved. Hence, the taxis or buses can directly upload the received warning message to the nearest cellular BS, and the BS will deliver the message to the vehicletraffic server.

RSUs deployed along the roads are assumed able to obtain vehicle-traffic statistical information (e.g., the vehicle arrival/ departure rate on each road). We consider that taxis and buses are perfectly connected to the cellular system, and RSUs are well connected with each other through wireline. If RSUs are deployed at intersections, the traffic information can be detected by the equipped cameras or traffic flowmeters connected to RSUs directly [30]. Otherwise, the traffic flow can be predicted by the nearest RSUs based on the obtained vehicle information (e.g., periodically obtained vehicle density and velocity) from the VANETs [31]. An RSU can share its own collected information with other RSUs and the vehicle-traffic server. When an accident happens, based on all the collected information, the vehicle-traffic server is capable of performing real-time path planning to provide globally optimized travel paths for vehicles of interest.
We further define a road network into four main components (i.e., intersections, roads, vehicles, and RSUs) as $\varsigma=$ $(\mathbb{I}, \Gamma, \mathbb{V}, \mathbb{R})$. The set of all intersections is denoted as $\mathbb{I}$. Let $\Gamma$ be the set of all the roads in the network. Each road between two adjacent intersections is assumed bidirectional, possibly with multiple lanes in one direction. We refer to each of those lanes with the same direction in a road as a road segment, i.e., one normal bidirectional road between two adjacent intersections $i$ and $j$ has two different road segments with opposite directions, i.e., road segment $(i, j)$ and road segment $(j, i)$. The set of vehicles and that of RSUs are defined as $\mathbb{V}$ and $\mathbb{R}$, respectively.

## B. Traffic Flow Model

To understand a vehicle-traffic flow more clearly, we model vehicle traffic as an "inflow/outflow" system [32]. Each vehicle is expected to follow a planned path from its starting point toward its destination. Here, the planned path can be referred to as a path preset in a GPS, according to the driver's preferences and based on the locations of the starting and ending points. The driver will keep following the preset path until the vehicle receives any information on congestion or accident. When an accident or congestion occurs, by running the path-planning algorithm, the vehicle-traffic server will be in charge of finding an optimal alternative path or routing for the vehicles of interest. Specifically, in this paper, we refer to the road segments in which one vehicle's starting point and destination are located as $s(\in \Gamma)$ and $d(\in \Gamma)$, respectively.
Let $J_{i}$ denote the set of neighboring crossings of intersection $i$. Define the inflow rate of road segment $(i, j), \lambda_{i j}(t)$, as the upstream-vehicle arrival rate from neighboring road segments in time slot $t$, where $j \in J_{i}$, as shown in Fig. 2. Let $\lambda_{i j}^{d}(t)$ $\left(j \in J_{i}\right)$ denote the traffic flow rate on road segment $(i, j)$ with the same destination $d$ in time slot $t$, and $\lambda_{i j}(t)=\sum_{d \in \Gamma} \lambda_{i j}^{d}(t)$.


Fig. 1. Real-time path planning in VANET-enhanced hybrid networks. (a) Hybrid-VANET-enhanced network architecture. (b) Path planning in a VANETenhanced ITS.


Fig. 2. Traffic flow model.
In this paper, we consider each sample time duration (denoted as $\Delta$ and including a series of time slots) as a time unit, which is defined by sampling theorem to avoid information loss in the compressive sensing for traffic estimation in [33]. Within the $T$ th sample time duration, based on the traffic flow rates of the involved time slots collected by RSUs, the average inflow rate of road segment $(i, j)$ of the $T$ th sample time duration is denoted as $\lambda_{i j}(T)$ and expressed as

$$
\begin{equation*}
\lambda_{i j}(T)=\frac{1}{\Delta} \sum_{t=(T-1) \Delta}^{T \Delta} \lambda_{i j}(t) \tag{1}
\end{equation*}
$$

Similarly, the outflow rate $\mu_{i j}(T)$ of road segment $(i, j)$ is the average departure rate of vehicles moving to neighboring road segments in the $T$ th sample time. Note that all variables for the opposite directed road segment of $(i, j)$, namely road segment $(j, i)$, can be defined correspondingly, e.g., $\lambda_{j i}(T)$ and $\mu_{j i}(T)$.

Let $c_{i j}(T)$ denote the maximum number of outflow vehicles of road segment $(i, j)$ in $T$ th sample time, i.e., road capacity, which is determined by the road conditions, the number of lanes, the length of the road, and traffic congestion, etc. Due to fluctuating road conditions and traffic flow conditions, the road capacity can fluctuate with time but is considered to remain constant within one sample time unit.

There are two kinds of traffic congestion: recurrent congestion and nonrecurrent congestion [34]. The recurrent congestion is due to the tension between the current traffic flow situation (e.g., the traffic inflow $\lambda_{i j}(T)$ ) and the road conditions (e.g., the road capacity $c_{i j}(T)$ ), which is nonincident related. The nonrecurrent congestion is caused by an accident or incident, which can reduce the road capacity (to be introduced in Section V). We define a congestion indicator of a warning message, $\delta\left(I_{i j}\right)(\in$ $[0,1])$, to represent how the congestion type $I$ happening on road segment $(i, j)$ impacts on the road capacity, where $\delta\left(I_{i j}\right)=1$ means recurrent congestion and $\delta\left(I_{i j}\right) \in[0,1)$ implies nonrecurrent congestion.

Each vehicle traveling from one intersection to the next is called routing in this paper. For each intersection (e.g., intersection $i$ ), consider that the RSU nearest to the intersection maintains a virtual queue of length $Q_{i}^{d}(T)$, representing the number of the buffered vehicles at this intersection specifically destined to destination $d(\in \Gamma)$ in sample time $T$. Then, the total length of all virtual queues of intersection $i$ for all destinations is $Q_{i}(T)=\sum_{d \in \Gamma} Q_{i}^{d}(T)$, where

$$
\begin{array}{r}
Q_{i}^{d}(T)=\max \left\{Q_{i}^{d}(T-1)-\sum_{j \in J_{i}} \mu_{i j}^{d}(T-1), 0\right\} \\
 \tag{2}\\
+\sum_{u \in J_{i}} \lambda_{u i}^{d}(T-1)
\end{array}
$$

with $\mu_{i j}^{d}(T-1)$ being the outflow rate of road segment $(i, j)$ with destination $d$ in the $(T-1)$ th sample time, satisfying $\mu_{i j}(T-1)=\sum_{d \in \Gamma} \mu_{i j}^{d}(T-1)$. Similarly, for road segment $(i, j)$, we define the leftover number of vehicles in sample time $T$ as $Q_{i j}(T)=\max \left\{Q_{i j}(T-1)-\mu_{i j}(T-1), 0\right\}+\lambda_{i j}(T-1)$.

## C. Vehicle Categorization and Mobility Model

Three types of vehicles are considered in this paper, namely private cars, taxis, and buses. GPS devices are supposed to be deployed on all vehicles, and GPS devices have ordered the
service of providing shortest paths. Compared with changeable paths of taxis or private cars, scheduled paths of buses are usually fixed. Let $w_{m} \in\{0,1\}(m \in \mathbb{V})$ denote the capability of flexible turning for the vehicle $m$ when the vehicle receives any information about congestion or accident, and take the value 1 if vehicle $m$ is a taxi or a private car and 0 , otherwise, since taxis or private cars can change their paths whereas buses have to wait until the traffic trap is cleaned up.

Furthermore, we refer to taxis and buses as super nodes, connected to a control center through GSM systems. With a specially designed message transmission mechanism (to be introduced in Section IV), warning messages can be delivered to the vehicle-traffic server as efficiently as possible to facilitate real-time path planning.
The mobility of each vehicle can be characterized by two random variables $(V, D)$ [35]. Here, $V$ represents the vehicle velocity that takes two possible values (i.e., a lower velocity $v_{L}$ and a higher velocity $v_{H}$ ). The velocity transition is modeled as a two-state continuous-time Markov chain with state transition rate $1 / D$. Under this model, a vehicle initially chooses $v_{L}$ (or $v_{H}$ ), and after an exponentially distributed time interval with the mean of $D$, the velocity changes to $v_{H}$ (or $v_{L}$ ). The model can be exploited to describe the realistic driving behaviors, i.e., a driver usually drives at a constant velocity for a period and then changes to a higher/lower velocity based on his/her will and/or road conditions. Moreover, when the vehicle density is low or medium (e.g., no larger than 30 vehicle/km/lane), vehicles can be considered to move independently [36] and the headway distance ${ }^{2}$ follows the exponential distribution with rate $\zeta$ [37].

## IV. Transmission Mechanism and Performance Analysis

Since the incident-related warning message is pivotal to the viability of a real-time path-planning algorithm, we propose the following rapid message transmission mechanism and give corresponding analytical results on the end-to-end transmission performance.

