Department of Pure Mathematics University of Waterloo Waterloo, ON N2L 3G1 Telephone: (519) 888-4567 ext. 45698 Fax: (519) 725-0160 Email: yrliu@uwaterloo.ca

Fields of Research

Analytic Number Theory, Number Theory in Function Fields, The Circle Method, Sieve Methods

Education

Ph.D. Mathematics, Harvard University, 2003 Dissertation: Generalizations of the Turán and the Erdős-Kac Theorems

Supervisor: Barry C. Mazur
M.S. Mathematics, Queen's University, 1998
Dissertation: The Turán Sieve and Some of its Applications
Supervisor: M. Ram Murty

B.A. Mathematics, McGill University, 1998

Employment History

2013–present	Professor, Department of Pure Mathematics, University of Waterloo
2008 – 2013	Associate Professor, Department of Pure Mathematics, University of Waterloo
Winter 2007	Visiting Scholar, Department of Mathematics, University of Michigan
Winter 2005	Visiting Scholar, Department of Mathematics, University of Michigan
2003-2008	Assistant Professor, Department of Pure Mathematics, University of Waterloo

Honours and Awards

2023	Colloquium Speaker, PIMS-Lethbridge Distinguished Lecture Series,
	University of Lethbridge
2021	Key Speaker, Hausdorff School: The Circle Method,
	Hausdorff Center for Mathematics
2021	Colloquium Speaker, Women Lecture Series for AWM's 50th Anniversary,
	Kansas States University
2013	Distinction in Teaching Award, Faculty of Mathematics, University of Waterloo
2012	Outstanding Performance Award, University of Waterloo
2011	Instructor of the Year, Mathematical Society at the University of Waterloo
2005	G. de B. Robinson Award, Canadian Mathematical Society
2003 – 2008	University Faculty Award, Natural Sciences and Engineering Research Council
2002	Certificate of Distinction in Teaching, Harvard University
2001	Certificate of Distinction in Teaching, Harvard University

Research Grants

2016 - 2022	NSERC Individual Discovery Grant
2011 - 2016	NSERC Individual Discovery Grant
2006 – 2011	NSERC Individual Discovery Grant
2003 – 2006	NSERC Individual Discovery Grant
2003 – 2005	University of Waterloo Start-up Grant

Publication List

- On the number of irreducible factors with a given multiplicity in function fields (with S. Das,
 E. Elma and W. Kuo), 20 pages, to apper in Finite Fields Appl..
- Equidistribution of polynomial sequences in function fields, with applications (with T. H. Lê and T. D. Wooley), 37 pages, submitted.
- Bounds on 10th moments of (x, x^3) for ellipsephic sets (with T. C. Anderson, B. Hu and A. Talmage), to appear in AMS Contemporary Mathematics, 11 pages.
- Sieve Methods in Random Graph Theory (with J.C. Sounders), Graphs and Combin. 39 (2023), Article number: 39, 23 pages.
- Number of prime factors with a given multiplicity (with E. Elma), Canad. Math. Bull., 65 (2022), 253-269.
- The shifted Turán sieve method on tournaments II (with W. Kuo, S. Ribas and K. Zhou), Discrete Mathematics, 344 (2021), Page No. 112602, 11 pages.
- The asymptotic estimates and Hasse principle for multidimensional Warings problem (with W. Kuo and X. Zhao), Adv. Math. 353 (2019), 1-66.
- The shifted Turán sieve method on tournaments (with W. Kuo, S. Ribas and K. Zhou),
 Canad. Math. Bull. 62 (2019), 841-855.
- A. Bhowmick, T. H. Le and Y.-R. Liu, A note on character sums in finite fields, Finite Fields Appl. 46 (2017), 247-254.
- Y.-R. Liu and C. Spencer, A prime analogue of Roth's theorem in function fields, Advances in the Theory of Number: Proceedings of the CNTA XIII (2015), 105-148.
- W. Kuo, Y.-R. Liu and X. Zhao, Multidimensional Vinogradov-type estimates in function fields, Canad. J. Math 66 (2014), 844-873.
- T. H. Le and Y.-R. Liu, On sets of polynomials whose difference set contain no squares, Acta. Arith. 161 (2013), 127-143.
- Y.-R. Liu and X. Zhao, A generalization of Roth's theorem in function fields, Michigan Math. J. 61 (2012), 839-866.

