

# Physics-based Control of Energy Systems Ranging from Smart Buildings and Power Grid to Smart Hybrid Electric Vehicles

**Mahdi Shahbakhti**

Director of Energy Mechatronics Laboratory  
Associate Professor of Mech. Eng.

# Outline

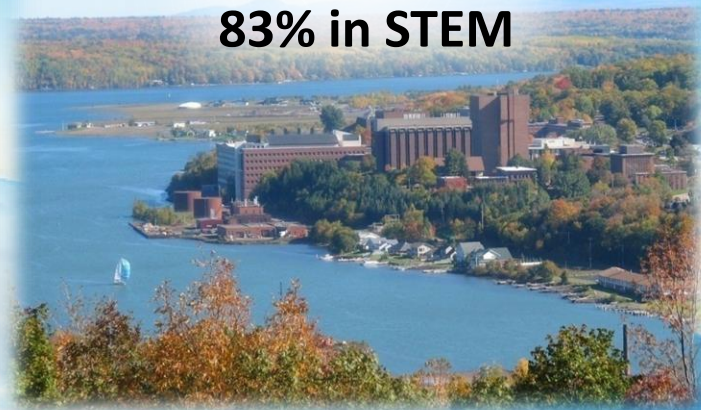
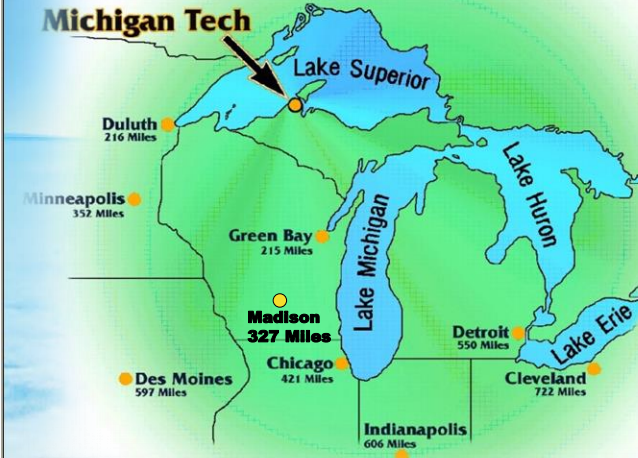


- About Michigan Tech and Me!
- Control of Building Energy Systems
- Control of Automotive Energy Systems

**Part I:  
About Michigan  
Tech and me!**

# Michigan Tech

Student  
Enrollment 7000  
83% in STEM



ME  
UG: 1395  
Grad: 367

Civil &  
Geological & Mining  
Material Sci & Eng

ECE

ChemE







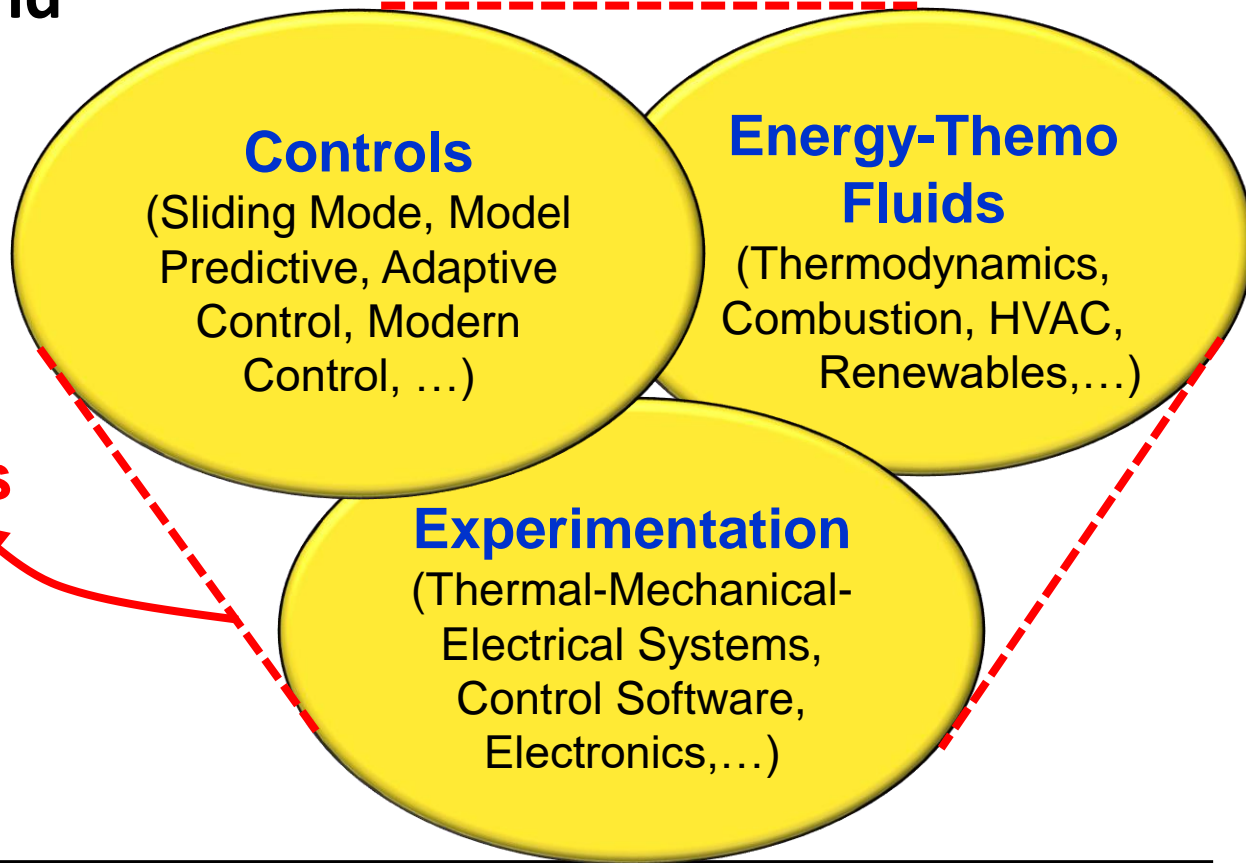
**AVERAGE SNOWFALL IS 5.3 METER!**

# Michigan Tech's Winter Carnival 2017



# My Background

**Energy  
Mechatronics**



# Research at Michigan Tech

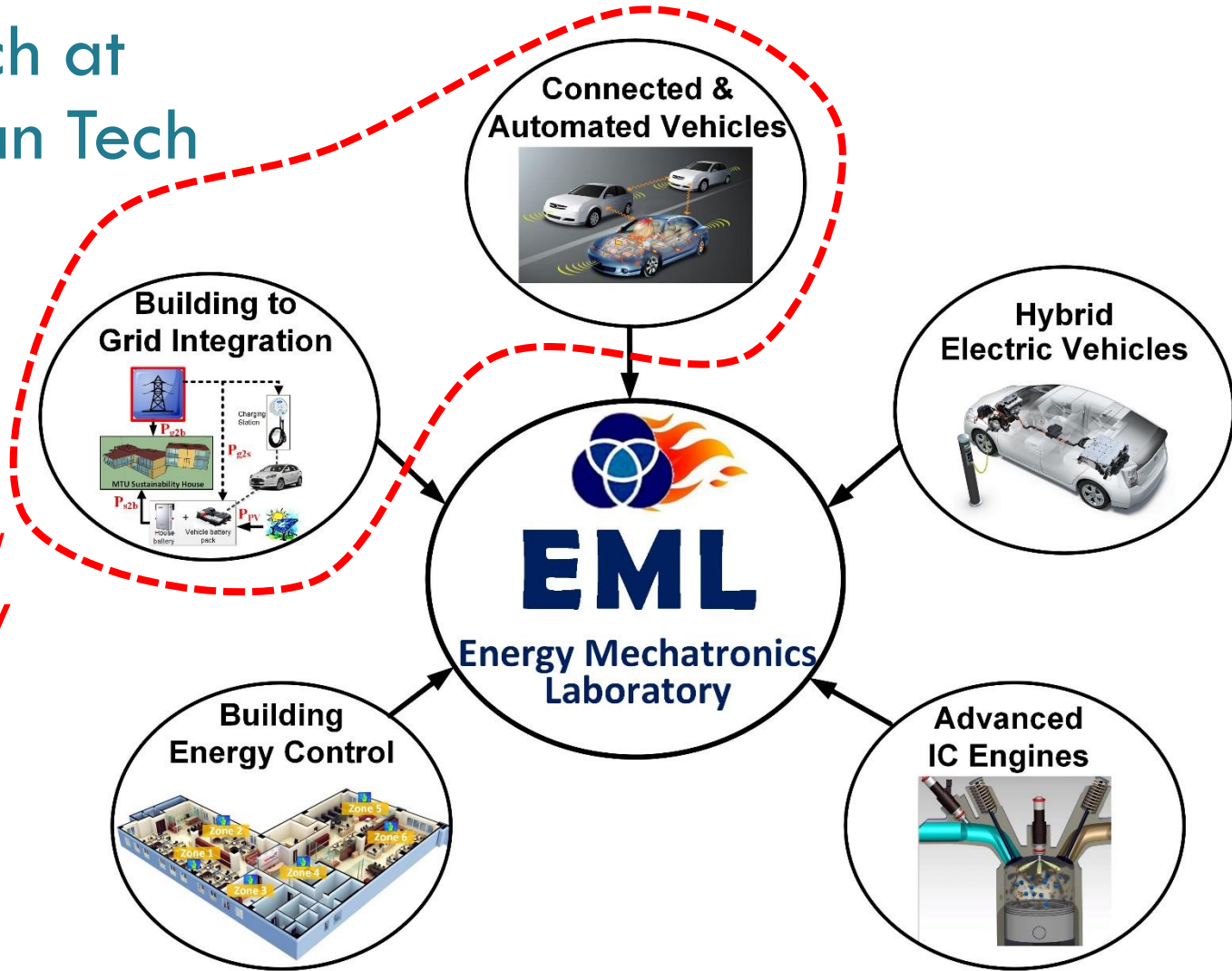


**Focus:** Increasing efficiency of energy systems through utilization of advanced control techniques

# Research at Michigan Tech



Smart City/  
Community





# EML Students

## □ Current: 6 PhD, 4 MS, 2 BS



Joe Tripp  
(PhD)