## A. Outline of Transmission Mechanism

After sensing the congestion, vehicles in the vicinity of the congestion will generate and forward the warning message to other vehicles via multihop V 2 V relaying. If a supernode receives a warning message, it will upload the message to the nearest cellular BS through cellular communication of the public transportation system; otherwise, the message will be transmitted all the way to one RSU via V2V and V2R transmissions. To reduce the redundancy of multihop relaying, the following relay node selection is adopted. If there is one bus/taxi within the transmission range of a vehicle, the bus/taxi will be the next-hop receiver; otherwise, the farthest vehicle ahead in the same lane within the transmission range will be

[^2]selected as the next relay [35]. Moreover, we assume that a vehicle deletes the warning message once it has been transmitted. On the other hand, a global message lifetime $T_{L}$ is preset for each warning message, at the end of which all the transmissions of the corresponding message will be terminated, thus to further control the redundancy in message delivery. Once an RSU or cellular BS receives a warning message, it forwards the message to the vehicle-traffic server via wireline. Upon receiving the warning message, the traffic server will operate the path-planning algorithm based on the collected timely roadtraffic information. By leveraging this transmission mechanism, emergent messages (e.g., congestion indicators) are promising to be disseminated more efficiently as compared with only utilizing VANETs or the cellular communication capabilities of the public transportation system. Finally, after the vehicletraffic server finished path planning, replanned paths are fed back to vehicles, demanding path planning via a downlink transmission (i.e., traffic server-RSU/vehicle relay-vehicle in need of path planning).

As shown in Fig. 1, the overall communications in the proposed VANET-enhanced ITS can be divided into three layers: V2V and V2R communications in VANETs, wireless communication between super nodes, and BSs via a cellular system, and wired communication between RSUs (or BSs) and the vehicle-traffic server. Thus, the main issues affecting the efficiency of the end-to-end message transmission comes to transmission delay in VANETs. By considering the following ideal medium access control (MAC) for V2V and V2R communications, we will analyze the transmission delay in VANETs in the following. Specifically, for analytical simplicity, we assume that once a vehicle moves into the coverage range of an RSU or another vehicle, time slots can be scheduled with neglectable delay for the corresponding V2R or V2V transmissions. Moreover, the link rate of a V2V or V2R transmission is assumed constant, and the contact duration between each transmission pair is considered long enough to accomplish at least one packet delivery, which can be achieved by appropriately setting the packet size [38].

In general, the transmission delay in VANETs can be discussed under two cases. First, when the vehicle density is very high (e.g., more than 56 vehicles $/ \mathrm{mi}$ ), the connections among vehicles can be found with high probability, considering that the transmission range of a vehicle (e.g., more than 100 m as shown in dedicated short-range communications) is way more than the average headway distance. In this case, for a given connection path, for example, from a vehicle to an RSU, we consider neglectable transmission delay because of the assumption of the ideal MAC and small-size packet delivery. Second, for the medium or sparse vehicle density case, due to the intermittency of vehicle communications caused by high-speed mobility and/or node sparsity, the intercontact time, namely, the waiting time of each hop for the receiver (vehicle or RSU) to fall into the transmission range of the transmitter, dominates the end-toend transmission delay. Notice that congestion may cause an unbalanced vehicle distribution on neighboring roads, and the traffic information report on a road of low node density can be the bottleneck of the VANET-assisted information collection. As such, in the following, we analyze the impact of vehicle
density on the intercontact time of one-hop V2V or V2R transmission and further on the end-to-end transmission delay along the transmission path.

## B. End-to-End Delay Analysis

In the following, we analyze the intercontact time for the aforementioned transmission mechanism. The end-to-end delay analysis begins from the transmissions in pure VANETs, and then involves the public transportation system.

1) End-to-End Delay in Pure VANETs: First, consider an uplink with no taxis or buses, i.e., all the hops are based on V2V and V2R communications. We evaluate the transmission delay for the last hop of the V2R transmission. The transmission delay here is mainly due to the intercontact time between a vehicle and an RSU. Similar to [35], we define the last hop as an ON-OFF model, where a vehicle either directly connects to an RSU (i.e., during the ON-state) or is the only vehicle approaching the RSU and there is no other vehicle in the transmission range of the RSU (i.e., during the OFF-state). According to the transmission model, the transmission delay of a packet during the ON -state should be way smaller than that during the OFF-state. Therefore, the transmission delay of the last V2R hop is mainly due to the OFF-state period.

Denote the ON-state period and the OFF-state period of a vehicle as $T_{\text {on }}$ and $T_{\text {off }}$, respectively. Accordingly, the travel distances within the two periods are defined as $U_{\text {on }}$ and $U_{\text {off }}$, respectively, with $T_{\text {on }}=U_{\text {on }} / \bar{V}$ and $T_{\text {off }}=U_{\text {off }} / \overline{\bar{V}}$, where $\bar{V}$ is the average velocity for a vehicle based on the ON-OFF mobility model (see Section III-C). Similar to [35], the event that a vehicle moves a distance of at least $u$ during $T_{\text {on }}$ before being scheduled to communicate with an RSU should satisfy the following: 1) There is no other vehicle within the distance $u$ from the end of the RSU coverage ahead of the vehicle; and 2) there is at least one vehicle within the distance $2 R-u$, which results in this vehicle moving at least $u$ distance to avoid the collision, with $R$ representing the transmission range of an RSU or a vehicle. Then, we have

$$
\begin{equation*}
P_{r}\left(U_{\mathrm{on}}>u\right)=\frac{\left(e^{-\zeta \cdot u}\right)^{b \gamma-1}\left[1-\left(e^{-\zeta \cdot(2 R-u)}\right)^{b \gamma-1}\right]}{1-\left(e^{-\zeta \cdot 2 R}\right)^{b \gamma}} \tag{3}
\end{equation*}
$$

where $b$ is the summation of all road lengths, and $\gamma$ is the average vehicle density on the roads. Since the vehicle headway distance follows an exponential distribution, as mentioned in Section III-C, the probability that a headway distance is larger than $u$ is $e^{-\zeta \cdot u}$. Based on (3), we can obtain

$$
\begin{equation*}
E\left[U_{\mathrm{on}}\right]=\int_{0}^{2 R} P_{r}\left(U_{\mathrm{on}}>u\right) d u \tag{4}
\end{equation*}
$$

Similarly, the event that a vehicle moves a distance of at least $u$ during $T_{\text {off }}$ should satisfy the following: 1) There is no vehicle within a distance of $2 R+u$ from the end of the coverage range of the nearest RSU ahead of the vehicle; and 2) there is at least
one vehicle within the distance $L-(u+2 R)$, where $L$ is the distance between the adjacent RSUs. Then, we have

$$
\begin{align*}
P_{r}\left(U_{\text {off }}>u\right) & =\frac{\left(e^{-\zeta \cdot(2 R+u)}\right)^{b \gamma-1}\left[1-\left(e^{-\zeta \cdot(L-(2 R+u))}\right)^{b \gamma-1}\right]}{\left(e^{-\zeta \cdot 2 R}\right)^{b \gamma}\left[1-\left(e^{-\zeta \cdot(L-2 R)}\right)^{b \gamma}\right]}  \tag{5}\\
E\left[U_{\text {off }}\right] & =\int_{0}^{L-2 R} P_{r}\left(U_{\text {off }}>u\right) d u . \tag{6}
\end{align*}
$$

In addition, the previous hops between vehicles within a transmission path, except the last hop, can be characterized with the vehicle mobility model. The process of the relative velocity between two vehicles can be represented by a CTMC with a state space $\mathbb{H}=\left\{h_{0}, h_{1}, h_{2}\right\}$. Here, $h_{0}$ represents a negative relative velocity when the vehicle in front moves with $v_{L}$, whereas the vehicle behind moves with $v_{H} ; h_{1}$ models a zero relative velocity (i.e., both vehicles move with the same velocity); $h_{2}$ represents a positive relative velocity. If each vehicle keeps the same velocity for an exponential time with an average of $D$, the transition rate between any two states of the Markov process is equal to $2 / D$. Thus, from [35], the average number of hops $M$ of an end-to-end transmission path from a message source to an RSU in pure VANETs can be approximated as

$$
\begin{equation*}
M=\frac{6\left(L-E\left[U_{\mathrm{on}}\right]-E\left[U_{\mathrm{off}}\right]\right)}{D\left(v_{L}+v_{H}\right)} \tag{7}
\end{equation*}
$$

Then, based on the average number of hops, the transmission delay of such a transmission path can be shown as

$$
\begin{equation*}
\psi=(M-1) E\left[T_{V 2 V}\right]+E\left[T_{\mathrm{off}}\right] \tag{8}
\end{equation*}
$$

where $E\left[T_{V 2 V}\right]=1 /\left(1-e^{-\zeta R}\right)$ is the average transmission delay for a V2V hop since the headway distance follows an exponential distribution. $E\left[T_{\text {off }}\right]$ is the average duration of the OFF-state period, as defined earlier. If we consider the downloading as a similar process with uploading, the total transmission delay can be approximated by $2 \psi^{3}$ Note that this transmission delay is related to the parameters, including vehicle mobility parameters ( $V$ and $D$ ), vehicle density $(\gamma)$, and RSU-related parameters (the transmission range $R$ and the average distance between RSUs $L$ ). Then, the probability of an $M$-hop transmission path with all V2V and V2R communications equals the probability that there is neither taxi nor bus in any hop within the $M$-hop transmission path, i.e., $\left(1-P_{T}-\right.$ $\left.P_{B}\right)^{M}$, where $P_{T}\left(P_{B}\right)$ is the percentage of taxis (buses) in the traffic stream.
2) End-to-End Delay in Hybrid-VANET-Enhanced Network: If the public transportation system is involved in delivering messages as aforementioned, the probability of a given number of hops from a private car to the nearest bus/taxi follows a