 Y.-R. Liu, C. V. Spencer and X. Zhao, A generalization of Meshulam's theorem on subsets of finite abelian groups with no 3-term arithmetic progression (II), European J. of Combin. 32 (2011), 258-264.

- Y.-R. Liu and T. D. Wooley, Waring's problem in function fields, J. Reine Angew. Math., 638 (2010), 1-67.
- Y.-R. Liu, C. V. Spencer and X. Zhao, Roth's theorem on system of linear forms in function fields, Acta. Arith., 142 (2010), 377-386.
- W. Kuo and Y.-R. Liu, Gaussian laws on Drinfeld modules, Int. J. Number Theory 7 (2009), 1179–1203.
- W. Kuo and Y.-R. Liu, Cyclicity of finite Drinfeld modules, J. London Math. Soc. 80 (2009), 567-584.
- W. Kuo and Y.-R. Liu, A Carlitz module analogue of a conjecture of Erdős and Pomerance, Trans. Amer. Math. Soc. 361 (2009), 4519-4539.
- Y.-R. Liu and C. V. Spencer, A generalization of Roth's theorem in function fields, Int. J. Number Theory 7 (2009), 1149-1154.
- Y.-R Liu and C. V. Spencer, A generalization of Meshulam's theorem on subsets of finite abelian groups with no 3-term arithmetic progression, Des. Codes Cryptogr. 52 (2009), 83-91.
- W. Kuo and Y.-R. Liu, The Erdős-Kac theorem and its generalizations, The anatomy of integers, CRM Proceedings & Lecture Notes 46 (2008), 209-216.
- Y.-R. Liu and T. D. Wooley, The unrestricted variant of Waring's problem in function fields, Funct. Approx. Comment. Math. 37 (2007), 285-292.
- Y.-R. Liu, Prime analogues of the Erdős-Kac theorem for elliptic curves, J. Number Theory 119 (2006), 155-170.
- Y.-R. Liu and M. R. Murty, A weighted Turán sieve method, J. Number Theory 116 (2006), 1-20
- Y.-R. Liu, A prime analogue of Erdős-Pomerance's conjecture for elliptic curves, Comment. Math. Helv. 80 (2005), 755-769.
- Y.-R. Liu, Prime divisors of the number of rational points on elliptic curves with complex multiplication, Bull. London Math. Soc. 37 (2005), 658-664.
- Y.-R. Liu and M. R. Murty, Sieve methods in combinatorics, J. Combin. Theory Ser. A 111 (2005), 1-23.
- Y.-R. Liu, A generalization of the Erdős-Kac theorem and its applications, Canad. Math. Bull. 47 (2004), 589-606.

 Y.-R. Liu, A generalization of the Turán theorem and its applications, Canad. Math. Bull. 47 (2004), 573-588.

- Y.-R. Liu, The Erdős theorem and the Halberstam theorem in function fields, Acta Arith. 114 (2004), 323-330.
- Y.-R. Liu and M. R. Murty, *The Turán sieve method and some of its applications*, J. Ramanujan Math. Soc. 14 (1999), 21-35.

Professional Activities

- Co-organizer, Analytic Number Theory and L-functions Session, CMS Meeting, Memorial University, June 2022
- Mini-course instrutor: An Introduction to the Circle Method, Lecture Series (3 online talks), Hausdorff School: the Circle Method, Hausdorff Center for Mathematics, May, 2021.
- Co-organizer, Analytic Number Theory Session, CMS Meeting, University of Toronto, December 2019
- Co-organizer, Analytic Number Theory Session, CMS Meeting, University of Waterloo, December 2017
- Co-instructor, Graduate Mini-Course on Efficient Congruencing, Fields Institute, March 2017
- Co-organizer, Workshop on Efficient Congruencing and Translation-invariant Systems, Fields Institute, March 2017
- Co-organizer, Thematic Program on o-minimality, Heights and Efficient Congruencing, Fields Institute, January-June 2017
- Member, Scientific Committee, CMS Meeting, Montreal, December 2015
- Editor, Taiwan Journal of Mathematics 2014-2020
- Local committee member, Two Weeks at Waterloo a Summer School for Women in Mathematics, University of Waterloo, August 2012
- Co-organizer, Canadian Number Theory Association Meeting X, University of Waterloo, July 2008
- Co-organizer, L-functions and Algebraic Curves Session, CMS Meeting, University of Waterloo, June 2005
- Co-organizer, Workshop in Number Theory and Random Matrix Theory, University of Waterloo, June 2005
- Lifetime member of Canadian Mathematics Society