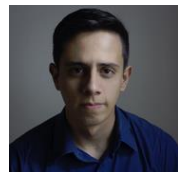
Behrouz Khoshbakht  
(PhD)



Lexy Krisztian  
(BS)



Drew Hanover  
(BS)



Vinicius Bonfochi  
(PhD)



Amir Khamenian  
(PhD)



Akshat A. Raut  
(MS)



Mayank Darji  
(MS)



Chethan R. Reddy  
(PhD)



Mohamed Toub  
(Visiting PhD)



Rajeshwar Yadav  
(MS)



Prithvi Reddy  
(MS)

## □ Graduated: 5 PhD, 12 MS



Dr. Ali Solouk



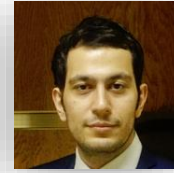
Dr. Meysam Razmara



Dr. Boopathi  
Mahadevan



Dr. Reza Amini



Dr. Mehran  
Bidarvatan



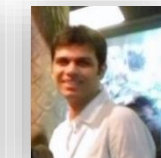
Madhura Paranjape  
(MS)



Deepak Kothari  
(MS)



Hrishikesh Saigaonkar  
(MS)



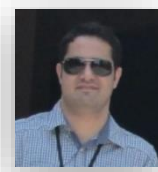
Vishal Thakkar  
(MS)



Nithin Teja Kondipati  
(MS)



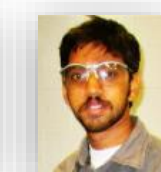
Jeremy Dobbs  
(MS)



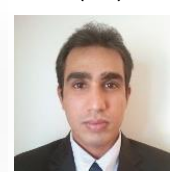
Kaveh Khodadadi  
(MS)



Mohammad Nazemi  
(MS)



Kaushik Kannan  
(MS)



Jayant Arora  
(MS)

**Part II:**  
**Control of building  
energy systems**

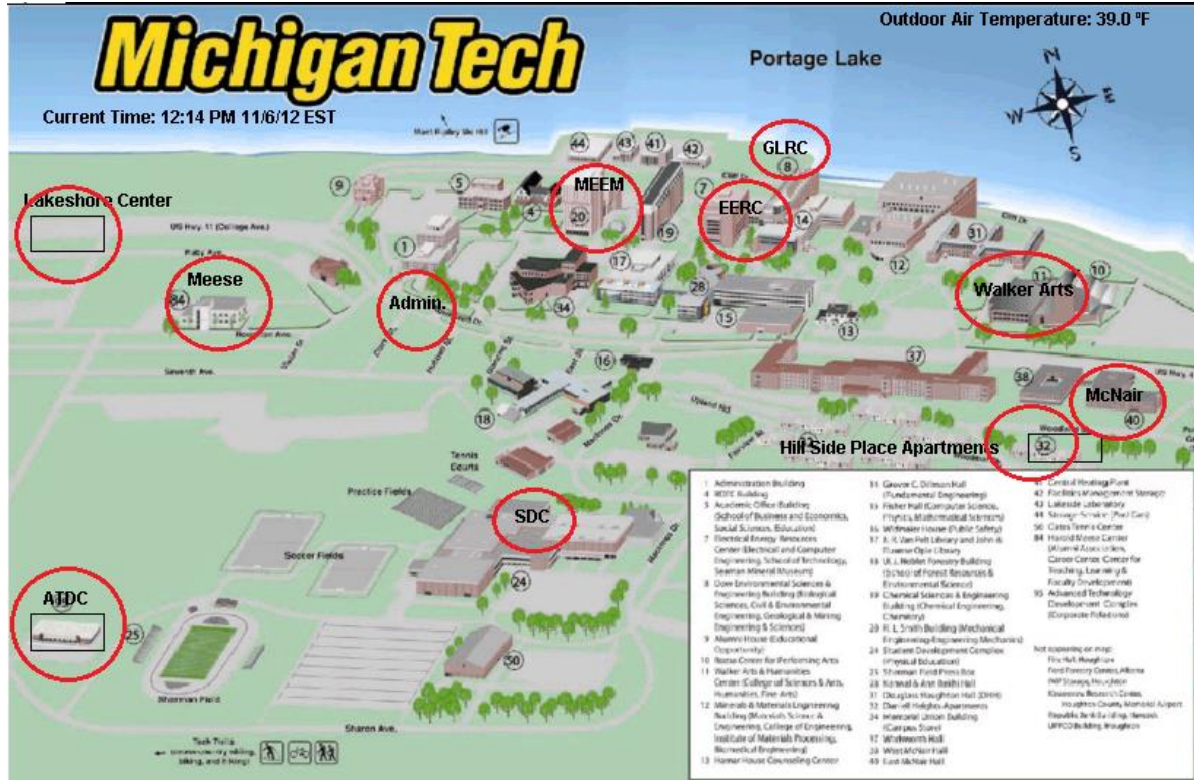
# Part II: Control of building energy systems



- Modeling of building energy systems
- Predictive control of building HVAC systems
- Building-to-grid optimization



