



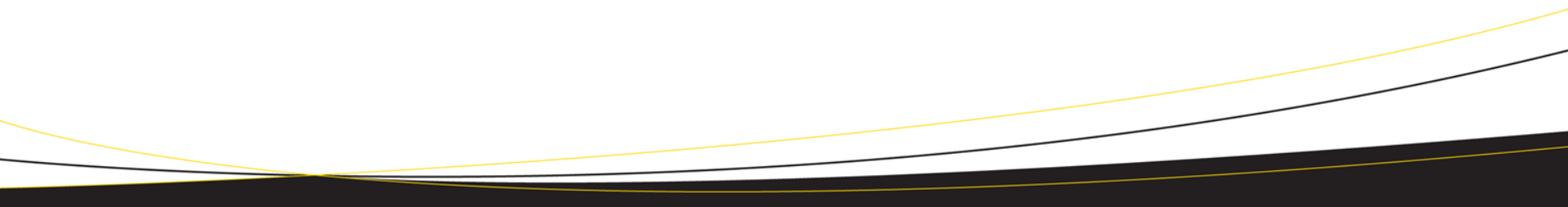
IGARSS 2013  
Melbourne, Australia  
July 21 – 26

# Continuous Sea Ice Thickness Estimation using a Joint MODIS/AMSR-E Guided Variational Model

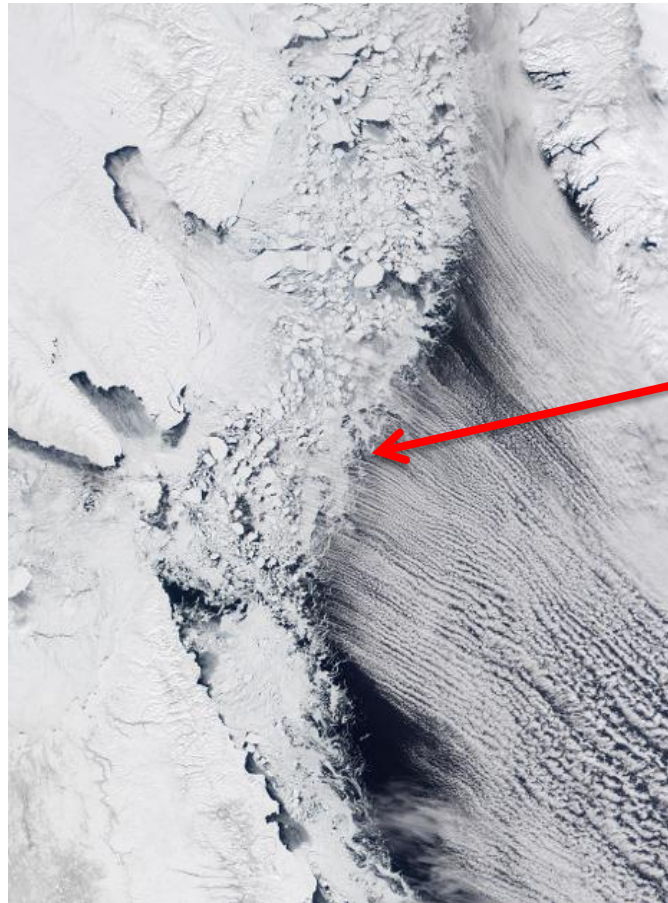
Alexander Wong, K. Andrea Scott, Edward Li, Robert Amelard  
Department of Systems Design Engineering  
University of Waterloo, Canada

# Motivation

- Sea ice thickness
  - Safe operations
  - Weather forecasts
- Manual measurement is unscalable
- Use remote sensing for estimating ice thickness



# Problem with VIS/IR

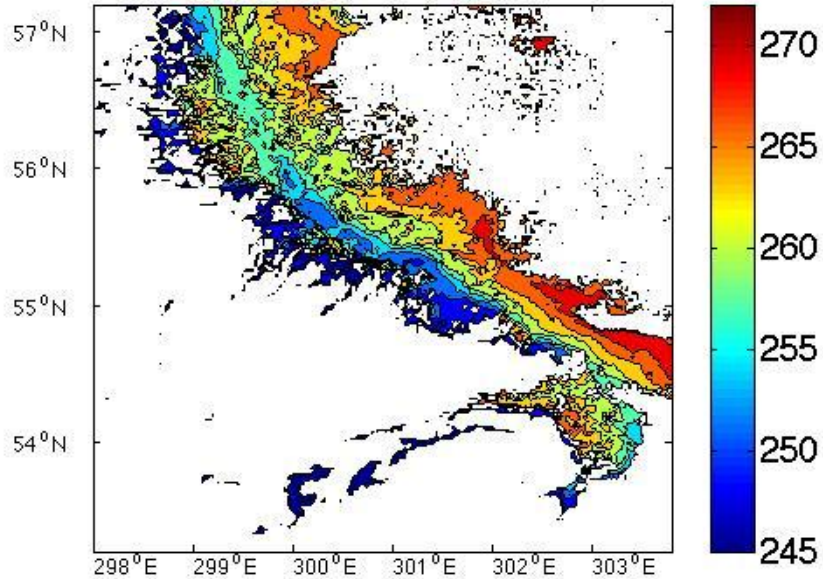


Cloud or ice?