Supervision (* indicates co-supervision and * indicates tenured or tenure-track positions)

PDF Zhenchao Ge* (in progress)

Alan Talmage*

2023
Julia Brandes*

2017

Thai Hoang Le^{\$\dightarrow\$} 2011, 2013, 2015

Craig Spencer[⋄] 2008

Ph.D. Jérémy Champagne (in progress)

Sourabhashis Das* (in progress)

Owen Sharpe (in progress) Yash Totani* (in progress)

Ertan Elma* 2020 John Sanders** 2018

Savio Ribas^{\$\display\$} 2017 (exchang student)

Shuntaro Yamagishi 2015 Xiaomei Zhao^{\dightarrow} 2010

M.Math Yen-Kang Fu (in progress)

Ismael El Yassini 2023

Zishen Qu* 2022 Owen Sharpe 2022 John Dykes 2018 Shuming Jia 2016 Cassie Naymie* 2012

Yui Nishizawa 2011 Leo Kwong 2010 Patrice Camire* 2008 Lalit Jain* 2008

Sourev Sen Gupta* 2008

Li Li 2007

Undergraduate Jason Hou 2023

Kareem Alfarra 2023 Logan Batson 2023

Aahan Chatterjee 2023 (two terms)

Thomas Plamondon 2023

James Houle 2022 Yen-Kang Fu 2022 Evan Girardin 2022 Maya Gusak 2022 Jacob Mausberg 2022 Zikang Lei 2021 Tuan Hiep Do 2021

Josué Kurke 2021 Andrew Luo 2021 11

Undergraduate Josué Kurke 2020

> Wanxin Li 2020 Jeffrey Tse 2020

Chin Ho Cheung* 2019 (exchange student)

Noah Rathjen* 2019 Yixin Chen 2018 Trevor Clokie 2018 Saiyue Lyn 2018

Zhenyuan Zhang 2018 Shouzhen Gu* 2017 Akshay Tiwary 2017

Ian Waudby-Smith 2017 Stephen Wen* 2017 Daniel Chen 2016

Arnaud Marek 2016 (exchange student)

David Spivak 2016

Kevin Kai Qi Zhao* 2015 Chao Hsian Lin 2013

Liyu Wang 2013 (two terms)

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Alexander Mangerel 2011, 2012

Peter Sinclair* 2011 Cassie Naymie 2010 Yui Nishizawa* 2010 Krishna Sivaranjan* 2010

Cyril Becker 2009, 2010 (exchange student)

Brad Hannigan-Daley* 2008

Jennifer Park* 2008

Pei Pei* 2008

David Rhee* 2008

Michael Lipnowski* 2007, 2008

Lloyd Elliot* 2007 Daniel Rowe* 2007

Michael Sgambelluri* 2007 Lalit Jain* 2006 (two terms)

Xiannan Li 2006

Adam Felix 2005, 2006

Eugene Eisenstein 2005

Teaching Experience

PMATH 944	Topics in Number Theory: Analytic Methods for Diophantine Problems (F13, F16)
PMATH 940	Topics in Number Theory: Analytic Methods for Diophantine Problems (W23)
PMATH 744	Topics in Number Theory: the Circle Method (F05)
PMATH 740/440	Analytic Number Theory (F15, F17; F23)
PMATH 642/442	Fields and Galois Theory (F04, F06, F07, F09)
PMATH 499	Elliptic Curves and Modular Forms (W08)
PMATH 499	Number Theory in Function Fields (S07)
PMATH 499	Sieve Methods (W10)
PMATH 348	Fields and Galois Theory (W16, W18, W20, W21, W22)
MATH 347	Groups and Rings (F16, S18, F22; F23)
MATH 145	Advanced Algebra (F07)
MATH 138	Calculus II (W08, W10, W14)
MATH 137	Calculus I (F06, S18)
MATH 135	Algebra (F03, F04, F05, F09, F10, W11, F15, W16, F16, F17, F19, F20, F21, F22)