# Building Research Test Bed



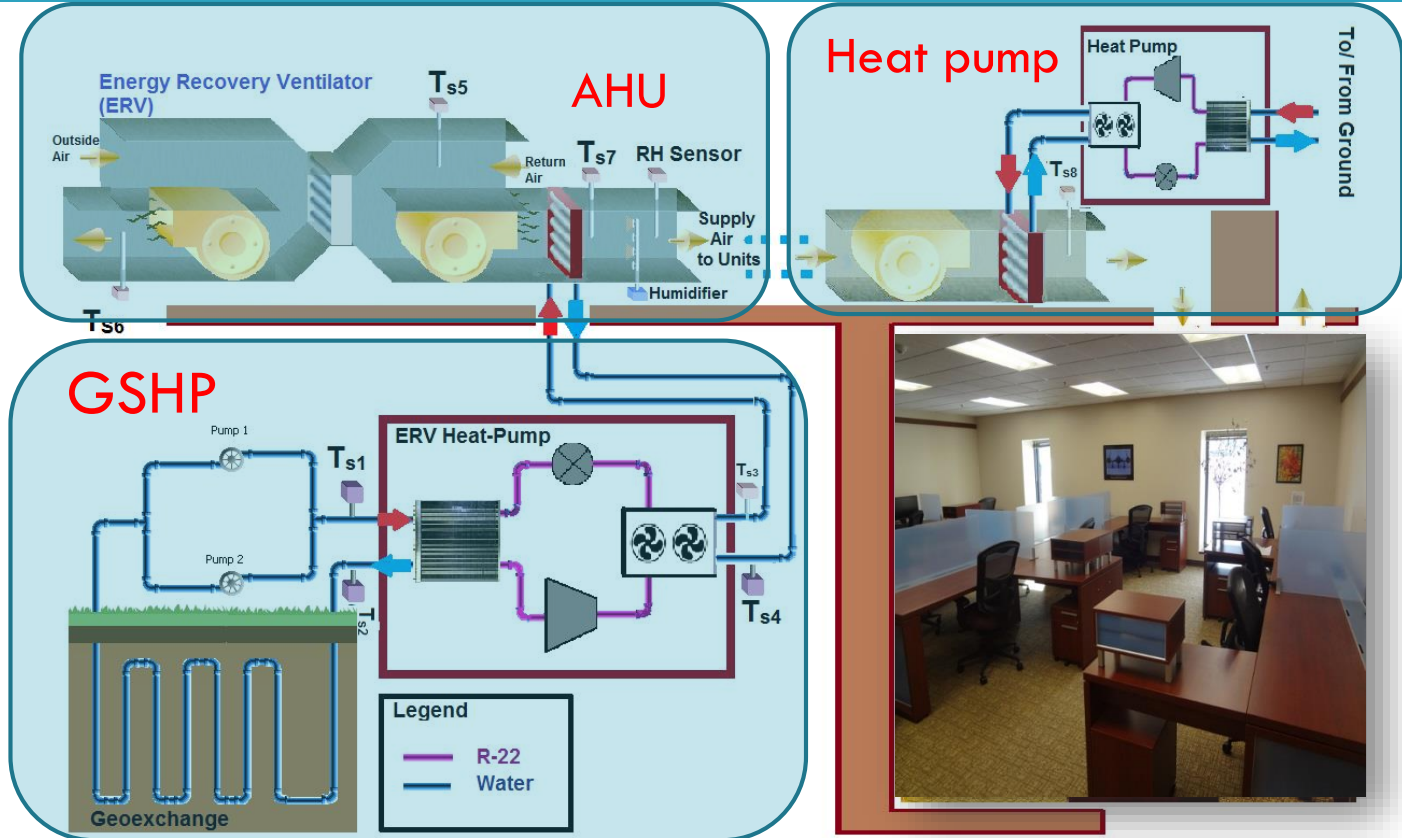
# HVAC System at Lakeshore Center

14



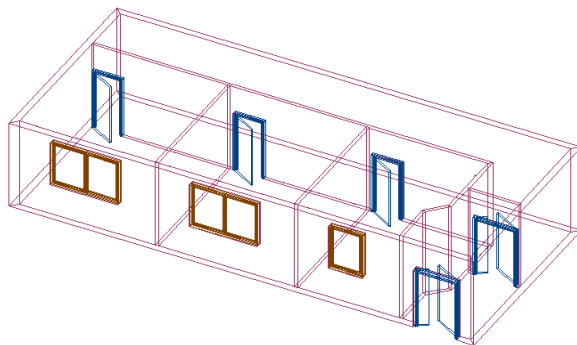
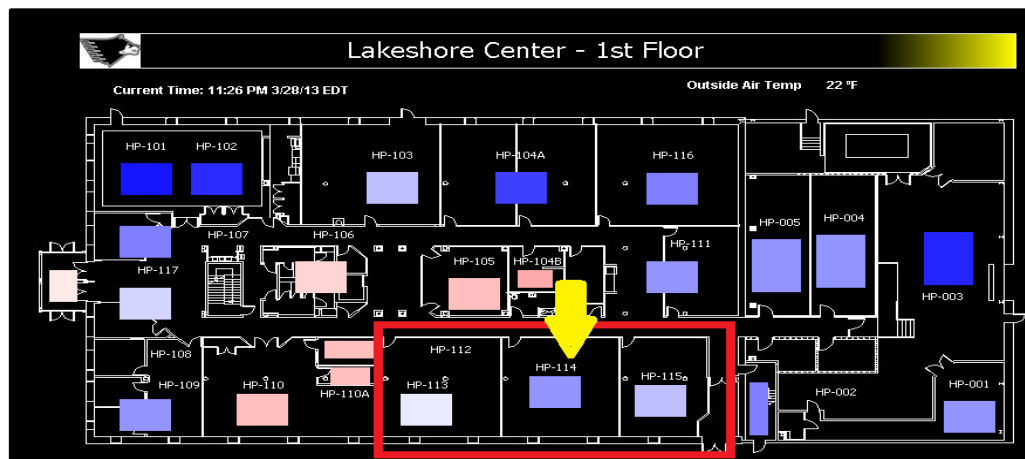
# HVAC System at Lakeshore Center

15



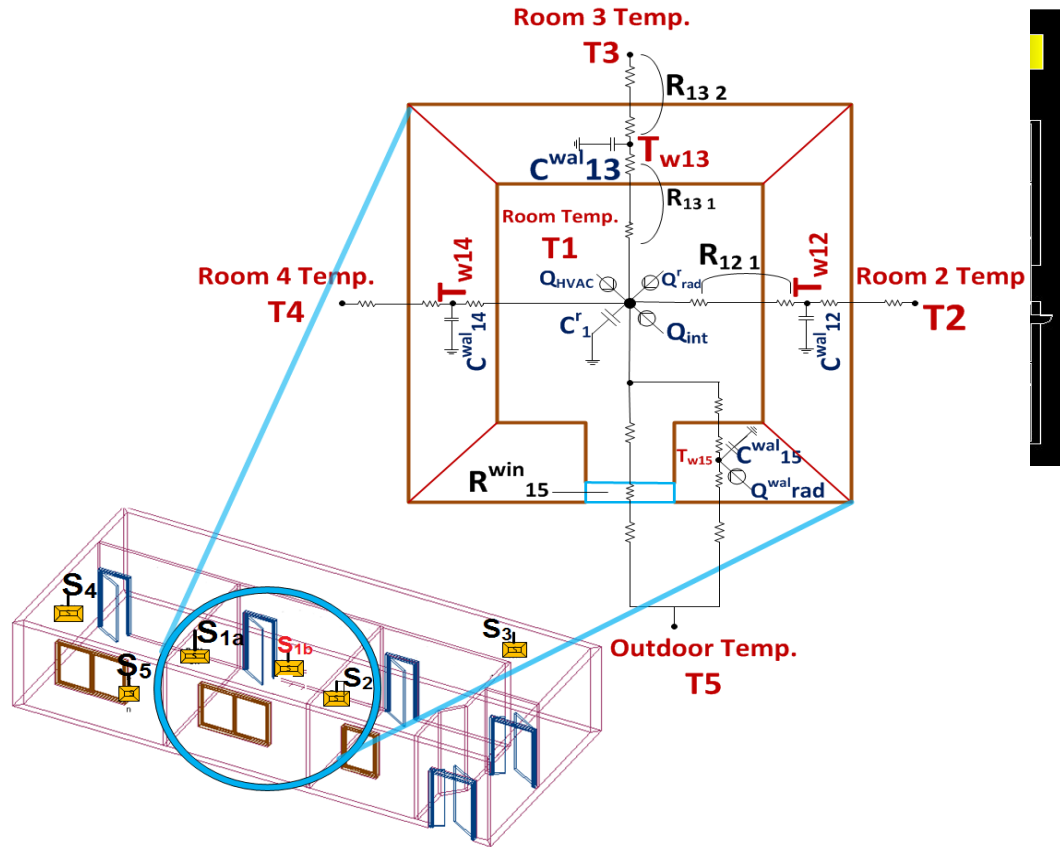
# Building Thermal Modeling-RC Model

16



# Building Thermal Modeling-RC Model

17



# Building Thermal Model

Energy balance for a **wall** node:

$$C_{i,j}^{w} \frac{dT_{i,j}^w}{dt} = \underbrace{\sum_{k \in \mathcal{N}_{i,j}^w} \frac{T_k^r - T_{i,j}^w}{R_{i,j}^k}}_{\text{Conduction \& convection}} + \underbrace{r_{i,j} \alpha_{i,j} A_{i,j}^w Q_{i,j}^{rad}}_{\text{Radiation}}$$

Conduction &  
convection

Radiation

Energy balance for a **room** node:

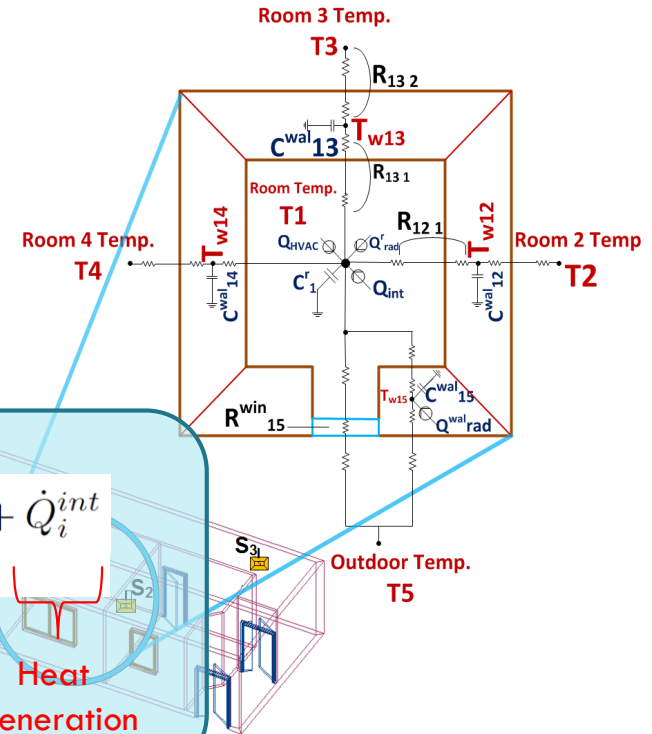
$$C_i^r \frac{dT_i^r}{dt} = \underbrace{\sum_{k \in \mathcal{N}_i^r} \frac{T_k^r - T_i^r}{R_{i,j}^k}}_{\text{Conduction \& convection}} + \underbrace{\dot{m}_i^r \bar{c}_p (T_i^s - T_i^r)}_{\text{HVAC heat flow}} + \underbrace{\pi_i \tau_i^w A_i^{win} Q_i^{rad}}_{\text{Radiation}} + \underbrace{\dot{Q}_i^{int}}_{\text{Heat generation}}$$