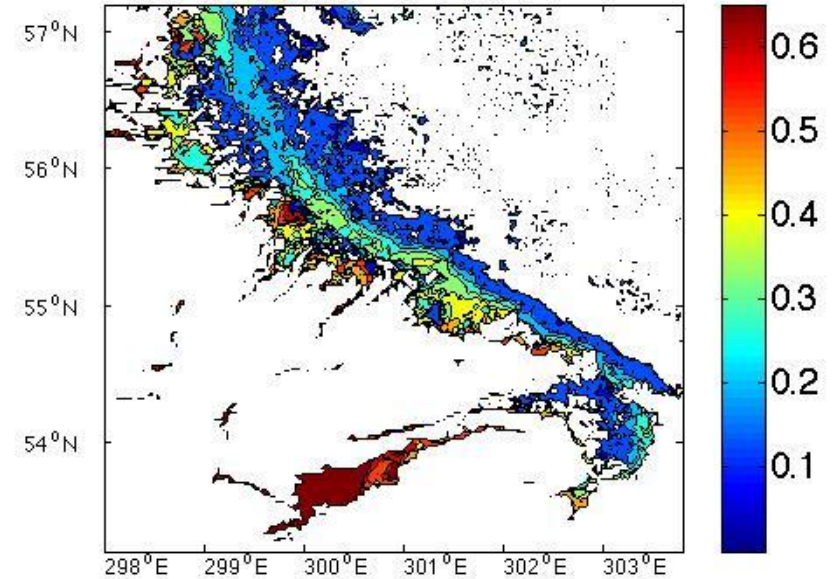
Source: Jacques Descloitres, MODIS Land Rapid  
Response Team

# Motivation

Ice temperature (K)



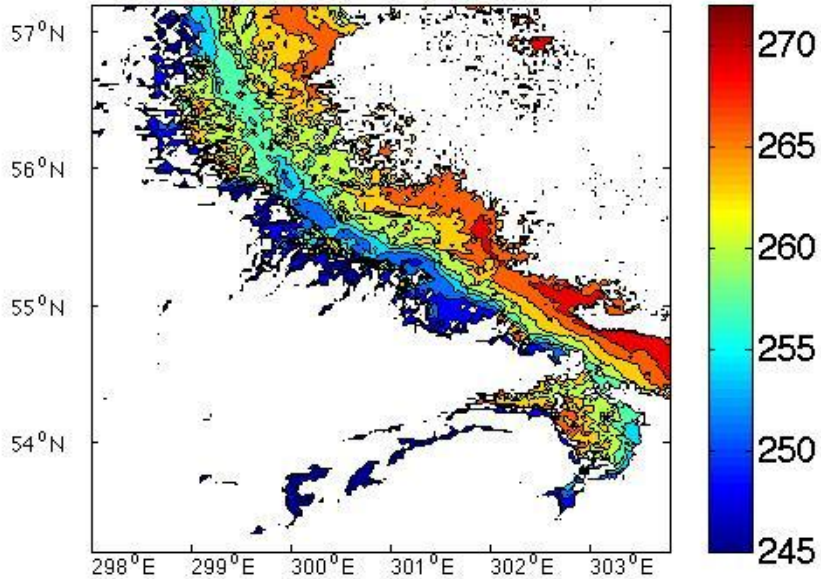
Ice thickness (m)



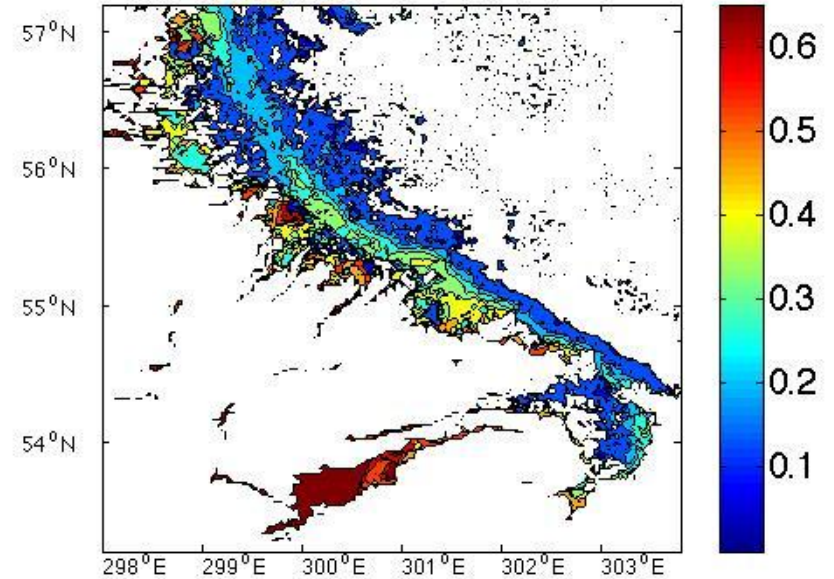
Labrador Coast, January 10, 2009

# Motivation

Ice temperature (K)

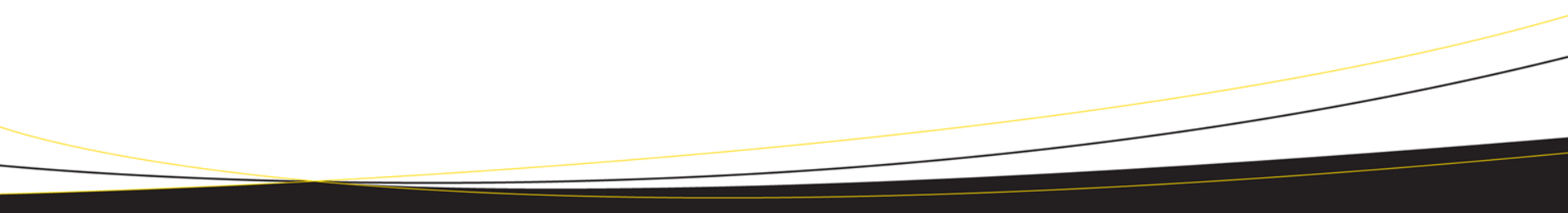


Ice thickness (m)

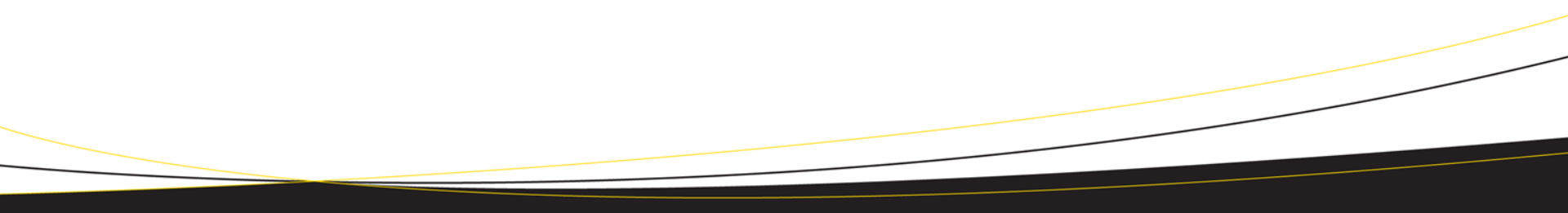


**(Inverse) correlation!**

# Outline

- Image data
  - Proposed Method
    1. **Temperature** generation
    2. **Ice thickness** estimate
  - Results
  - Conclusions & Future Work
- 

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- The bottom of the slide features decorative wavy lines in yellow and dark grey/black, creating a modern, abstract footer design.