[^3]geometric distribution. The average number of hops in the hybrid-VANET-enhanced ITS, i.e., $M^{\prime}$, is
\[

$$
\begin{align*}
M^{\prime}=M & \left(1-P_{B}-P_{T}\right)^{M} \\
& +\sum_{i=1}^{M}(i-1) \cdot\left(1-P_{B}-P_{T}\right)^{i-1} \cdot\left(P_{B}+P_{T}\right) . \tag{9}
\end{align*}
$$
\]

Then, if we consider that the public transportation system are perfectly connected with no delay, the average transmission delay is dominated by the transmission delay in VANETs. Based on the probability of a given number of hops from a private car to the nearest bus/taxi, the transmission delay in a multihop message transmission path is rewritten as

$$
\begin{align*}
& \psi^{\prime}=\psi \cdot\left(1-P_{B}-P_{T}\right)^{M}+ \sum_{i=1}^{M}(i-1) \cdot\left(1-P_{B}-P_{T}\right)^{i-1} \\
& \cdot\left(P_{B}+P_{T}\right) \cdot E\left[T_{V 2 V}\right] \cdot \tag{10}
\end{align*}
$$

From (10), the end-to-end transmission delay in hybrid ITS is related to 1) vehicle mobility parameters (i.e., $V$ and $D$ ), 2) vehicle density and super-node percentage (i.e., $\gamma, P_{B}$, and $P_{T}$ ), and 3) RSU deployment in the network (e.g., the transmission range $R$ and the average distance between RSUs $L$ ).

## V. Problem Formulation

Here, based on the traffic flow model defined in Section III-B, the traffic flow balance constraint of each intersection is first identified. The road capacity and congestion indicator are then discussed under different traffic conditions. Subsequently, considering the drivers' travel-cost preferences in the path planning, the cost metric of path planning for individual vehicle is defined. In addition, the network stability constraint is shown. Finally, the real-time path planning problem is formulated to not only avoid the congestion but reduce the average travel cost caused by path planning as well.

## A. Intersection Flow Balance Constraint

For an intersection $i(\in \mathbb{I})$, the following flow balance equation should be satisfied to guarantee that the aggregate vehicle arrival rate is equal to the aggregate vehicle departure rate:

$$
\begin{equation*}
\sum_{j \in J_{i}} \mu_{j i}(T)=\sum_{u \in J_{i}} \lambda_{i u}(T) \quad \forall i \in \mathbb{I} \tag{11}
\end{equation*}
$$

where the left and right sides of the equation are, respectively, referred to as the aggregate vehicle arrival and departure rates.

## B. Road Capacity and Congestion Indicator

For road segment $(i, j)$, the vehicle inflow rate for sample time $T$ is $\lambda_{i j}(T)$. The average outflow rate changes with the inflow rate, but with some time delay (denoted as $\Lambda$ seconds, which is the travel time for a vehicle moving from intersection $i$ to intersection $j$, i.e., $\mu_{i j}(T)=\lambda_{i j}(T-\Lambda)$, until reaching the outflow rate limit, i.e., road capacity $c_{i j}(T)$. Here, $\Lambda$ is decided by the tension between the traffic inflow and road capacity. Once an incident/accident occurs, the outflow rate drops dramatically on one road segment. To illustrate the road
capacity under different traffic conditions, we discuss the road capacity in two cases: 1) no incident-related congestion (i.e., recurrent congestion) and 2) the incident-related congestion (i.e., nonrecurrent congestion). The road capacities under two cases will be illustrated respectively as follows.

1) When there is no incident-related congestion on $(i, j)$, according to [34], we have

$$
\begin{equation*}
c_{i j}(T)=c_{i j}^{N}=N_{i j} \cdot c_{i j}^{p} \cdot F_{\mathrm{PH}} \cdot \frac{1}{\left(1+E_{B} \cdot P_{B}\right) \cdot A} \tag{12}
\end{equation*}
$$

where $c_{i j}^{N}$ is the road capacity under no incident-related congestion case. $N_{i j}$ is denoted as the number of lanes in road segment $(i, j)$. The ideal capacity per lane is $c_{i j}^{p}$. $F_{\mathrm{PH}}$ is the peak-hour factor, i.e., the ratio of the peak $15-\mathrm{min}$ flow rate in vehicles per hour ( vph ) to the average hourly flow rate (vph). $E_{B}$ is the bus equivalent ${ }^{4}$ to private cars or taxis. $P_{B}$ is the percentage of buses in the traffic stream. $A$ is an adjustment factor to account for other factors with impact on road capacity. Under this case

$$
\begin{equation*}
\mu_{i j}(T)=\min \left\{\lambda_{i j}\left(T-\Lambda^{r}\right), c_{i j}(T)\right\} \tag{13}
\end{equation*}
$$

with $\Lambda^{r}$ called recurrent delay [34] and satisfying

$$
\begin{align*}
\Lambda^{r}=T_{i j}^{0} & +D_{i j}^{q}+0.25 T\left[\left(\frac{\lambda_{i j}(T)}{c_{i j}(T)}-1\right)\right. \\
& +\sqrt{\left.\left(\frac{\lambda_{i j}(T)}{c_{i j}(T)}-1\right)^{2}+\frac{16 J_{i j} \cdot L_{i j}^{2} \cdot \lambda_{i j}(T)}{N_{i j}^{2} \cdot T^{2} \cdot c_{i j}(T)}\right]} \tag{14}
\end{align*}
$$

Here, $T_{i j}^{0}=L_{i j} / V_{0}$ is the segment travel time measured at free flow speed $V_{0}$, with $L_{i j}$ being the length of road segment $(i, j)$. $J_{i j}=\left(T_{i j}^{c}-T_{i j}^{0}\right)^{2} / L_{i j}^{2}$ is a calibration parameter, with $T_{i j}^{c}$ being the segment travel time measured when the traffic demand equals road capacity. $D_{i j}^{q}$ is the delay due to leftover queue from the prior sample time, i.e.,
$D_{i j}^{q}=\frac{Q_{i j}(T)}{2 \cdot c_{i j}(T) \cdot T} \cdot \min \left\{T, \frac{Q_{i j}(T)}{c_{i j}(T) \cdot\left[1-\min \left(1, \frac{\lambda_{i j}(T)}{c_{i j}(T)}\right)\right]}\right\}$.
2) When there is an incident $I_{i j}$ on road segment $(i, j)$, we still hold

$$
\begin{equation*}
\mu_{i j}(T)=\min \left\{\lambda_{i j}\left(T-\Lambda^{\mathrm{nr}}\right), c_{i j}(T)\right\} \tag{15}
\end{equation*}
$$

where $\Lambda^{\mathrm{nr}}$ is called nonrecurrent delay and can also be calculated based on (14). However, in this case

$$
\begin{equation*}
c_{i j}(T)=c_{i j}^{I}=c_{i j}^{N} \cdot \delta\left(I_{i j}\right) \quad \forall \delta\left(I_{i j}\right) \in[0,1) \tag{16}
\end{equation*}
$$

where $\delta\left(I_{i j}\right)$ is the percentage of remaining road capacity during incident type $I$ on road segment $(i, j)$, i.e., congestion indicator. The value of $\delta\left(I_{i j}\right)$ depends on the incident type $I$ and is considered to be sensed by witness/victim vehicles and delivered to the nearest RSU or BS. $c_{i j}^{I}$ is thus the road capacity under the incident $I$. Take the case that a road segment has one lane in each

[^4]direction as an example. When an accident $I$ happens, we may consider that $\delta\left(I_{i j}\right)=0$ and $\mu_{i j}(T)=c_{i j}^{I}=0$ since no vehicle-traffic flow will pass. On the other hand, in the case that a road segment has multiple lanes in each direction, the traffic flow will not be zero but might still drop dramatically.
Furthermore, if there is no incident-related congestion on $\operatorname{road}(i, j), \delta\left(I_{i j}\right)=1$. Then, we can extend the following relationship between the indicator and road capacity:
\[

$$
\begin{equation*}
c_{i j}(T)=c_{i j}^{N} \cdot \delta\left(I_{i j}\right) \quad \forall \delta\left(I_{i j}\right) \in[0,1] \tag{17}
\end{equation*}
$$