Conduction &  
convection

HVAC heat  
flow

Radiation

Heat  
generation

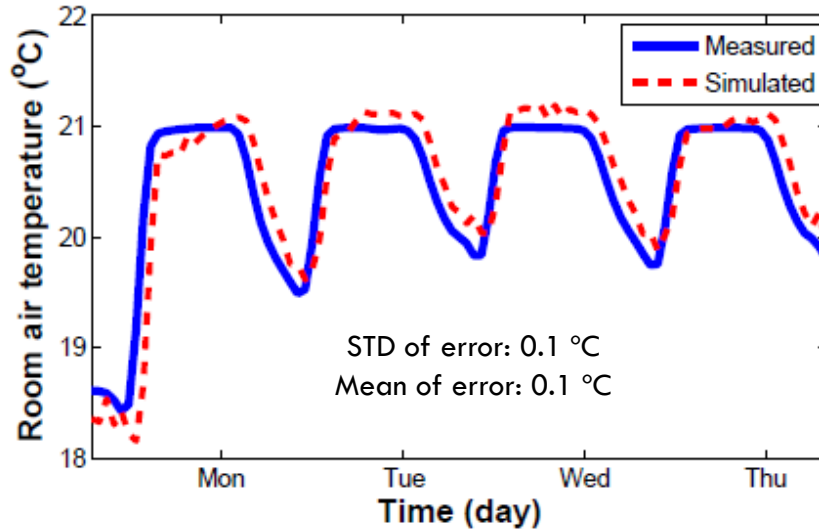


# Building Thermal Model

19

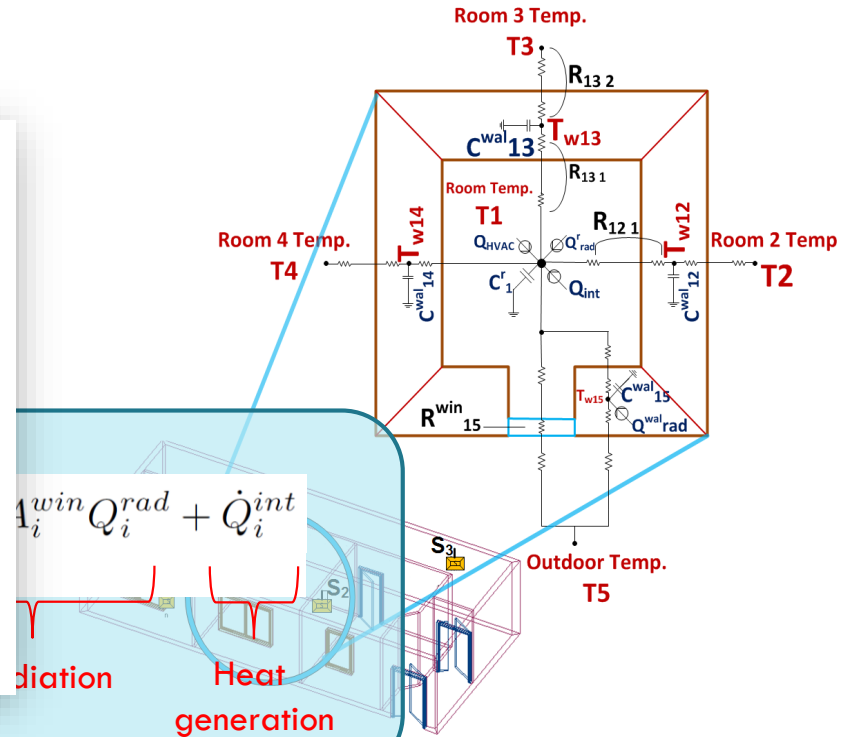
Energy balance for a **wall** node:

$$C_{wal}^w \frac{dT_{i,j}^w}{dt} = \sum \frac{T_k^r - T_{i,j}^w}{R_{k,i,j}} + r_{i,i} \alpha_{i,i} A_{i,i} Q_{rad}$$



convection

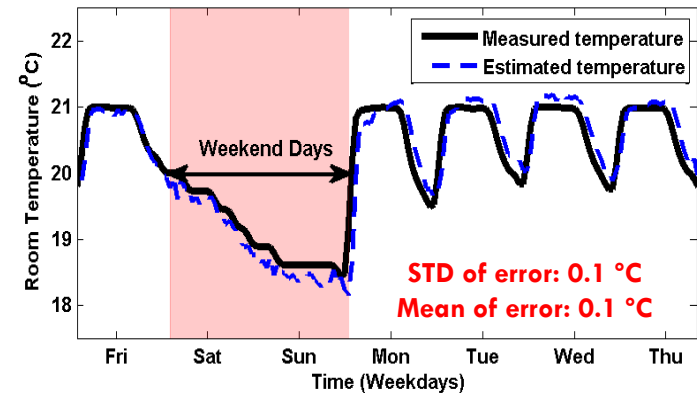
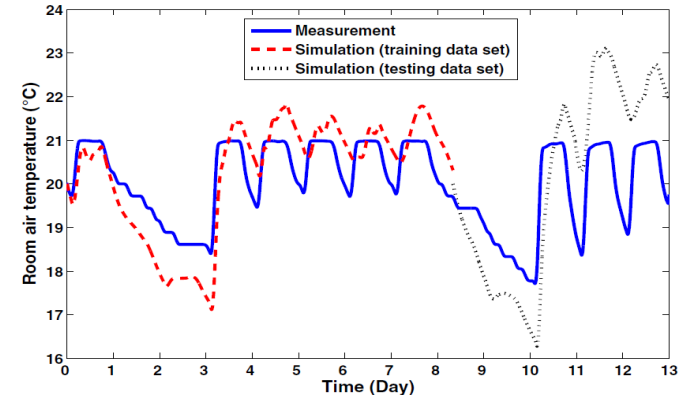
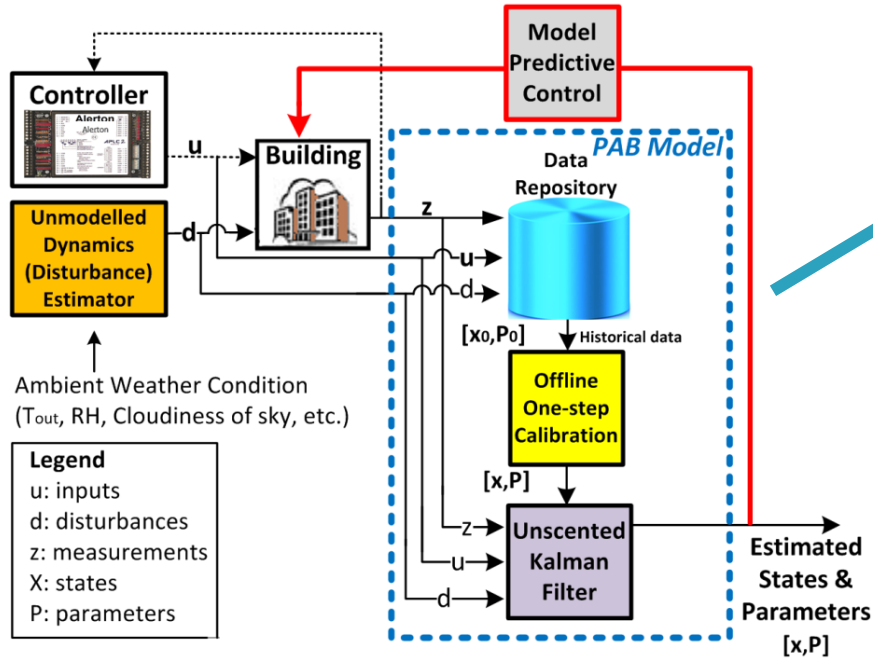
flow





# Parameter Adaptive Building (PAB) Model

20



M. Maasoumy, M. Shahbakhti, et. al, " Handling Model Uncertainties in Model Predictive Control for Energy Efficient Buildings ", *J. of Energy and Buildings*, 2014.



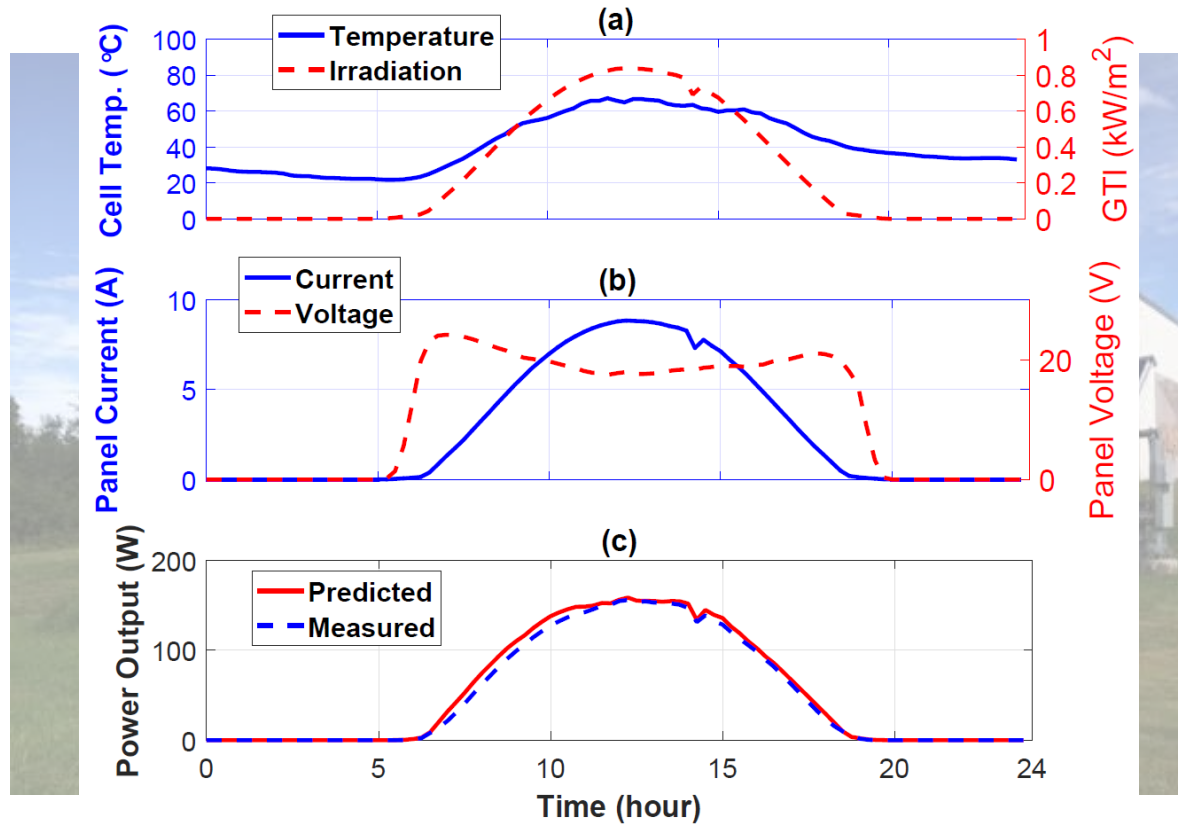
# Modeling:

## Photovoltaic Single Diode Modeling



## Photovoltaic Single Diode Modeling

22



# Exergy vs. Energy

- The **1<sup>st</sup> Law** of Thermodynamics is related to energy conservation
- The **2<sup>nd</sup> Law** of Thermodynamics concerns entropy generation and irreversibility which cause deficiency
- **Exergy** is based on the 1<sup>st</sup> and 2<sup>nd</sup> Laws of Thermodynamics and is relevant to quality of energy
- **Exergy** is defined as the maximum useful work during a process in a specific environment
- **Exergy** is a more precise metric compared to energy to evaluate energy systems. (e.g. HVAC systems, IC engines, power-plants, etc.)