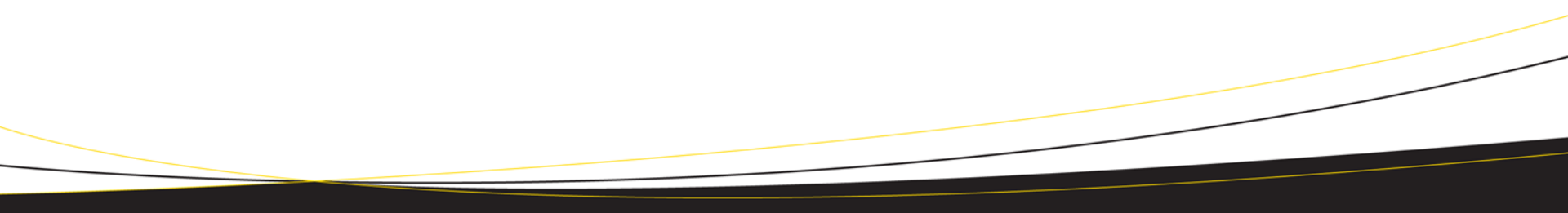


# Data

- Aqua satellite
  - AMSR-E (passive microwave)
    - 12.5km, sea ice concentration product
    - Lowest 3 bands (6.9, 10.8, 18.7 GHz)
  - MODIS (VIS/IR)
    - MOD29: 1km, ice temperature product (240—271K)
- Imagery
  - Jan 1 2007 – Feb 28 2007 (daily)
  - Baffin Island, Labrador Coast (Canada)



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- 



# High-Level Rationale

- 2 data types are very complementary

	Affected by Cloud?	Resolution
<b>Passive Microwave</b> (AMSR-E)	No	Coarse
<b>VIS/IR</b> (MODIS)	Yes	Fine

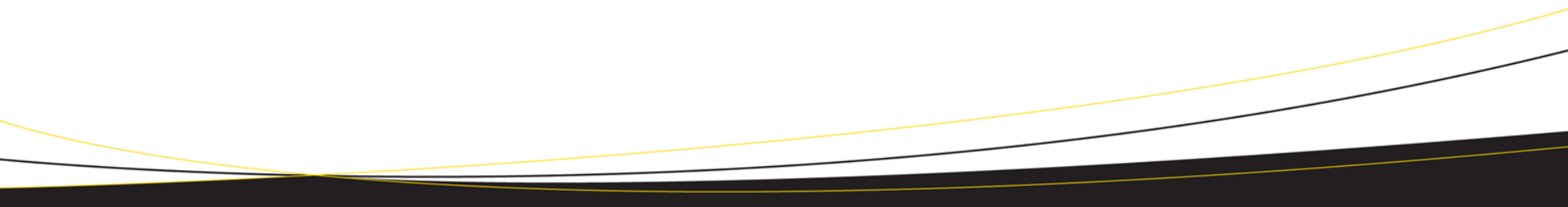
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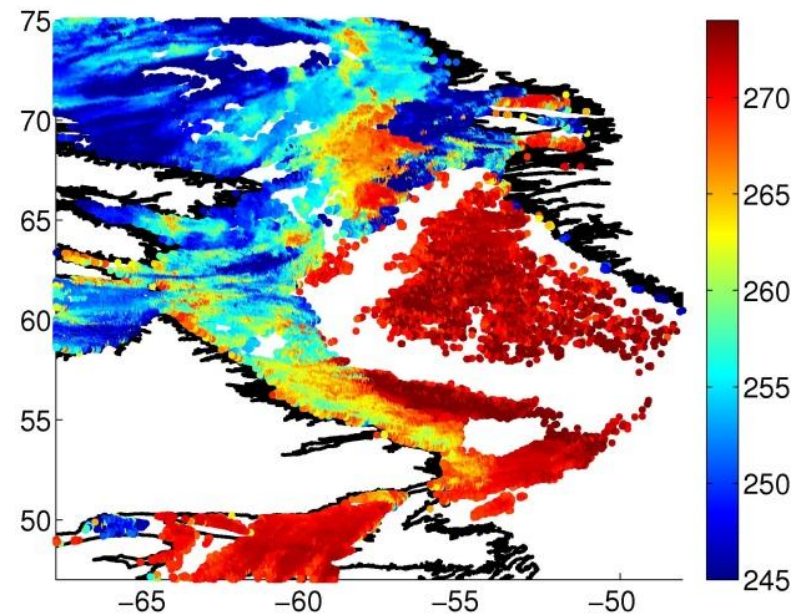
# Method Overview

1. **Generation:** Generate continuous surface temperature map.
2. **Estimation:** Estimate ice thickness from surface temperature.



# Step 1: Generation

- **Goal:** continuous surface temperature map
- **Idea:** regard cloud-cover pixels as noise
- Multi-modality Guided Variational (MGV) model
  - Total variation
  - Polarization ratio (AMSR-E)