\]

which implies that the road capacity drops once an accident happens on a certain segment until the accident is cleaned up. The outflow rate should be always no more than that according to the road capacity, i.e.,

$$
\begin{equation*}
\mu_{i j}(T) \leq c_{i j}(T) \tag{18}
\end{equation*}
$$

## C. Path-Planning Cost Metric

The path-planning algorithm is to avoid the congestion on the road, with considering the preference of drivers, e.g., the shortest path or the most familiar path. Here, we consider the path length as the driver's first-order preference. Let $L_{r_{i j}}^{m_{d}}$ denote the changed path for vehicle $m$ (with destination $d$ ) at intersection $i$, where $r_{i j}$ means that, according to the newly planned path, vehicle $m$ changes its path by going through road segment $(i, j)$ toward destination $d$, satisfying $j \in J_{i}$. Compared with current path length $L_{S_{i}}^{m_{d}}$, the increased path length is $\left|L_{r_{i j}}^{m_{d}}\right|-\left|L_{S_{i}}^{m_{d}}\right|$, where $S_{i}$ is the path choice before being replanned. Obviously, it is possible that the changed path leads to more travel time and more consumed fuel energy. Let $p_{r_{i j}}^{m_{d}}$ denote the cost of vehicle $m$ for a certain turning decision $r_{i j}$ toward destination $d$, given $S_{i} \neq r_{i j}$. If intersection $i$ is not in the current path of $m_{d}, p_{r_{i j}}^{m_{d}}$ is zero; otherwise, it is modeled with respect to the increased path length as follows:

$$
\begin{equation*}
p_{r_{i j}}^{m_{d}}=\rho\left(\left|L_{r_{i j}}^{m_{d}}\right|-\left|L_{S_{i}}^{m_{d}}\right|\right) \tag{19}
\end{equation*}
$$

where $\rho(\cdot)$ is a nonnegative increasing function to measure the impacts of the increase in path length, i.e., $\left(\left|L_{r_{i j}}^{m_{d}}\right|-\left|L_{S_{i}}^{m_{d}}\right|\right)$ [40]. Then, the average cost of vehicles taking turning $r_{i j}$ on road segment $(i, j)$ can be calculated as

$$
p_{i j}(T)= \begin{cases}\frac{1}{\sum_{m \in \mathbb{V}} w_{m}} \sum_{m \in \mathbb{V}, d \in D} w_{m} \cdot p_{r_{i j}}^{m_{d}}, & \text { if } \sum_{m \in \mathbb{V}} w_{m} \neq 0  \tag{20}\\ \infty, & \text { otherwise. }\end{cases}
$$

For an intersection (e.g., intersection $i$ ), since there may be several neighboring intersections as the candidates of the coming intersections, the average cost of vehicles belonging to intersection $i$ is defined as
$p_{i J_{i}}(T)=\left\{\begin{array}{lc}\frac{1}{\sum_{j \in J_{i}} \alpha_{i j}(T)} \sum_{j \in J_{i}} \alpha_{i j}(T) p_{i j}(T), & \text { if } \sum_{j \in J_{i}} \alpha_{i j}(T) \neq 0 \\ 0, & \text { otherwise }\end{array}\right.$
where $\alpha_{i j}(T)$ is set as 1 in the first case of (20) (i.e., when $\sum_{m \in \mathbb{V}} w_{m} \neq 0$ ); otherwise, it is 0 .

## D. Network Stability

The definition of Queue and Network Stability [41] is used to represent traffic congestion avoidance in our path-planning optimization problem. ${ }^{5}$ For intersection $i, Q_{i}(T)$ is strongly stable if and only if

$$
\begin{equation*}
\lim _{T_{0} \rightarrow \infty} \sup \frac{1}{T_{0}} \sum_{T=0}^{T_{0}} E\left[Q_{i}(T)\right]<\infty \tag{22}
\end{equation*}
$$

The information on $Q_{i}(T)$ is required to identify whether an intersection is stable or not. If the traffic inflow and outflow information is detected by the cameras or traffic flowmeters connected to RSUs; $Q_{i}(T)$ is expected to be calculated directly. If the traffic information is relayed in VANETs as there is no RSU at the intersection, the relayed information is utilized in the vehicle-traffic server to predict the traffic flow information with a certain transmission delay. According to (10), this uploading transmission delay can be estimated as $\psi^{\prime} / \Delta$, which here is mainly caused by the intermittent connections in VANETs. With this transmission delay, the proposed algorithm can utilize a more accurate virtual queue information for path planning in each sample time, i.e., $Q_{i}\left(T-\left\lceil\psi^{\prime} / \Delta\right\rceil\right)$. Note that, if and only if all queues in the network are strongly stable, vehicle traffic in the whole road network is strongly stable.

## E. Utilization-Minus-Cost Maximization Problem

Taking account of both the traffic flows of the network and the path-planning cost of vehicles, the objective of the path-planning algorithm is considered to maximize the overall spatial utilization minus planning cost at the same time with the network congestion avoidance. This objective indicates that the total traffic flow improvement and the path-planning cost reduction should be jointly considered and carefully balanced. Specifically, once the traffic server receives the traffic flow and accident warning messages collected from both RSUs and vehicles via VANETs (or cellular networks), a path-planning algorithm is calculated to update and determine $\lambda_{i j}(T)$ according to the optimization problem, i.e., the number of vehicles dispatched over road segment $(i, j)$ in the $T$ th sample time

$$
\begin{align*}
& \max \sum_{i \in \mathbb{I}} \sum_{j \in J_{i}} \lambda_{i j}(T)-\sum_{i \in \mathbb{I}} p_{i J_{i}}(T) \\
& \text { s.t. }(11),(18), \text { and }(22) . \tag{23}
\end{align*}
$$

This objective is to maximize the spatial utility while minimizing travel cost, under the following constraints: 1) the flow balance of each intersection; 2) the limitation of outflow rate on each road segment; and 3) the congestion avoidance of each intersection. We exploit Lyapunov optimization process [41] to

[^5]solve this problem (to be introduced in Section VI). Then, in the sample time $T$, based on the path-planning algorithm, a vehicle with destination $d$ can be dispatched from one intersection to another (e.g., from intersection $i$ to intersection $j$ with contribution $\lambda_{i j}(T)$ ), in order to improve the spatial utility and to reduce travel cost. This updated path will deliver to the GPS device to navigate the required vehicle. In other words, a turning decision, $r_{i j}$, for a taxi or a private car at intersection $i$, can be decided based on the corresponding $\lambda_{i j}(T)$ and $p_{i J_{i}}(T)$, and furthermore, the replanned path can be calculated based on this turning decision. Note that, if the traffic flow information is collected by VANETs (or cellular networks), the transmission delay in VANETs, i.e., $\psi^{\prime} / \Delta$, should be considered in the third constraint as discussed in Section V-D.

## VI. Real-Time Optimal Path Planning

Here, the path-planning algorithm is first proposed to help vehicles to bypass congestion and balance traffic evenly in the whole network. Then, the convergence and the computation complexity of the proposed algorithm are discussed.

## A. Path-Planning Algorithm Design

The optimization problem (23) can be solved by applying the drift-plus-penalty framework in the Lyapunov optimization process [41]. By following dynamic algorithm at each sample time, we derive vehicles' turning decisions for maximizing the lower bound of network throughput. According to the Lyapunov optimization process, let $W_{i J_{i}}(T)$ denote the weight of intersection $i$ in sample time $T$

$$
\begin{array}{r}
W_{i J_{i}}(T)=\sum_{j \in J_{i}} \alpha_{i j}(T) \min \left\{c_{i j}(T), \sum_{d \in D}\left\{Q_{i}^{d}(T)-Q_{j}^{d}(T)\right\}\right\} \\
-K p_{i J_{i}}(T) \tag{24}
\end{array}
$$

where $K$ is a nonnegative constant defined by vehicle traffic server used for all vehicles, with the same order of the reciprocal of travel cost (i.e., $p_{i J_{i}}(T)$ ) [41]. Equation (24) implies that the weight of an intersection (e.g., intersection $i$ ) is related to: 1) the differential queue backlog between intersection $i$ and its neighboring intersections and 2) average intersection travel cost. Vehicles at intersection with the largest weight are replanned first. Vehicles with destination $d$ stored at intersection $i$ should be dispatched to queue $Q_{j_{d}^{*}}^{d}(T)$ of intersection $j_{d}^{*}$, where $j_{d}^{*}=\arg \max _{j \in J_{i}}\left\{Q_{i}^{d}(T)-Q_{j}^{d}(T)\right\}$, according to the largest differential queue backlog. The number of the vehicles with destination $d$ replanned to intersection $j_{d}^{*}$ is $\min \left\{Q_{i}^{d}(T)-\right.$ $\left.Q_{j_{d}^{*}}^{d}(T), c_{i j_{d}^{*}}(T)\right\}$. Then, queues at all the remaining intersections are updated correspondingly. The same process continues until all intersections related are processed. The sketch of the proposed dynamic algorithm is summarized in Algorithm 1. The implication of path planning is to prioritize those vehicles in such an intersection with larger differential queue backlogs and shorter increased path lengths under new turning decisions (i.e., lower average travel cost).

```
procedure Path Planning (Algorithm 1)
    /* Initialization */
    A candidate set of intersections \(I_{c}=\emptyset\);
    for each intersection \(i \in \mathbb{I}\) do
        Calculate the weight \(W_{i J_{i}}(T)\) for each intersection;
        if \(W_{i J_{i}}(T) \neq 0\) then
            update the set \(I_{c} \leftarrow I_{c} \cup\{i\}\).
        end if
    end for
    \(/^{*}\) Path planning */
    while intersection \(I_{c} \neq \emptyset\) do
        Schedule intersection \(i=\arg \max _{u \in I_{c}}\left\{W_{u J_{u}}(T)\right\}\).
        /* Path planning */
        for each destination \(d\) do
            Find \(j_{d}^{*}=\arg \max _{j \in J_{i}}\left\{Q_{i}^{d}(T)-Q_{j}^{d}(T)\right\}\).
            \(q_{j_{d}^{*}}^{d}(T) \leftarrow \min \left\{Q_{i}^{d}(T)-Q_{j_{d}^{*}}^{d}(T), c_{i j_{d}^{*}}(T)\right\}\).
            \(/^{*}\) Update queues \(Q_{i}^{d}(T)\) and \(Q_{j_{d}^{*}}^{d}(T)^{* /}\)
            \(Q_{i}^{d}(T) \leftarrow Q_{i}^{d}(T)-q_{j_{d}^{*}}^{d}(T) ;\)
            \(Q_{j_{d}^{*}}^{d}(T) \leftarrow Q_{j_{d}^{*}}^{d}(T)+q_{j_{d}^{*}}^{d}(T) ;\)
        end for
        \(I_{c} \leftarrow I_{c} \backslash\{i\}\).
    end while
    end procedure
```


## B. Analysis of Algorithm Performance

For the network stability of the proposed path-planning algorithm, we have the following lemma.