# Exergy vs. Energy

24

- The 1<sup>st</sup> Law of Thermodynamics is related to energy conservation
- The 2<sup>nd</sup> Law of Thermodynamics concerns irreversibility, which is because of efficiency
- **Exergy** is based on the 1<sup>st</sup> and 2<sup>nd</sup> Law to quantify the quality of energy
- **Exergy** is the maximum use of energy in an environment
- **Exergy** is a more precise metric comparing systems. (e.g. HVAC systems, IC engines)

$$E_1 = m_w u_w = 42 \text{ kJ}$$

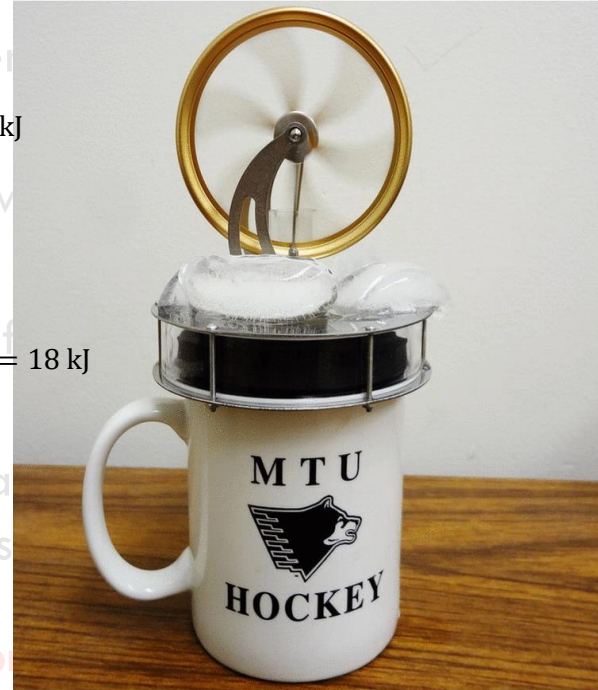
$$X_1 = m_w [(u_w - u_0) + P_0(v_w - v_0) - T_0(s_w - s_0)] = 1 \text{ kJ}$$

After adding ice

$$E_2 = m_w u_w = 42 \text{ kJ}$$

$$X_2 = m_w [(u_w - u'_0) + P'_0(v_w - v'_0) - T'_0(s_w - s'_0)] = 18 \text{ kJ}$$

Exergy is a more p



relevant

a specific

energy

# Building Exergy Model

25

$\dot{X}_{dest_i}^r = \overbrace{\sum_{k \in N_i^r} (1 - \frac{T_0}{T_i^r}) \dot{Q}_i^{H.T.,k}}^{\dot{X}_i^{H.T.,r}} - \dot{W}_i^r + \sum_{in} \dot{m}_i \psi - \sum_{out} \dot{m}_i^r \psi - \frac{dX_i^r}{dt}$

$\dot{X}_i^{H.T.,r} = \sum_{k \in N_i^r} (1 - \frac{T_0}{T_i^r}) (\frac{T^k - T_i^r}{R_{i,j}^k})$

$\psi = (h - h_0) - T_0(s - s_0) + \frac{V^2}{2} + gz$

$\frac{dX_i^r}{dt} = m_i^{room} (\frac{dh}{dt} - T_0 \frac{ds}{dt})$

$\dot{X}_{dest_i}^r[k] = \sum_{k \in N_i^r} (1 - \frac{T_0[k]}{T_k^r[k]}) (\frac{T_k^r[k] - T_i^r[k]}{R_{i,j}^k}) +$   
 $\dot{m}_i^r[k] [\bar{c}_p (T_i^s[k] - T_i^r[k]) - T_0[k] \bar{c}_p \ln(\frac{T_i^s[k]}{T_i^r[k]})]$   
 $+ \frac{m_i^{room}}{T_{sample}} [\bar{c}_p (T_i^r[k] - T_i^r[k-1])$   
 $- T_0[k] \bar{c}_p \ln \frac{T_i^r[k]}{T_i^r[k-1]}]$

$\Delta h = \int \bar{c}_p dT$   
 $\Delta s = \int_1^2 \bar{c}_v \frac{dT}{T} + R \cdot \ln \frac{v_2}{v_1}$

# Building Thermal and Exergy Model

$$d_t = g(Q_{rad_i}(t), \dot{Q}_{int}(t), T_{out}(t))$$

$$\dot{x}_t = f(x_t, u_t, d_t, t)$$

$$y_t = Cx_t$$

Nonlinear System Dynamics  
(Bilinear due to Inputs multiplication)

Discretized System Dynamics

$$x_{k+1} = \begin{cases} A_d x_k + B_d u_k + E_d d_k & k \in [5, 6, \dots, 18] \\ A_n x_k + B_n u_k + E_n d_k & k \in [19, \dots, 24, 1, \dots, 5] \end{cases}$$

**Input:** Supply air temperature

**States:** Room air temperature & neighboring zones temperature

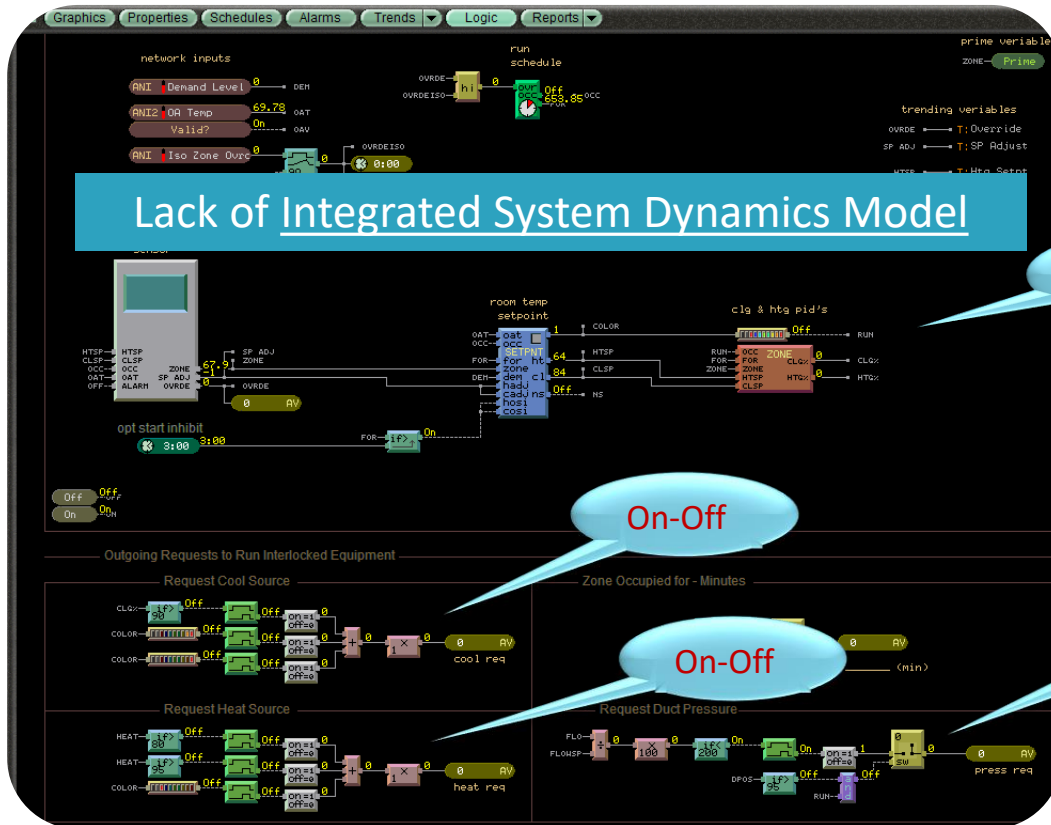
**Output:** Room air temperature

# Part II: Control of building energy systems

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- Modeling of building energy systems
- **Predictive control of building HVAC systems**
- Building-to-grid optimization