# Aside: Total Variation

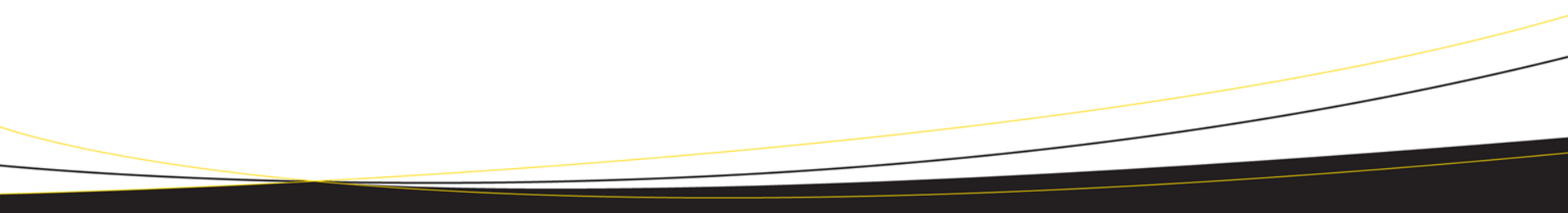
- Consider least-squares
  - Infinite number of solutions: how to interpolate missing data?
  - $\hat{s} = \operatorname{argmin} ||\hat{s} - s||_2$
  - But  $s$  is incomplete!
- Total variation assumes piecewise smoothness
  - Realistic assumption for ice transitions
  - $\hat{s} = \operatorname{argmin} \alpha ||\hat{s} - s||_2 + \beta \sum_i |\hat{s}_i - \hat{s}_{i+1}|$

# Aside: Polarization Ratio

- Normalized difference between polarization brightness temperatures:

$$PR(\nu) = \frac{B_V(\nu) - B_H(\nu)}{B_V(\nu) + B_H(\nu)}$$

- Related to ice thickness





# Step 1: Generation

- Represent sparse info as sampled from a continuous map:

$$\begin{bmatrix} \mathbf{m}_0 \\ \mathbf{m}_1 \\ \mathbf{m}_2 \\ \mathbf{m}_3 \end{bmatrix} = \begin{bmatrix} C_0 \\ C_1 \\ C_2 \\ C_3 \end{bmatrix} \begin{bmatrix} \mathbf{z}_0 \\ \mathbf{z}_1 \\ \mathbf{z}_2 \\ \mathbf{z}_3 \end{bmatrix}$$

MODIS

AMSR-E

$\mathbf{m}_0$  – sparse MODIS surface temperature

$\mathbf{z}_0$  – continuous surface temperature

$\mathbf{m}_{1,2,3}$  – PR for lowest 3 AMSR-E frequencies

$\mathbf{z}_{1,2,3}$  – continuous PR

$C_i$  – observation matrix

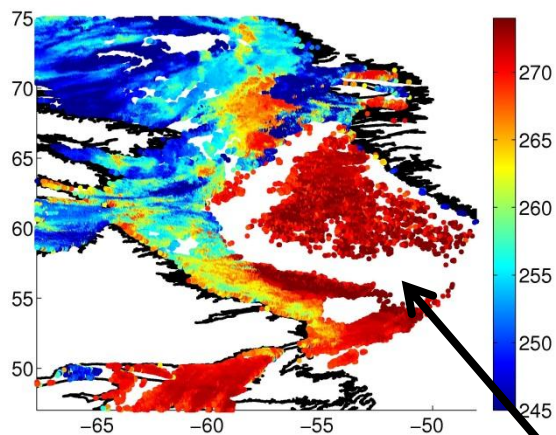
# Step 1: Generation

- Use MGV to find  $\mathbf{z}_0$ 
  - Fit temperature map with least-squares
  - Use spatial variability of AMSR-E PRs

$$\hat{z}_o = \operatorname{argmin} \left[ \alpha \|m_o - C_o \hat{z}_o\|_2 + \beta \sum_j \sum_{k \in N(j)} \exp(-\lambda_s \|j - k\|_2) \underbrace{\sum_{i=0}^3 \exp(-\lambda_i \|z_i(j) - z_i(k)\|)}_{\text{AMSR-E data}} |\hat{z}_o(j) - \hat{z}_o(k)| \right]$$

- Sum over 3 lowest AMSR-E frequencies

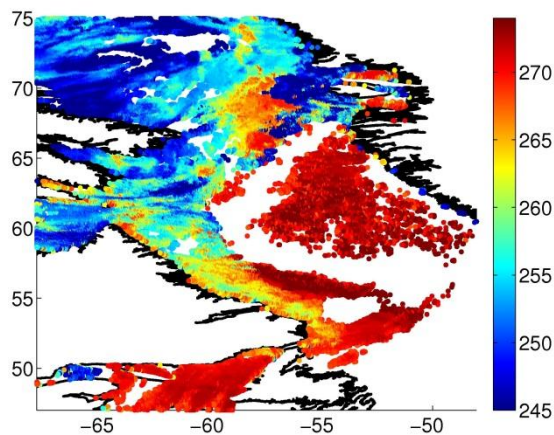
# Step 1: Generation



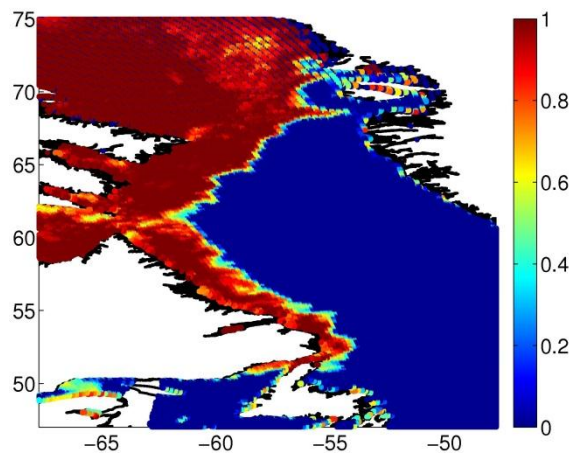
Swath data  
(MODIS)