Lemma 1: With the proposed path-planning algorithm, network stability can be guaranteed.

Proof: To prove network stability, according to [41], we need to show that the summation of the average square of queue sizes of those intersections' virtual queues does not increase with time. Consider the interflow exchange between any two intersections (e.g., $i$ and $j$ ). Let $Q_{i}(T)\left(Q_{i}(T+1)\right)$ and $Q_{j}(T)\left(Q_{j}(T+1)\right)$, respectively, denote the queue lengths of intersections $i$ and $j$ in sample time $T(T+1)$. In specific, based on our path-planning algorithm, between two neighboring intersections, vehicles are always dispatched from a long queue to a short queue. Assume that the change of the queue length of the two intersection is because $q_{j}^{d}(T)$ vehicles, where $d \in \Gamma$, are dispatched from intersection $i$ to intersection $j$, i.e., $Q_{i}^{d}(T+1)=Q_{i}^{d}(T)-q_{j}^{d}(T)$ and $Q_{j}^{d}(T+1)=$ $Q_{j}^{d}(T)+q_{j}^{d}(T)$. Then, the consequence of $q_{j}^{d}(T)$ dispatched vehicles is

$$
\begin{array}{r}
E\left\{\left(\left[Q_{i}(T+1)\right]^{2}+\left[Q_{j}(T+1)\right]^{2}\right)-\left(\left[Q_{i}(T)\right]^{2}+\left[Q_{j}(T)\right]^{2}\right)\right\} \\
\quad=2 E\left\{\left(\sum_{d} q_{j}^{d}(T)-Q_{i}(T)+Q_{j}(T)\right) \cdot \sum_{d} q_{j}^{d}(T)\right\} \tag{25}
\end{array}
$$

where $\sum_{d} q_{j}^{d}(T)$ is the total number of vehicles, which are dispatched from intersection $i$ to intersection $j$ at time $T$. As we
have $q_{j}^{d}(T)=\min \left\{Q_{i}^{d}(T)-Q_{j}^{d}(T), c_{i j}(T)\right\}, Q_{i}(T)=\sum_{d} Q_{i}^{d}(T)$, and $Q_{j}(T)=\sum_{d} Q_{j}^{d}(T)$, the following inequality holds:

$$
\begin{equation*}
\sum_{d} q_{j}^{d}(T)+Q_{j}(T)-Q_{i}(T) \leq 0 \tag{26}
\end{equation*}
$$

Thus, the right side of (25) is no more than zero. Then, the summation of average squares of queue size is satisfied as

$$
\begin{align*}
E\left\{\left[Q_{i}(T+1)\right]^{2}\right\} & +E\left\{\left[Q_{j}(T+1)\right]^{2}\right\} \\
& \leq E\left\{\left[Q_{i}(T)\right]^{2}\right\}+E\left\{\left[Q_{j}(T)\right]^{2}\right\} \tag{27}
\end{align*}
$$

That is, the summation of average square of queue size of those intersections' virtual queues does not increase with time. Under the cases with all destinations and multiple intersections, the similar results still hold, which implies the stability of network and the avoidance of traffic congestion in a network, as discussed in [41].
Furthermore, the computational complexity of the proposed algorithm is given as the following lemma.

Lemma 2: The total computational complexity is proportional to the square of the number of intersections in the map times the upper bound of the number of neighboring intersections.

Proof: We first calculate the weight of each intersection; thus, the complexity of this step is $O(|\mathbb{I}|)$. Second, we schedule each intersection in $I_{c}$. For each intersection to be scheduled, we need to find the right neighboring intersection $j_{d}^{*}$ for each destination $d$. Therefore, the complexity of the second step is $O\left(\left|I_{c}\right|\left(\left(1+\left|I_{c}\right|\right) / 2+|\Gamma| U\right)\right)$, where $U$ is the upper bound of the number of neighboring intersections of one intersection. As the $\left|I_{c}\right|$ and $|\mathbb{I}|$ are in the same order, the overall complexity is given by

$$
\begin{equation*}
O(|\mathbb{I}|)+O\left(\frac{|\mathbb{I}|+|\mathbb{I}|^{2}}{2}+|\mathbb{I}||\Gamma| U\right) \tag{28}
\end{equation*}
$$

Furthermore, as the number of roads $|\Gamma|$ and that of intersections $|\mathbb{I}|$ have the relationship $2 \Gamma / U \leq|\mathbb{I}|$, the complexity can be further simplified as

$$
\begin{equation*}
O(|\mathbb{I}|)+O\left(\frac{|\mathbb{I}|+|\mathbb{I}|^{2}}{2}+\frac{|\mathbb{I}|^{2} U^{2}}{2}\right)=O\left(|\mathbb{I}|^{2} U^{2}\right) \tag{29}
\end{equation*}
$$

Thus, the total computational complexity is proportional to the square of the number of intersections in the map times the upper bound of the number of neighboring intersections.

The proposed path-planning algorithm can perform better than the conventional path planning because of the following reasons. First, the proposed path-planning algorithm is updated based on real-time and accurate messages received from V2V/V2R communication, by which, for instance, a warning message of traffic jam can be delivered and impact timely on decisions of path planning. Second, in hybrid-VANET-enhanced networks, public transportation system can help to deliver the messages, leading to the reduced transmission delay for delaysensitive real-time path planning. Third, the proposed path planning is designed to reduce traveling cost in a coordinated manner to avoid particular parts of the road network overloaded. Finally, the relatively low computational complexity


Fig. 3. Simulation scenario of University of Waterloo region in VISSIM.
of the proposed algorithm makes the path-planning algorithm achieve better performance in a reasonable and realistic way.

## VII. Performance Evaluation

Here, we consider a realistic suburb scenario, as shown in Fig. 3, which is the region around the campus of University of Waterloo, Waterloo, ON, Canada. To emulate the timeliness of the proposed communication framework, a highly realistic microscopic vehicle traffic simulator, known as VISSIM [44], is employed to generate vehicle trace files for recording the vehicle mobility characteristics, based on which the effectiveness of the hybrid communication in supporting real-time path planning is studied. However, since the paths of vehicles cannot be changed or controlled by the external algorithm in VISSIM, we further develop a Java-based platform to investigate the performance of the proposed path-planning algorithm. Specifically, average moving delay (AMD), defined as the average travel time per trip, is used as a metric in the evaluation.

## A. Simulation Setup

1) Simulation Settings in VISSIM: To simulate a VANET with VISSIM in Kitchener-Waterloo (K-W) downtown region, vehicles are pushed into the region of $6000 \mathrm{~m} * 2800 \mathrm{~m}$, as shown in Fig. 3. At the beginning of the simulation, vehicles are set to enter the region from the preset entries (e.g., nine entries at the ends of main roads), following a Poisson process at a rate of 2500 vehicle/h/entry. The proportion of a bus or a taxi in the traffic flow is set as $5 \%$. After the duration of the first 240 s , the vehicle pushing in stops to reach an equivalent average density of 30 vehicle $/ \mathrm{km} / \mathrm{lane}$, which represents a medium-density scenario. Similarly, if the first duration is set to be 480 s , the scenario becomes a high-density one. In the VISSIM, vehicle information (e.g., location and velocity, etc.) is recorded every 0.2 s . The total simulation time lasts for 3600 s . In addition, the velocity distribution for all vehicles follows the velocity model described in Section III-C with parameters $v_{L}=30 \mathrm{~km} / \mathrm{h}$, $v_{H}=60 \mathrm{~km} / \mathrm{h}$, and $D=600 \mathrm{~s}$. The reduced speed areas can be set at any time during the simulation in VISSIM, to simulate different kinds of incidents/accidents in the suburb scenarios.
2) Simulation Settings in Java: To evaluate the performance of the path-planning algorithm in Java, with the same region, 500 vehicular nodes with transmission radius of 150 m are first randomly deployed to cover the $\mathrm{K}-\mathrm{W}$ downtown region, as shown in Fig. 3. In addition, 12 intersections are chosen as candidates for RSU deployment in the region. Further, each


Fig. 4. Performance evaluation of the proposed transmission mechanism in a medium-vehicle-density scenario. (a) Transmission performances in a high-vehicledensity scenario. (b) PDF of V2V distance. (c) PDF of the last hop V2R distance. (d) Transmission delay of a vehicle to an RSU given the transmission range.
vehicle moves to its destination with a velocity of $60 \mathrm{~km} / \mathrm{h}$ (or $30 \mathrm{~km} / \mathrm{h}$ ). The path planning can be performed at the beginning of a sample time, e.g., 10 s . The lifetime of a warning message, i.e., $T_{L}$, is set as 300 s . The duration for each simulation is set to be 3 h , and the results are averaged over 100 runs. To illustrate the effect of different kinds of accidents on path planning, big accidents are set to last for 20 min , whereas small accidents are set to last for only 10 min .