# Existing HVAC Control Logics



Lack of Integrated System Dynamics Model

PID

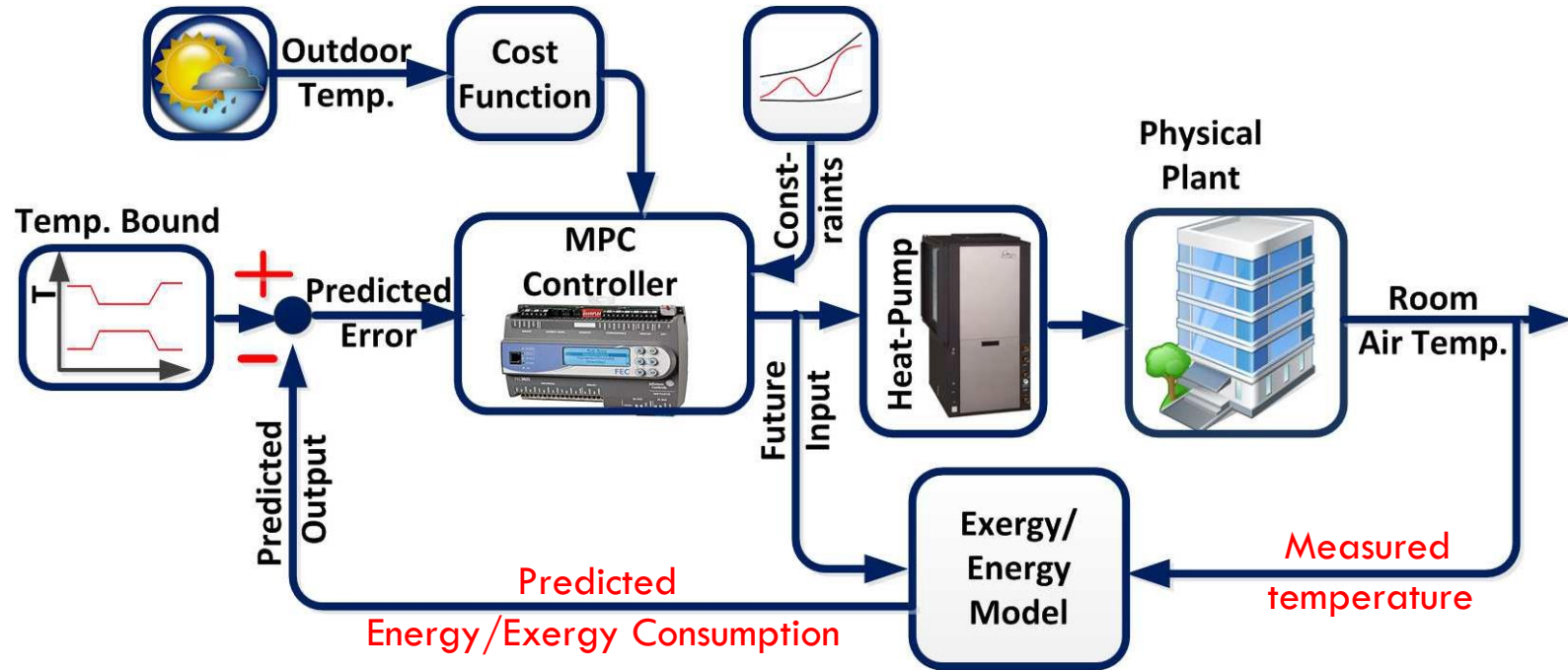
On-Off

On-Off

On-Off



# Model Predictive Control of HVAC Systems



# MPC formulation

Controllers:  $\left\{ \begin{array}{l} \text{Rule-based controller (RBC)} \\ \text{Energy-based MPC (EMPC)} \\ \text{Exergy-based MPC (XMPC)} \end{array} \right.$

**EMPC:**  $\min_{U_t, \bar{\epsilon}, \underline{\epsilon}} \{ |I_e|_1 + \rho(|\bar{\epsilon}_t|_1 + |\underline{\epsilon}_t|_1) \}$

subject to:

$$x_{t+k+1|t} = Ax_{t+k|t} + Bu_{t+k|t} + Ed_{t+k|t}$$

$$y_{t+k|t} = Cx_{t+k|t}$$

$$\underline{U}_{t+k|t} \leq u_{t+k|t} \leq \bar{U}$$

$$\delta \underline{U} \leq u_{t+k+1|t} - u_{t+k|t} \leq \delta \bar{U}$$

$$\underline{T}_{t+k|t} - \underline{\epsilon}_{t+k|t} \leq y_{t+k|t} \leq \bar{T}_{t+k|t} + \bar{\epsilon}_{t+k|t}$$

$$\underline{\epsilon}_{t+k|t}, \bar{\epsilon}_{t+k|t} \geq 0$$

$$I_e = \int_{t=1}^{24} [P_c(t) + P_h(t) + P_f(t)] dt$$

$$P_c(t) = \dot{m}_i^r(t) \bar{c}_p [T_{r_i}(t) - T_c(t)]$$

$$P_h(t) = \dot{m}_i^r(t) \bar{c}_p [T_h(t) - T_{r_i}(t)]$$

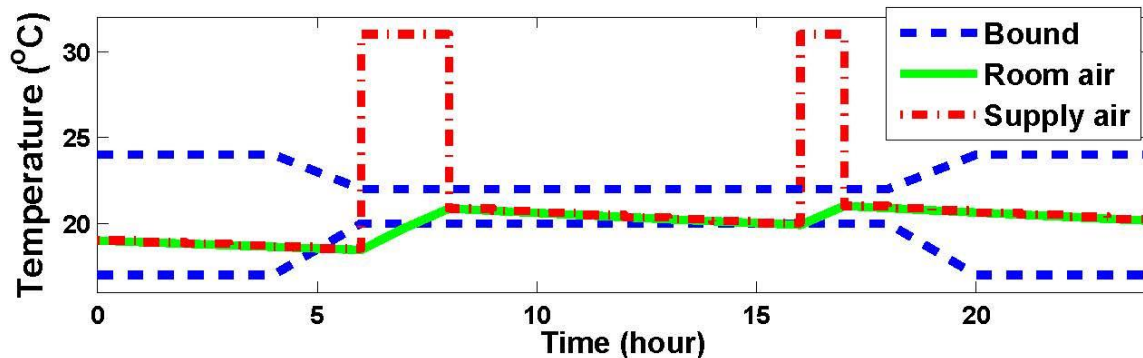
$$P_f(t) = \alpha (\dot{m}_i^r)^3$$

**XMPC:**  $\min_{U_t, \bar{\epsilon}, \underline{\epsilon}} \{ \dot{X}_{dest_t} + \rho(|\bar{\epsilon}_t|_1 + |\underline{\epsilon}_t|_1) \}$

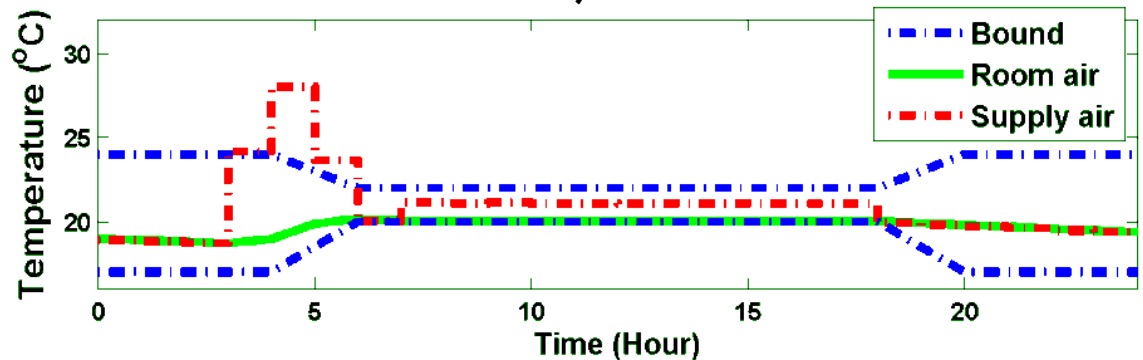
# Results: Rule-Based Control vs. MPC

31

## a) RBC

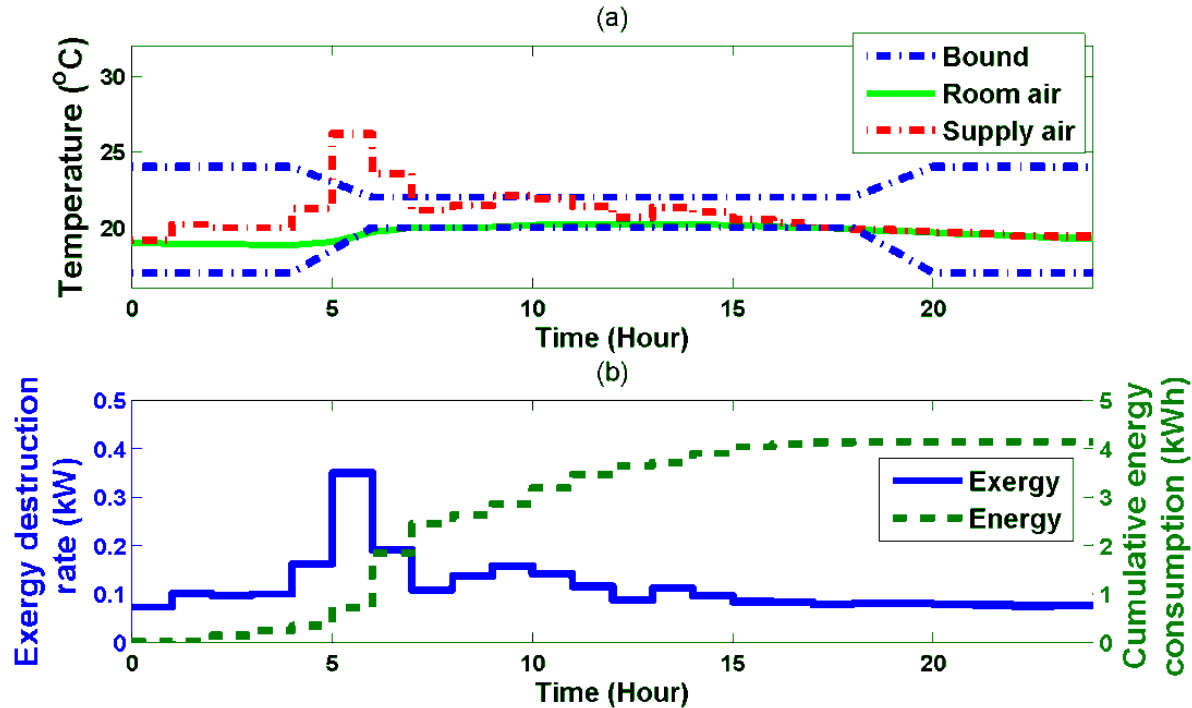


## b) MPC



# Results: Exergy-Based MPC (XMPC)

32



# Results: Comparison Table

33

Controller type	Exergy destruction [kWh]	Energy consumption [kWh]	Reduction in exergy destruction* w/r to RBC [%]	Reduction in energy consumption* w/r to RBC [%]
XMPC	2.7	4.2	22	36
EMPC	2.8	4.6	18	24
RBC	3.3	5.7	-	-