Cloud cover

# Step 1: Generation



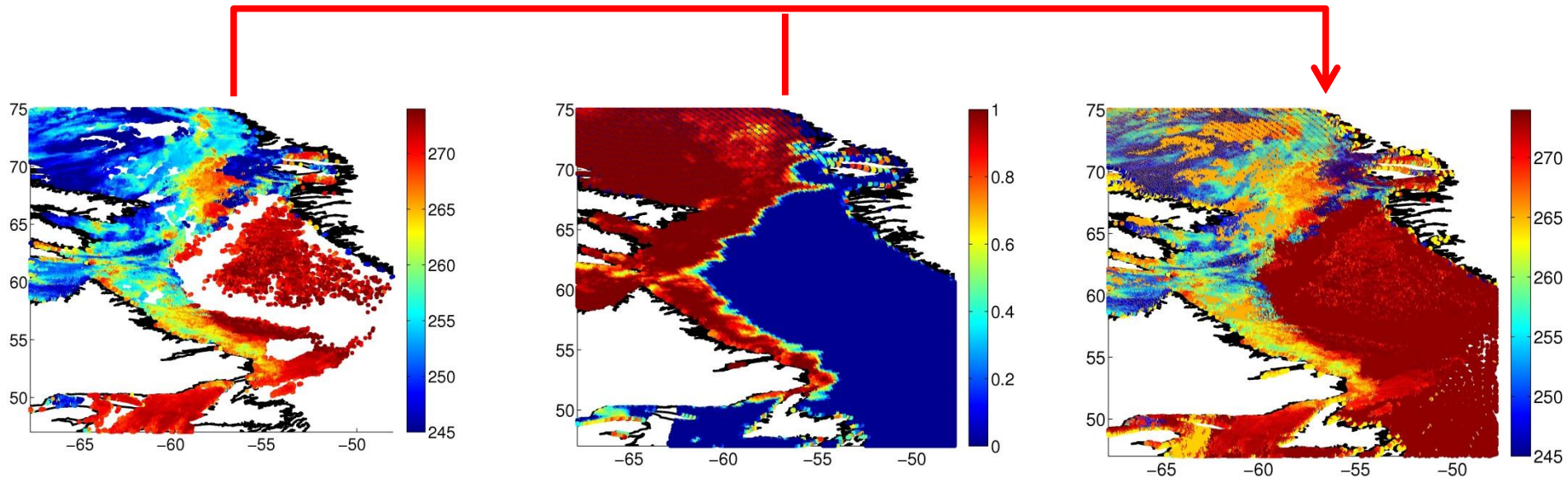
Swath data  
(MODIS)



Ice concentration (IC)  
from AMSR-E

$$T_s = 265 * IC + 274 * (1 - IC)$$

# Step 1: Generation



Swath data  
(MODIS)

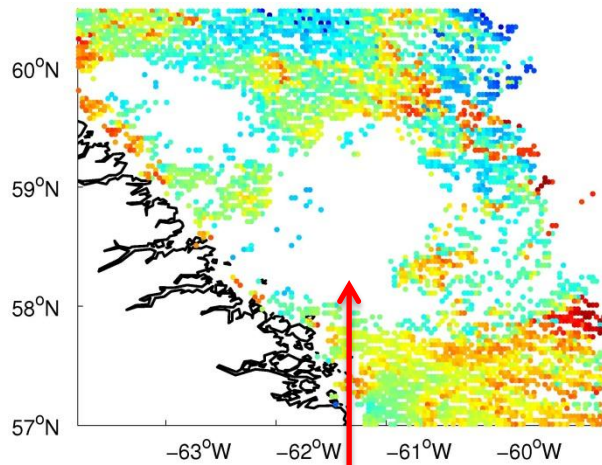
Ice concentration (IC)  
from AMSR-E

Complete temperature  
image

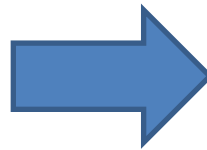
$$T_s = 265 * IC + 274 * (1 - IC)$$

# Example: Surface Temperature

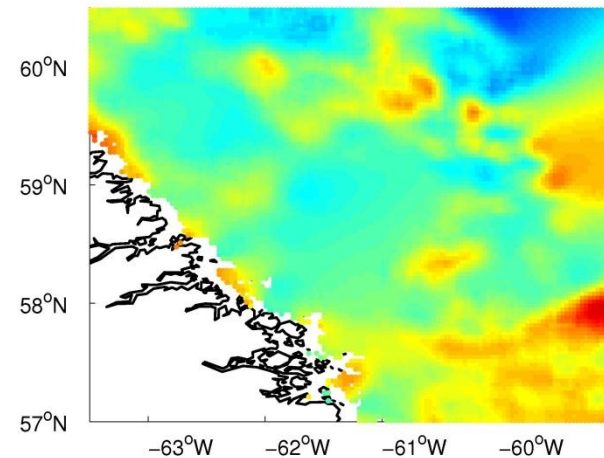
MODIS Swath data



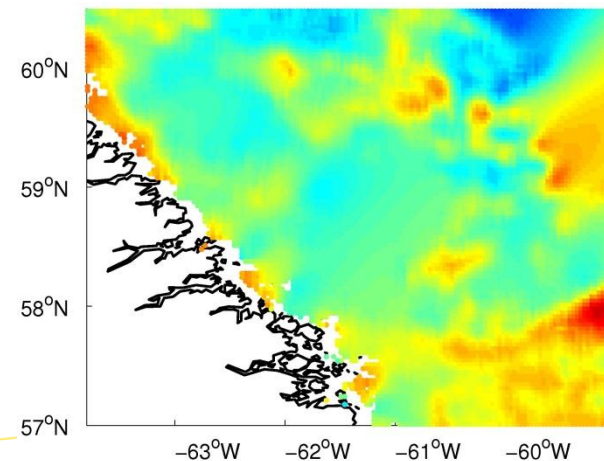
Cloud covered pixels!



TV (MODIS only)



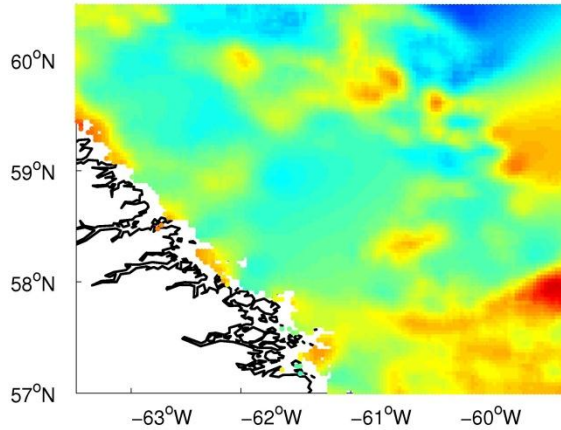
MGV (MODIS+AMSR-E)