## B. Evaluation of Transmissions in VISSIM

We first evaluate the transmission performance of VANETs in a high-density scenario. The evaluated metrics are the connection probability of a vehicle to an RSU and the end-to-end transmission delay. As shown in Fig. 4(a), in a high-density scenario, the connection probability is high even without the support of a cellular network. For instance, when the vehicle transmission range is 120 m (which is very easy to be reached as discussed in [45] and way larger than the average headway distance), the connection probability can be $80 \%$. As the transmission range of vehicle increases, the connection probability increases; since the increased, the transmission range supplies more chances to connect with other vehicles or RSUs. Furthermore, as shown in Fig. 4(a), in the high-density case, the transmission delay is only around 5.5 s , which is less than a sample time of 10 s . Notice that a short end-to-end transmission delay facilitates the implementation of real-time path planning,
which needs traffic information update as timely and accurate as possible.

The intercontact time is evaluated through the vehicle headway distance (i.e., V2V distance) and the last-hop V2R distance. Based on the trace files from VISSIM, Fig. 4(b) shows the probability density function (pdf) of vehicle headway distance. It is shown that the pdf of the headway distance matches well with an exponential distribution, as shown in Fig. 4(b), which validates the premise in Section III-C. Based on the resultant headway-distance distribution, the average V 2 V intercontact time $E\left[T_{\mathrm{v} 2 \mathrm{v}}\right]$ can be obtained, as shown in Section IV-B,

Moreover, the pdf of the distance from the last-hop vehicle to the nearest RSU for one delivery is given in Fig. 4(c). The simulated pdf matches well with the theoretical pdf, which is calculated with the parameters in the simulation setup based on (5). According to Fig. 4(c), the average distance from a last-hop vehicle to its neatest RSU can be further calculated to be around 180 m . Then, the transmission delay incurred by the intercontact time of the last-hop V2R transmission can be calculated as discussed in Section IV-B, i.e., $E\left[T_{\text {off }}\right]=$ $E\left[U_{\text {off }}\right] / \bar{V}=E[$ Last - hop $V 2 R$ distance $-R] / \bar{V}$.

We then investigate the end-to-end transmission performance in terms of the connection probability and transmission delay in the medium-density scenario. Based on the proposed transmission mechanism, a hybrid VANET is utilized to reduce the transmission delay, making the path planning more efficient and
timely. As shown in Fig. 4(d), via pure VANETs, the average end-to-end transmission delay decreases as the transmission range increases since the increased transmission range gives higher possibilities for a transmitting vehicle to find an end-toend path to an RSU (given neglectable transmission delay when two vehicles are within the transmission range of each other). Moreover, in hybrid VANETs, when the public transportation system is utilized, the increased transmission range can significantly create more chances to meet a bus or a taxi, thus leading to a smaller transmission delay. Notice that, once any bus or taxi nodes receive the messages, they can help deliver the messages to the vehicle-traffic server directly via the cellular network, and the intermittent connections of the multihop VANET can be efficiently reduced. In particular, as the transmission range of vehicles becomes smaller (i.e., the problem of intermittent connections in VANETs is more severe), the delay reduction comes to be bigger if the hybrid-VANET-enhanced transportation system is involved. The reason is that, with a smaller transmission range, an end-to-end transmission path is more difficult to be guaranteed by pure VANETs, leading to a larger delay gap compared with the one that utilizes the hybrid-VANET-enhanced transportation system. In addition, the simulated results of transmission delay match well to the theoretical ones shown in (10). Hence, based on the proposed transmission mechanism, an efficient and timely message transmission for path planning can be achieved, which makes it possible to perform global real-time path planning.

## C. Simulation of the Proposed Path Planning in Java

Fig. 5(a) shows the AMD with and without implementing the proposed path-planning algorithm. We can observe that the AMD with the proposed path planning is much lower than that without path planning. For example, when accident number is two, AMD is reduced by $35 \%$. Furthermore, with more accidents, AMD becomes longer; however, the ones utilizing the proposed path-planning algorithm increase more slowly. The cost of path planning in terms of the increased path length is also shown in Fig. 5(a). When a vehicle wants to change its previous shortest path due to a sensed accident ahead, a novel smooth path is generated with less AMD at the cost of the increased path length. It shows that the average cost for users is still admissible when traffic environments are experiencing terrible conditions.
In addition, Fig. 5(b) shows the AMD comparison between our proposed path-planning algorithm and a distributed pathplanning algorithm proposed in [46]. In the distributed path planning, each individual vehicle researches a new path based on the known information of accidents when it receives any information on congestion or accidents but neither with coordination among vehicles nor considering the individual cost of path planning. As shown in Fig. 5(b), AMD under our proposed path planning is reduced on average by $27 \%$, as compared with that of the distributed algorithm. Because each individual vehicle plans path only on its own interest, it is very possible that a number of vehicles swarm into the same road segment based on the same warning message information. Then, new traffic jam can happen with high probability and result in the increased


Fig. 5. AMD reduction by path planning. (a) Comparison of AMD between the proposed path planning and the traditional one. (b) Comparison of AMD between the proposed path planning and one distributed algorithm.

AMD. Fig. 5(b) shows a good adaptability of the proposed pathplanning algorithm to avoid introducing other traffic jam.

Fig. 6(a) shows the effect of different kinds of accidents on AMD. It is shown that, when a big accident continues for long duration (i.e., 20 min ), AMD increases, compared with a small accident (i.e., lasting 10 min only). This is because, as some vehicles have no capabilities to change their current paths (e.g., buses), AMD increases due to their longer trapped time in congestion. Similarly, when the number of accidents increases, AMD becomes longer, but not much. Thus, it implies that our proposed path-planning algorithm is with a good adaptability to different accident duration. Moreover, if the number of slow-speed vehicles increases, more vehicles slowed down to $30 \mathrm{~km} / \mathrm{h}$ will introduce larger AMD, as shown in Fig. 6(b). Since more slow vehicles on one road can result in high vehicle density, Fig. 6(b) shows good adaptability to vehicle densities. Furthermore, comparing this performance with the one in Fig. 5(a), AMD is a little longer than the case under few slow vehicles since network vehicle-traffic throughput is diminished due to more vehicles with slow speed stranded on one road.

The sensitivity analyses in terms of both the vehicle number and the number of accidents on AMD are discussed in Fig. 7. Here, we considered that the accidents are big, lasting for 20 min . First, we can see that the AMD increases with the increased number of vehicles under our algorithm in Fig. 7.


Fig. 6. AMD versus specified accidents. (a) AMD comparison between different accident time duration. (b) AMD comparison between different numbers of slow vehicles.


Fig. 7. AMD versus both the number of vehicles and specified accidents.

The reason for this AMD increment is that more vehicles may result in a higher probability of introducing another traffic jam at crossings. However, taking the case with three accidents as an example, even when the number of vehicles increases to 800 , AMD is relatively small, around 375 s, as shown in Fig. 7. This result shows a good adaptability of the proposed path-planning algorithm to the total vehicle number. In addition, Fig. 7 shows that the AMD increases with the increased number of accidents with the similar trend as stated previously.

## VIII. Conclusion

In this paper, we have developed a hybrid-VANET-enhanced real-time path planning for vehicles to avoid congestion in an ITS. We first propose a hybrid-VANET-enhanced ITS framework with functionalities of real-time traffic information collection, involving both V2V and V2R communications in VANETs and cellular communications in public transportation system. Then, a globally optimal real-time path-planning algorithm is designed to improve overall spatial utilization and reduce average vehicle travel cost by means of Lyapunov optimization. Extensive simulations have been conducted to demonstrate that the proposed path-planning algorithm can achieve better performance than that without real-time path planning in terms of AMD and the adaptability to different accident duration and traffic densities. In future work, we intend to find large-scale real-world vehicle traffic traces to further validate benefits of the proposed algorithm in practical scenarios.