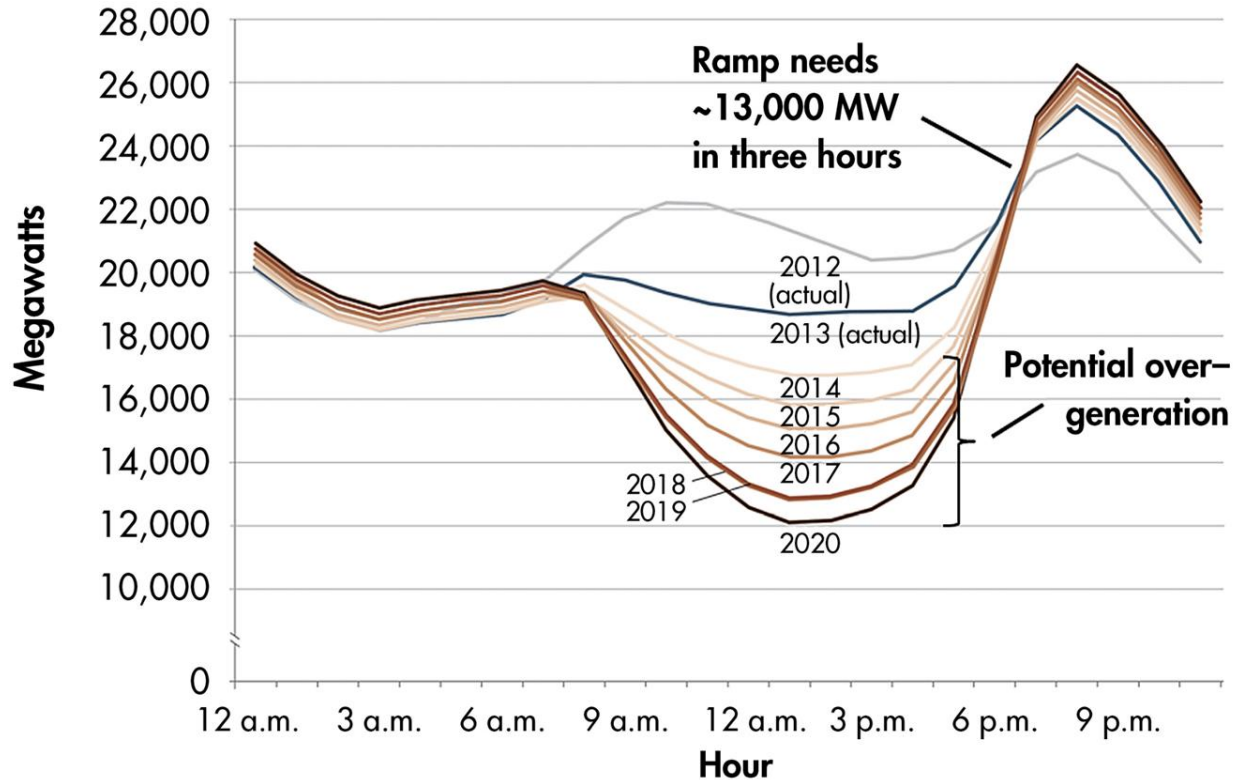
\*Saving percentage is calculated by  $\frac{(x_0 - x)}{x}$ , where  $x_0$  is result of RBC controller.

## Part II: Control of building energy systems

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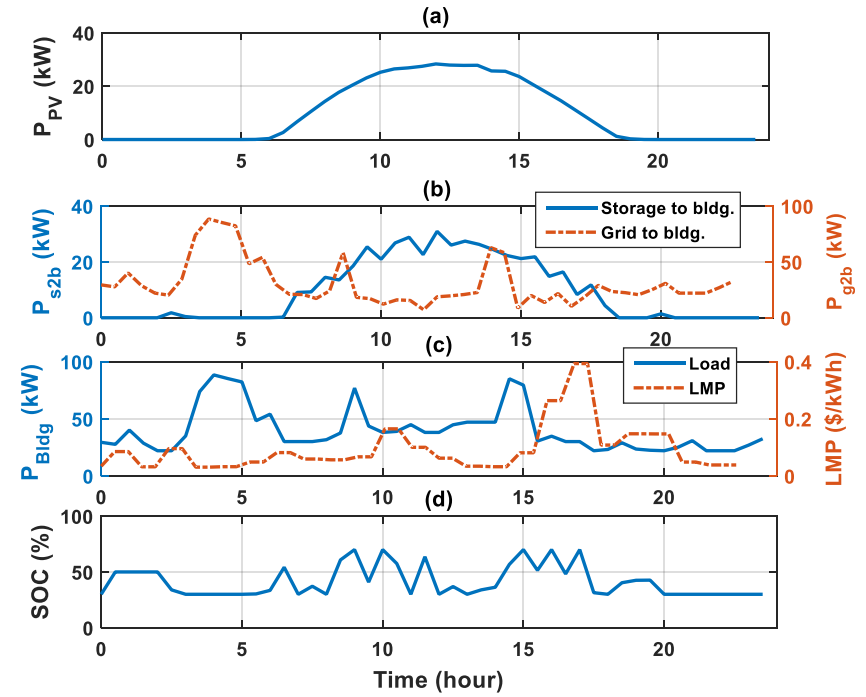
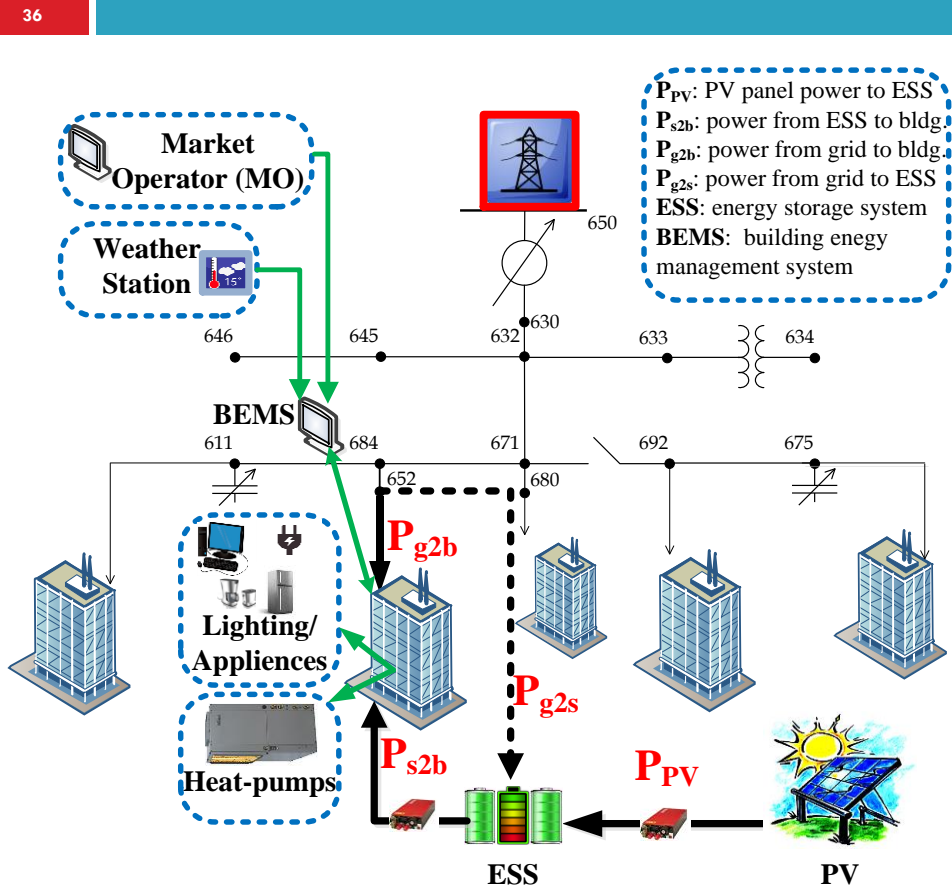
- Modeling of building energy systems
- Predictive control of building HVAC systems
- **Building-to-grid optimization**

# Motivation: Rapid renewable penetration and ramp rate during peak hours



Source: California ISO, Net Load on CASIO system.  
<http://www.caiso.com/informed/Pages/CleanGrid/TodaysRenewables.aspx>. Accessed Feb 28<sup>th</sup> 2017.