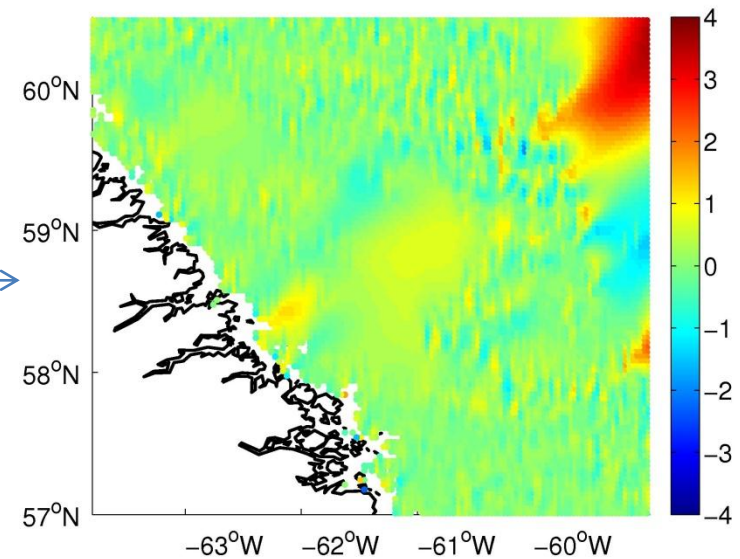


# Example: Surface Temperature

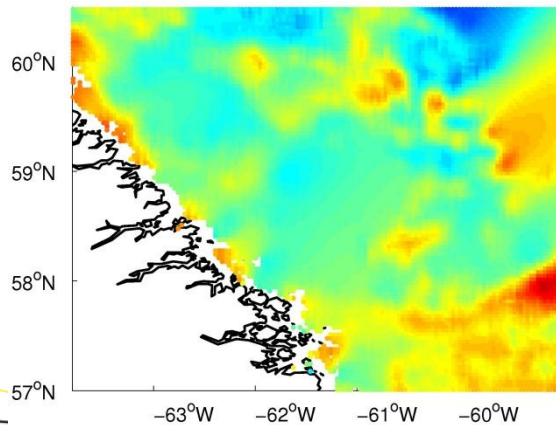
TV (MODIS only)



MGV – TV



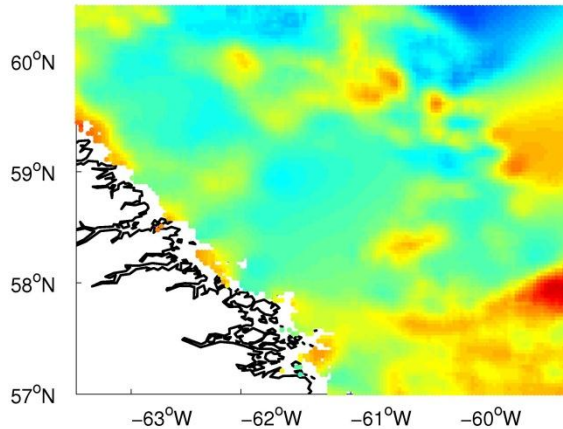
MGV (MODIS+AMSRE)





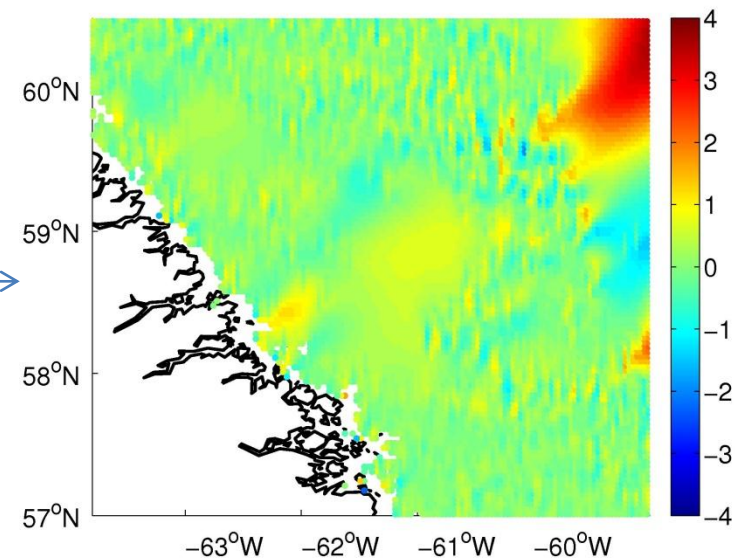
# Example: Surface Temperature

TV (MODIS only)

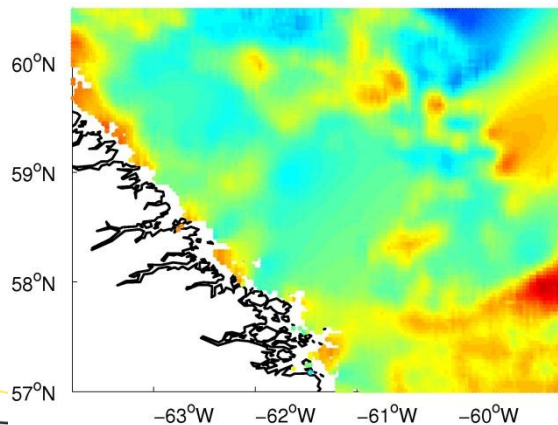


$2^\circ \approx 10\text{cm}$  [Wang et al. 2010]