## REFERENCES

[1] Texas Transp. Inst. (2007). Texas Transportation Institute: Urban mobility information annual urban mobility report, College Station, TX, USA. [Online]. Available: http://mobility.tamu.edu/ums
[2] M. Papageorgiou, C. Diakaki, V. Dinopoulou, A. Kotsialos, and Y. Wang, "Review of road traffic control strategies," Proc. IEEE, vol. 91, no. 12, pp. 2043-2067, Dec. 2003.
[3] T. Hunter, R. Herring, P. Abbeel, and A. Bayen, "Path and travel time inference from GPS probe vehicle data," in Proc. Neural Inf. Process. Syst. Found., Vancouver, BC, Canada, Dec. 2009, pp. 1-8.
[4] H. Hartenstein and K. Laberteaux, VANET: Vehicular Applications and Inter-Networking Technologies. Hoboken, NJ, USA: Wiley, 2010.
[5] [Online]. Available: http://www.nhtsa.gov/
[6] R. Lu, X. Lin, and X. Shen, "SPRING: A social-based privacy-preserving packet forwarding protocol for vehicular delay tolerant networks," in Proc. IEEE INFOCOM, San Diego, CA, USA, Mar. 2010, pp. 1-9.
[7] M. Wang, H. Liang, R. Zhang, R. Deng, and X. Shen, "Mobility-aware coordinated charging for electric vehicles in VANET-enhanced smart grid," IEEE J. Sel. Areas Commun., vol. 32, no. 7, pp. 1-17, Jul. 2014.
[8] A. Skabardonis and N. Geroliminis, "Real-time monitoring and control on signalized arterials," J. Intell. Transp. Syst.-Technol., Plan., Oper., vol. 12, no. 2, pp. 64-74, May 2008.
[9] I. Leontiadis et al., "On the effectiveness of an opportunistic traffic management system for vehicular networks," IEEE Trans. Intell. Transp. Syst., vol. 12, no. 4, pp. 1537-1548, Dec. 2011.
[10] N. Drawil and O. Basir, "Intervehicle-communication-assisted localization," IEEE Trans. Intell. Transp. Syst., vol. 11, no. 3, pp. 678-691, Sep. 2010.
[11] A. Khosroshahi, P. Keshavarzi, Z. KoozehKanani, and J. Sobhi, "Acquiring real time traffic information using VANET and dynamic route guidance," in Proc. IEEE Comput., Control Ind. Eng., Wuhan, China, Aug. 2011, pp. 9-13.
[12] P. Chen, Y. Guo, and W. Chen, "Fuel-saving navigation system in VANETs," in Proc. IEEE Veh. Technol. Conf., Ottawa, ON, Canada, Sep. 2010, pp. 1-5.
[13] T. Schouwenaars, B. Moor, E. Feron, and J. How, "Mixed integer programming for multi-vehicle path planning," in Proc. Eur. Control Conf., Porto, Portugal, Sep. 2001, pp. 2603-2608.
[14] M. Kimra, S. Inoue, Y. Taoda, T. Dohi, and Y. Kakuda, "A novel method based on VANET for alleviating traffic congestion in urban transportations," in Proc. IEEE Auton. Decentralized Syst., Mexico City, Mexico, Mar. 2013, pp. 1-7.
[15] M. Abboud, L. Jaoude, and Z. Kerbage, "Real time GPS navigation system," 2004. [Online]. Available: http://webfea-lb.fea.aub.edu.lb/ proceedings/2004/SRC-ECE-27.pdf
[16] Y. Chung, "Development of an accident duration prediction model on the Korean Freeway Systems," Accid. Anal. Prev., vol. 42, no. 1, pp. 282-289, Jan. 2010.
[17] Y. Zhao, K. Triantis, D. Teodorovic, and P. Edara, "A travel demand management strategy: The downtown space reservation system," Eur. J. Oper. Res., vol. 205, no. 3, pp. 584-594, Sep. 2010.
[18] J. Herrera, D. Work, R. Herring, X. Ban, and A. Bayen, "Evaluation of traffic data obtained via GPS-enabled mobile phones: The mobility century field experiment," presented at the 15th World Congr. Intell. Transp. Syst., New York, NY, USA, Aug., 2009, Working Paper UCB-ITS-VWP-2009-8.
[19] R. Herring, A. Hofleitner, and S. Amin, "Using mobile phones to forecast arterial traffic through statistical learning," in Proc. 89th Annu. Meet. Transp. Res. Board, Washington, DC, USA, Jan. 2010, pp. 1-22.
[20] J. Jariyasunant et al., "Mobile transit trip planning with real-time data," in Proc. 89th Annu. Meet. Transp. Res. Board, Washington, DC, USA, Jan. 2010, pp. 1-17.
[21] J. Chen and A. M. Bayen, "Traffic flow reconstruction using mobile sensors and loop detector data," in Proc. 87th Annu. Meet. Transp. Res. Board, Washington, DC, USA, Jan. 2008, pp. 1-18.
[22] H. Liu, A. Danczyk, R. Brewer, and R. Starr, "Evaluation of cell phone traffic data in minnesota," Transp. Res. Rec., vol. 2086, no. 1, pp. 1-7, Dec. 2008.
[23] B. Hoh, M. Gruteser, and R. Herring, "Virtual trip lines for distributed privacy-preserving traffic monitoring," in Proc. 6th Annu. Int. Conf. Mobile Syst., Appl. Serv., Breckenridge, CO, USA, Jun. 2008, pp. 15-28.
[24] H. T. Cheng, H. Shan, and W. Zhuang, "Infotainment and road safety service support in vehicular networking: From a communication perspective," Mech. Syst. Signal Process., vol. 25, no. 6, pp. 2020-2038, Aug. 2011.
[25] J. Zhao and G. Cao, "VADD: Vehicle-assisted data delivery in vehicular ad hoc networks," in Proc. IEEE INFOCOM, Barcelona, Spain, Apr. 2006, pp. 1-12.
[26] T. H. Luan, X. Ling, and X. Shen, "Provisioning QoS controlled media access in vehicular to infrastructure communications," Ad Hoc Netw., vol. 10, no. 2, pp. 231-242, Mar. 2012.
[27] C. Xu, F. Zhao, J. Guan, and G. Muntean, "QoE-driven user-centric VoD services in urban multihomed P2P-based vehicular networks," IEEE Trans. Veh. Technol., vol. 62, no. 5, pp. 2273-2289, Jun. 2013.
[28] L. Zhou, Y. Zhang, K. Song, W. Jing, and A. Vasilakos, "Distributed media services in P2P-based vehicular networks," IEEE Trans. Veh. Technol., vol. 60, no. 2, pp. 692-703, Feb. 2011.
[29] M. Rousan, A. AlAli, and K. Darwish, "GSM-based mobile telemonitoring and management system for inter-cities public transportations," in Proc. IEEE Int. Conf. Ind. Technol., Hammamet, Tunisia, Dec. 2004, pp. 859-862.
[30] T. Schoepflin and D. Dailey, "Dynamic camera calibration of roadside traffic management cameras for vehicle speed estimation," IEEE Trans. Intell. Transp. Syst., vol. 4, no. 2, pp. 90-98, Jun. 2003.
[31] S. Dornbush and A. Joshi, "Streetsmart traffic: Discovering and dissemination automobile congestion using VANETs," in Proc. IEEE Veh. Technol. Conf., Dublin, Ireland, Apr. 2007, pp. 11-15.
[32] J. Chen et al., "Utility-based asynchronous flow control algorithm for wireless sensor networks," IEEE J. Sel. Areas Commun., vol. 28, no. 7, pp. 1116-1126, Sep. 2010.
[33] Z. Li, Y. Zhu, H. Zhu, and M. Li, "Compressive sensing approach to urban traffic sensing," in Proc. ICDCS, Minneapolis, MN, USA, Jun. 2011, pp. 889-898.
[34] R. Dowling, A. Skabardonis, M. Carroll, and Z. Wang, "Methodology for measuring recurrent and nonrecurrent traffic congestion," Transp. Res. Rec., J. Transp. Res. Board, no. 1867, pp. 60-68, 2004.
[35] A. Abdrabou and W. Zhuang, "Probabilistic delay control and road side unit placement for vehicular ad hoc networks with disrupted connectivity," IEEE J. Sel. Areas Commun., vol. 29, no. 1, pp. 129-139, Jan. 2011.
[36] A. May, Traffic Flow Fundamentals. Englewood Cliffs, NJ, USA: Prentice-Hall, 1990.
[37] N. Wisitpongphan, F. Bai, P. Mudalige, V. Sadekar, and O. Tonguz, "Routing in sparse vehicular ad hoc networks," IEEE J. Sel. Areas Commun., vol. 25, no. 8, pp. 1538-1556, Oct. 2007.
[38] M. Wang et al., "Throughput capacity of VANETs by exploiting mobility diversity," in Proc. IEEE ICC, Ottawa, ON, Canada, Jun. 2012, pp. 4980-4984.
[39] Highway Capacity Manual (2000), Transp. Res. Board, Nat. Res. Council, Washington, DC, USA, 2000.
[40] H. Liang, B. J. Choi, W. Zhuang, and X. Shen, "Optimizing the energy delivery via V2G systems based on stochastic inventory theory," IEEE Trans. Smart Grid, vol. 4, no. 4, pp. 2230-2243, Dec. 2013.
[41] M. Neely, Stochastic Network Optimization With Application to Communication and Queueing Systems. San Rafael, CA, USA: Morgan and Claypool, 2010.
[42] L. Georgiadis, M. Neely, and L. Tassiulas, "Resource allocation and crosslayer control in wireless networks," Found. Trends Netw., vol. 1, no. 1, pp. 1-149, Apr. 2006.
[43] R. Urgaonkar, U. C. Kozat, K. Igarashi, and M. Neely, "Dynamic resource allocation and power management in virtualized data centers," in Proc. IEEE Netw. Oper. Manage. Symp., Osaka, Japan, Apr. 2010, pp. 479-486.
[44] [Online]. Available: http://vision-traffic.ptvgroup.com/en-uk/products/ ptv-vissim/
[45] L. Cheng, B. E. Henty, D. D. Stancil, F. Bai, and P. Mudalige, "Mobile vehicle-to-vehicle narrow-band channel measurement and characterization of the 5.9 GHz Dedicated Short Range Communication (DSRC) frequency band," IEEE J. Sel. Areas Commu., vol. 25, no. 8, pp. 15011516, Oct. 2007.
[46] R. Guha and W. Chen, "A distributed traffic navigation system using vehicular communication," in Proc. IEEE Veh. Netw. Conf., Tokyo, Japan, Oct. 2009, pp. 1-8.