MGV – TV

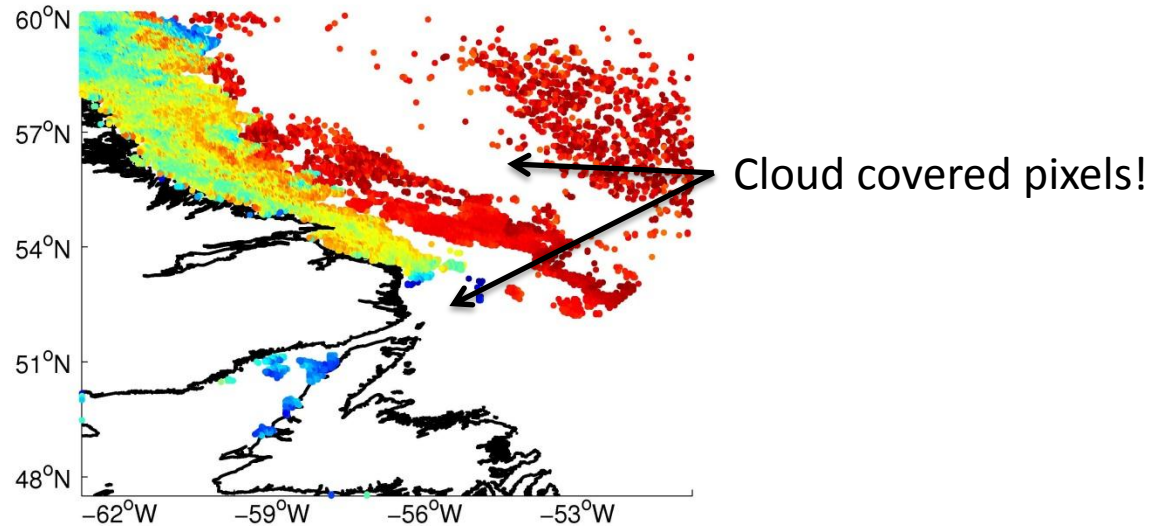


MGV (MODIS+AMSRE)

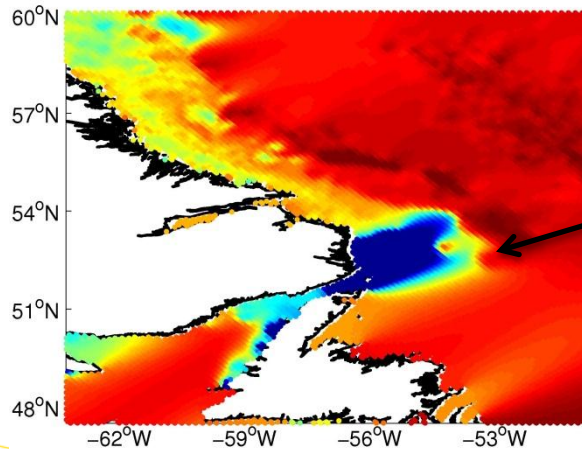


# Example: Surface Temperature

Swath data

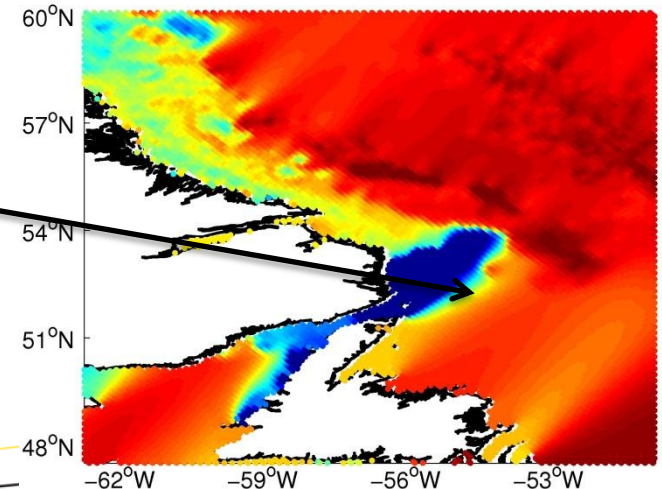


TV (MODIS only)



MGV more realistic

MGV (MODIS+AMSR-E)




# Step 2: Estimation

- Given surface temperature, solve heat balance equation:


$$F_{long}^{\beta} - F_{long}^{\gamma} + F_{sens} + F_{lat} + F_c = 0$$



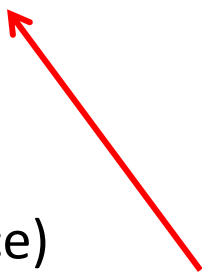
Longwave radiation



Sensible heat flux  
( $\Delta T$  air & ice)



Latent heat flux  
( $\Delta$ vapour over ice)



Conduction  
(transfer through ice)

## Step 2: Estimation

- Given surface temperature, solve heat balance equation:

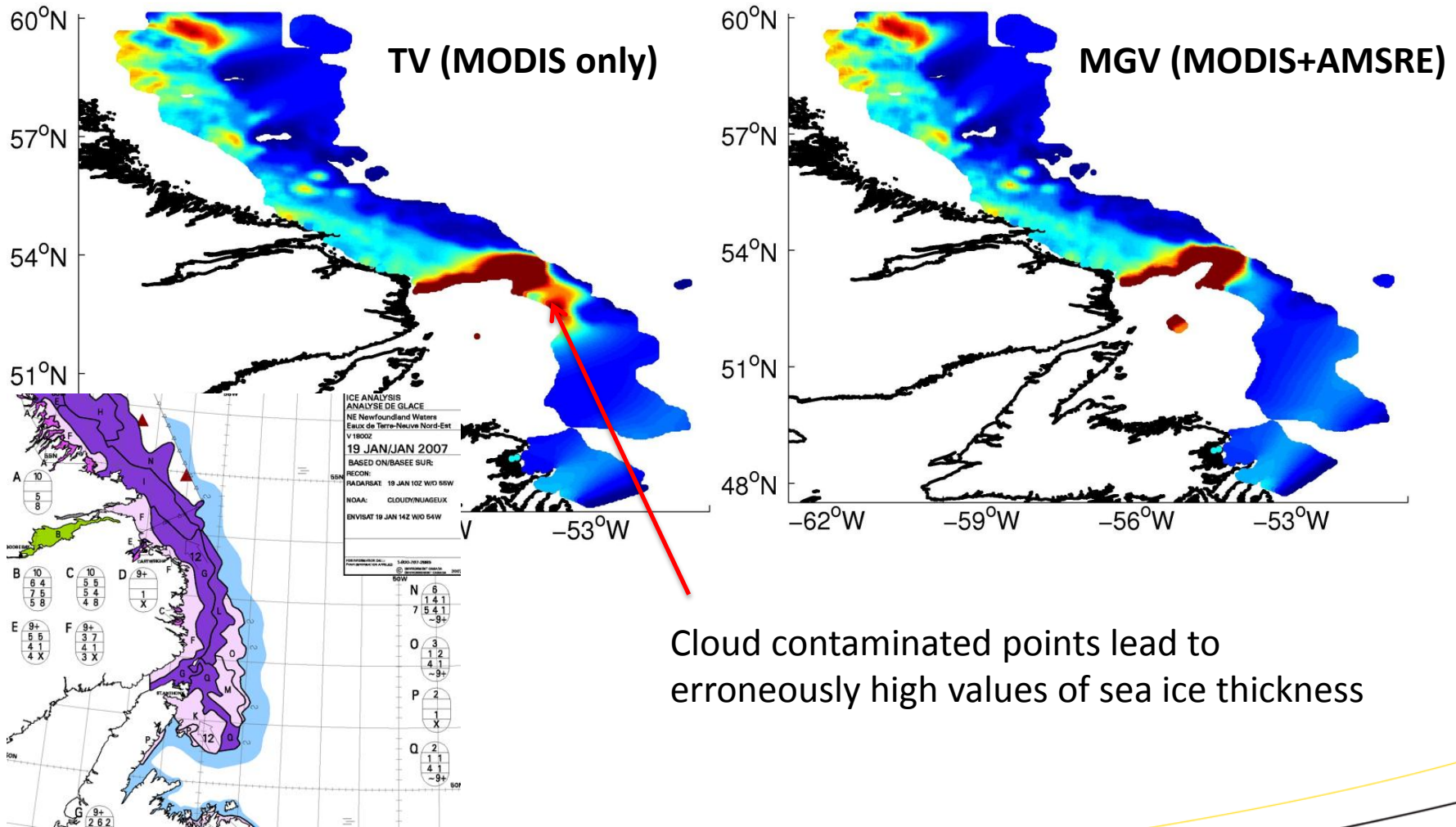
$$F_{long}^{\beta} - F_{long}^{\gamma} + F_{sens} + F_{lat} + F_c = 0$$

- Most are functions of surface temperature ( $z_0$ )
- $F_c = \frac{k(T_s - T_w)}{h}$ , where is  $h$  ice thickness
  - Given surface temperature, solve for  $h$ !

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# Results





# Comparison with Ice Charts

- Surface temperature and ice thickness calculated for each day from Jan 1 2007 – Feb 28 2007

	Absolute difference in [m]		
<b>Ice chart Thickness (m)</b>	<b>Swath data</b>	<b>MODIS TV</b>	<b>MODIS+AMSR-E MGV</b>
<b>0-0.1</b>	0.1274	0.1225	0.1198
<b>0.1-0.15</b>	0.0820	0.0764	0.0774
<b>0.15-0.30</b>	0.1019	0.1029	0.1029
<b>&gt; 0.30</b>	0.2130	0.2115	0.2094
<b>Number of points</b>	5242	6753	6711



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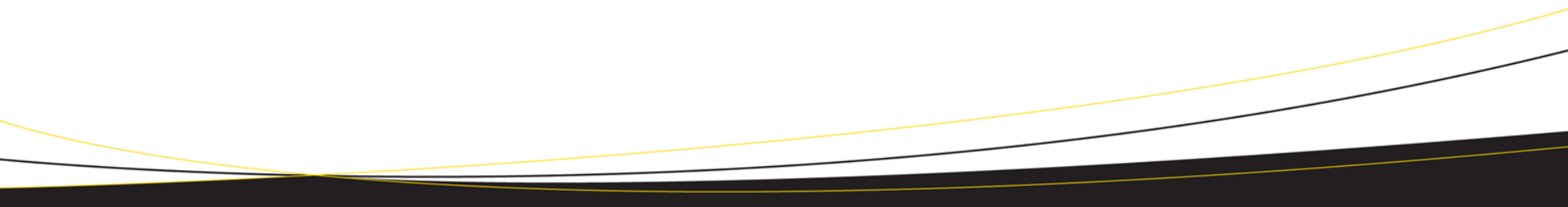
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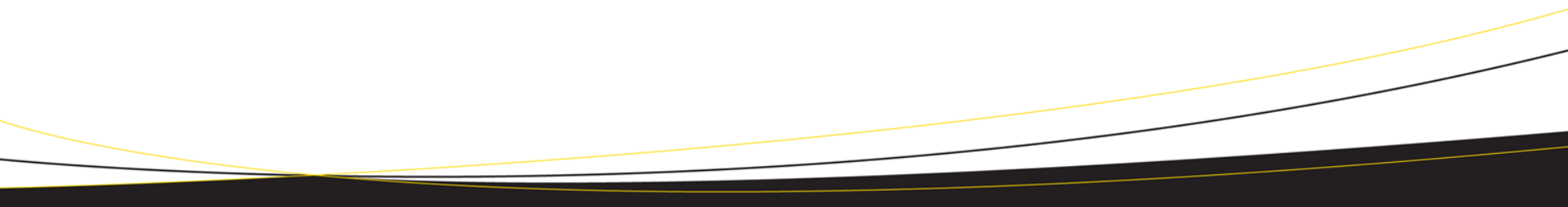
# Conclusions

- MGVI produced realistic surface temperature estimates in regions with cloud cover.
- However, method can also spread the influence of a cloud contaminated pixels.
- MGVI accuracy in cloud covered pixels attains base accuracy of visible pixels.



# Future Work

- Limit the spread of information in a local region to avoid unrealistic results.
- Automatic parameter selection



# Acknowledgements

- Data Sources:
  - Ice charts provide by the Canadian Ice Service
  - MODIS data – MOD product NSIDC
  - AMSR-E brightness temperatures – NSIDC
  - AMSR-E sea ice concentration – NSIDC
- Funding provided by the National Science and Engineering Research Council of Canada

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# Thank You!

Comments/Questions/Feedback:

[ramelard@uwaterloo.ca](mailto:ramelard@uwaterloo.ca)

<http://vip.uwaterloo.ca>



# Comparison with Ice Chart – QC

<b>Ice chart Thickness (m)</b>	<b>Swath data</b>	<b>MODIS TVD</b>	<b>MODIS+AMSR-E MGV</b>
0-0.1	0.0469	0.0456	0.0444
0.1-0.15	0.0622	0.0559	0.0558
0.15-0.30	0.0718	0.0710	0.0726
> 0.30	0.1248	0.1248	0.1232
Number of points	3119	4146	4086