Miao Wang received the B.Sc. degree from Beijing University of Posts and Telecommunications, Beijing, China, in 2007 and the M.Sc. degree from Beihang University, Beijing, in 2010. She is currently working toward the Ph.D. degree with the Department of Electrical and Computer Engineering, University of Waterloo, Waterloo, ON, Canada.

Her current research interests include traffic control, capacity and delay analysis, and routing protocol design for vehicular networks.


Hangguan Shan (M'10) received the B.Sc. degree in electrical engineering from Zhejiang University, Hangzhou, China, in 2004 and the Ph.D. degree in electrical engineering from Fudan University, Shanghai, China, in 2009.

From 2009 to 2010, he was a Postdoctoral Research Fellow with the University of Waterloo, Waterloo, ON, Canada. Since February 2011, he has been with the Department of Information Science and Electronic Engineering, Zhejiang University, as an Assistant Professor. His research interests include resource management and quality-of-service provisioning in vehicular ad hoc networks, wireless body area networks, and cooperative networks.

Dr. Shan coreceived the Best Industry Paper Award at the IEEE Wireless Communications and Networking Conference, Quintana-Roo, Mexico, in 2011.


Rongxing Lu (S'09-M'11) received the Ph.D. degree in computer science from Shanghai Jiao Tong University, Shanghai, China, in 2006 and the Ph.D. degree in electrical and computer engineering from the University of Waterloo, Waterloo, ON, Canada, in 2012.

From May 2012 to April 2013, he was a Postdoctoral Fellow with the University of Waterloo, Waterloo, ON, Canada. Since May 2013, he has been an Assistant Professor with the School of Electrical and Electronics Engineering, Nanyang Technological University, Singapore. His research interests include wireless network security, big data security and privacy, network coding security, and applied cryptography.


Ran Zhang received the B.E. degree in electronics engineering from Tsinghua University, Beijing, China, in 2010. He is currently working toward the Ph.D. degree with the Broadband Communication Research Group, University of Waterloo, Waterloo, ON, Canada.

His current research interests include resource management in heterogeneous wireless access networks, carrier aggregation in Long-Term Evolution Advanced systems, and electrical vehicle charging control in smart grids.


Xuemin (Sherman) Shen (M'97-SM'02-F'09) received the B.Sc. degree from Dalian Maritime University, Dalian, China, in 1982 and the M.Sc. and Ph.D. degrees from Rutgers University, Piscataway, NJ, USA, in 1987 and 1990, all in electrical engineering.

From 2004 to 2008, he was the Associate Chair for Graduate Studies with the Department of Electrical and Computer Engineering, University of Waterloo, Waterloo, ON, Canada. He is currently a Professor and the University Research Chair with the Department of Electrical and Computer Engineering, University of Waterloo. He is a coauthor or editor of six books and the author of several papers and book chapters in wireless communications and networks, control, and filtering. His research interests include resource management in interconnected wireless/ wired networks, wireless network security, wireless body area networks, and vehicular ad hoc and sensor networks.

Dr. Shen served as the Technical Program Committee Chair for the 2010 Fall IEEE Vehicular Technology Conference (IEEE VTC'10 Fall); the Symposia Chair for the 2010 IEEE International Conference on Communications (IEEE ICC'10); the Tutorial Chair for IEEE VTC'11 Spring and IEEE ICC'08; the Technical Program Committee Chair for the 2007 IEEE Global Communications Conference; the General Cochair for the 2007 IEEE International Conference on Communications and Networking in China and the 2006 Third International Conference on Quality of Service in Heterogeneous Wired/ Wireless Networks; and the Chair for IEEE Communications Society Technical Committee on Wireless Communications and Peer-to-Peer Communications and Networking. He also serves/served as the Editor-in-Chief for IEEE NETWORK, Peer-to-Peer Networking and Application, and IET Communications; as a Founding Area Editor for IEEE Transactions on Wireless Communications; as an Associate Editor for IEEE Transactions on Vehicular Technology, Computer Networks, and ACM Wireless Networks; and as the Guest Editor for IEEE Journal on Selected Areas in Communications, IEEE Wireless Communications, IEEE Communications Magazine, and ACM Mobile Networks and Applications. He is a registered Professional Engineer of Ontario, Canada; a Fellow of the Canadian Academy of Engineering and the Engineering Institute of Canada; and a Distinguished Lecturer of the IEEE Vehicular Technology and Communications Societies.


Fan Bai received the B.S. degree in automation engineering from Tsinghua University, Beijing, China, in 1999 and the M.S. and Ph.D. degrees in electrical engineering from the University of Southern California, Los Angeles, CA, USA, in 2005.

Since September 2005, he has been a Senior Researcher with the Electrical and Control Integration Laboratory, Research and Development and Planning, General Motors Corporation, Warren, MI, USA. He is also serving as a Ph.D. supervisory committee member at Carnegie Mellon University, Pittsburgh, PA, USA, and the University of Illinois at Urbana-Champaign, Champaign, IL, USA. He is the author of about 40 book chapters and papers presented in conference and published in prestigious journals, including the ACM Annual International Conference on Mobile Computing and Networking, the IEEE International Conference on Computer Communications, the ACM International Symposium on Mobile Ad Hoc Networking and Computing, the IEEE Communications Society Conference on Networks, the IEEE International Conference on Communications, the IEEE Global Communications Conference, the IEEE Wireless Communications and Networking Conference, the IEEE Journal on Selected Areas in Communications, the IEEE Wireless Communication Magazine, the IEEE Communication Magazine, and the Elsevier Ad Hoc Networks Journal. His current research interests include the discovery of fundamental principles and the analysis and design of protocols/systems for next-generation vehicular ad hoc networks for safety, telematics, and infotainment applications.

Dr. Bai serves as a Technical Program Cochair for the 2007 IEEE International Symposium on Wireless Vehicular Communications and the 2008 International Workshop on Mobile Vehicular Networks. He also currently serves as an Associate Editor for the IEEE Transaction on Vehicular Technology and the IEEE Transaction on Mobile Computing. He also serves as a Guest Editor for IEEE Wireless Communication Magazine, IEEE Vehicular Technology Magazine, and Elsevier Ad Hoc Networks Journal. He received the Charles L. McCuen Special Achievement Award from General Motors Corporation in 2006, in recognition for his extraordinary accomplishment in the area of vehicle-to-vehicle communications for drive assistance and safety.


[^0]:    Manuscript received February 10, 2014; revised April 28, 2014; accepted June 6, 2014. Date of publication July 2, 2014; date of current version May 12, 2015. This work was supported in part by a research grant from the Natural Science and Engineering Research Council (NSERC) of Canada, by a research grant from General Motors, and by the Zhejiang Provincial Natural Science Foundation of China under Grant LY12F01021. The review of this paper was coordinated by Prof. Y. Qian. (Corresponding author: H. Shan.)
    M. Wang, R. Zhang, and X. Shen are with the Department of Electrical and Computer Engineering, University of Waterloo, Waterloo, ON N2L 3G1, Canada.
    H. Shan is with the Department of Information Science and Electronic Engineering, Zhejiang University, Hangzhou 310027, China.
    R. Lu is with Communication Engineering School of Electrical and Electronics Engineering, Nanyang Technological University, Singapore 639798.
    F. Bai is with ECI Lab, General Motors Global RD, Warren, MI 48092 USA.

    Color versions of one or more of the figures in this paper are available online at http://ieeexplore.ieee.org.

    Digital Object Identifier 10.1109/TVT.2014.2335201

[^1]:    ${ }^{1}$ On February 3, 2014, the U.S. Department of Transportation's National Highway Traffic Safety Administration announced that it will begin taking steps to enable V2V for vehicles to talk to each other and ultimately avoid crashes altogether by exchanging basic safety data [5].

[^2]:    ${ }^{2}$ In this paper, the headway distance is defined as the distance between two neighboring vehicles in the same lane.

[^3]:    ${ }^{3}$ The approximation is valid if the end-to-end transmission delay can be well controlled to a small value in which the network topology changes little or the source vehicle only moves a relatively short distance.

[^4]:    ${ }^{4}$ The bus equivalent is the number of buses displaced by a single taxi or a private car in a suburb area [39].

[^5]:    ${ }^{5}$ The definition of queue and network stability is also used, for example, in [42] and [43] for the stability and utility optimization to make online control decisions.