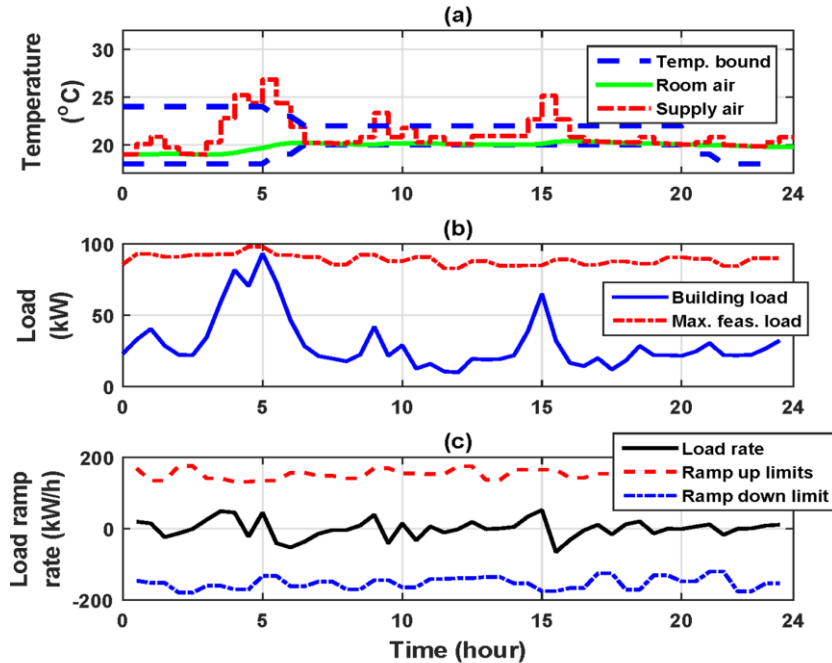
# Demand Response via B2G system with PV panels and energy storage system (ESS)



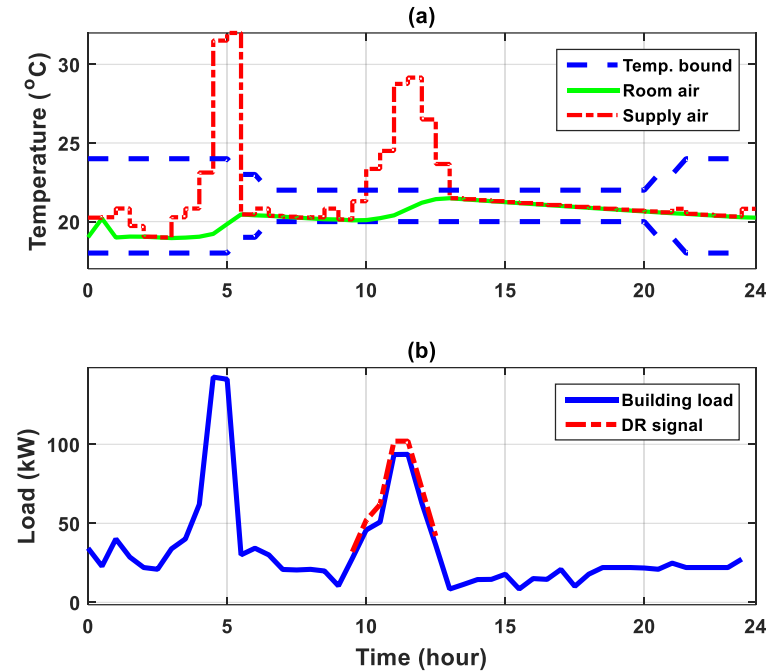


# Building load and ramp rate controls

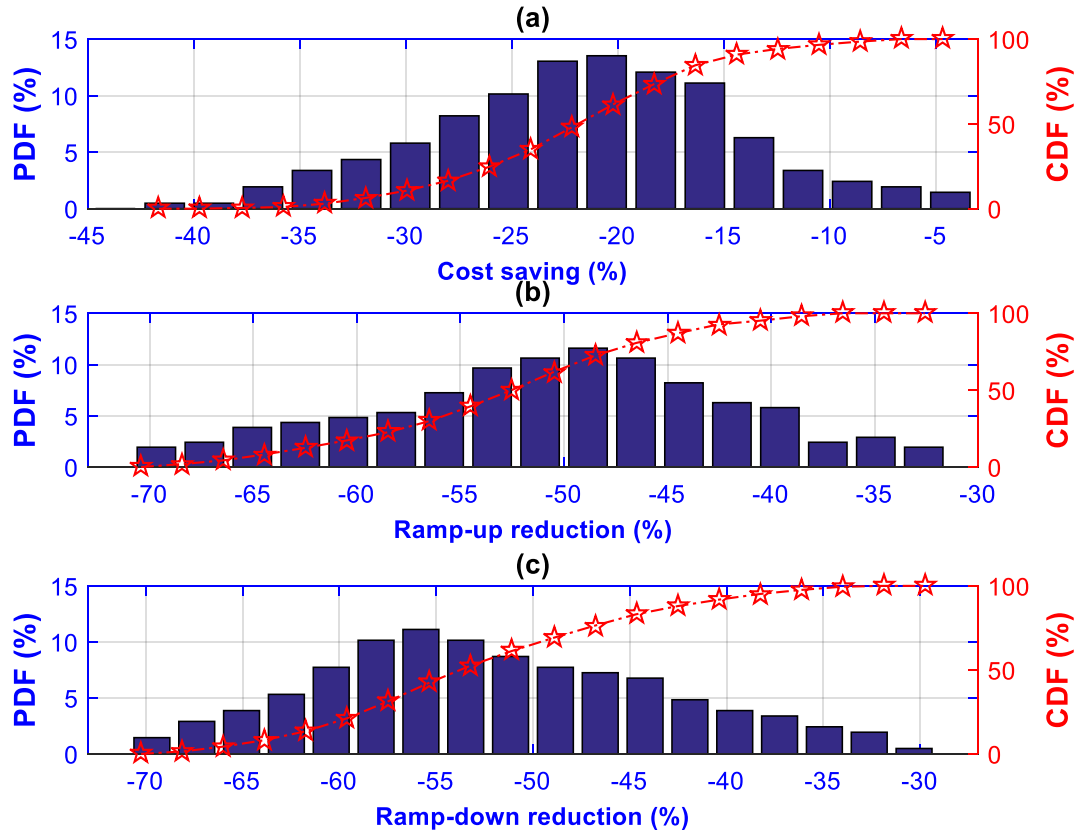
- Ramp rate control



- Load following



# Probability of providing benefits from proposed bidirectional B2G controls based on Monte-Carlo simulations



# Summary (I)

- Model-based predictive control for buildings
  - requires an accurate dynamic model of buildings and renewable sources → *Parameter Adaptive Building Model*;
  - can optimize HVAC system performance by integrating system dynamics;
  - can achieve 36% reduction in energy consumption in building HVAC systems, using exergy-wise MPC.

# Summary (II)

- Bi-directional building-to-grid (B2G) optimization
  - can help the power grid to employ the flexibility of buildings HVAC system to prevent problems such as duck-curve, over generation, and intermittent production;
  - can reduce monthly electricity costs 5-42%, compared to the unoptimized rule-based control;
  - can help to reduce load ramp-rate by 30-70% in buildings

**Part III:  
Control of Powertrain  
and Hybrid Electric  
Vehicles**

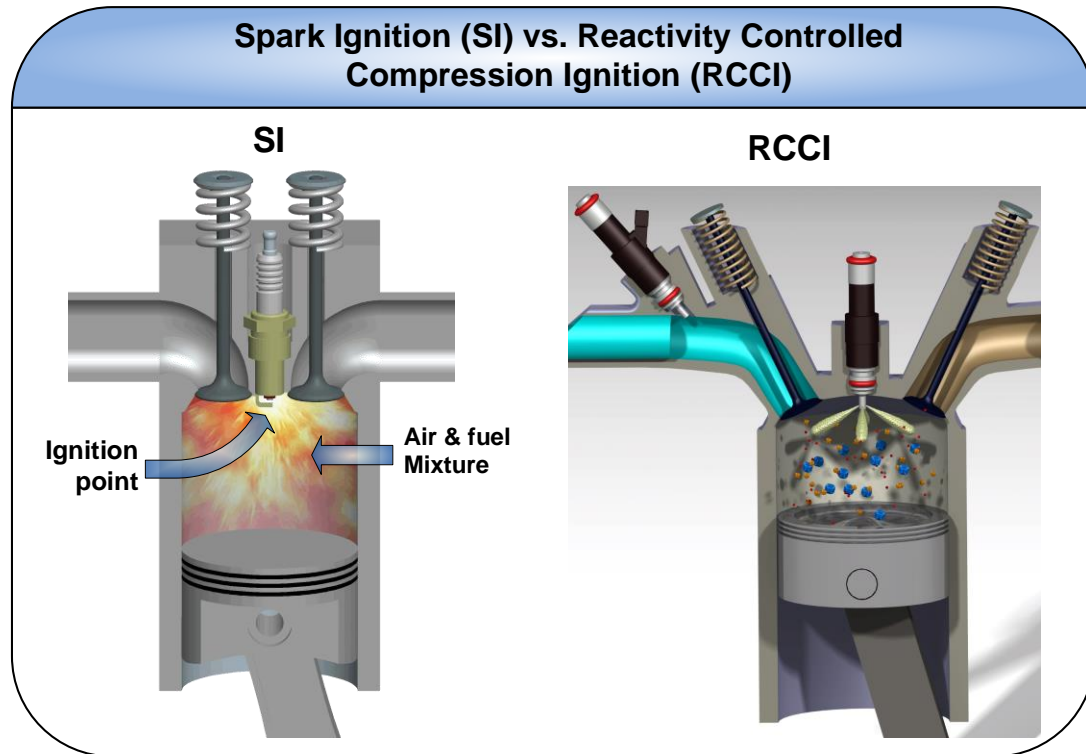
# Part III: Control of automotive energy systems

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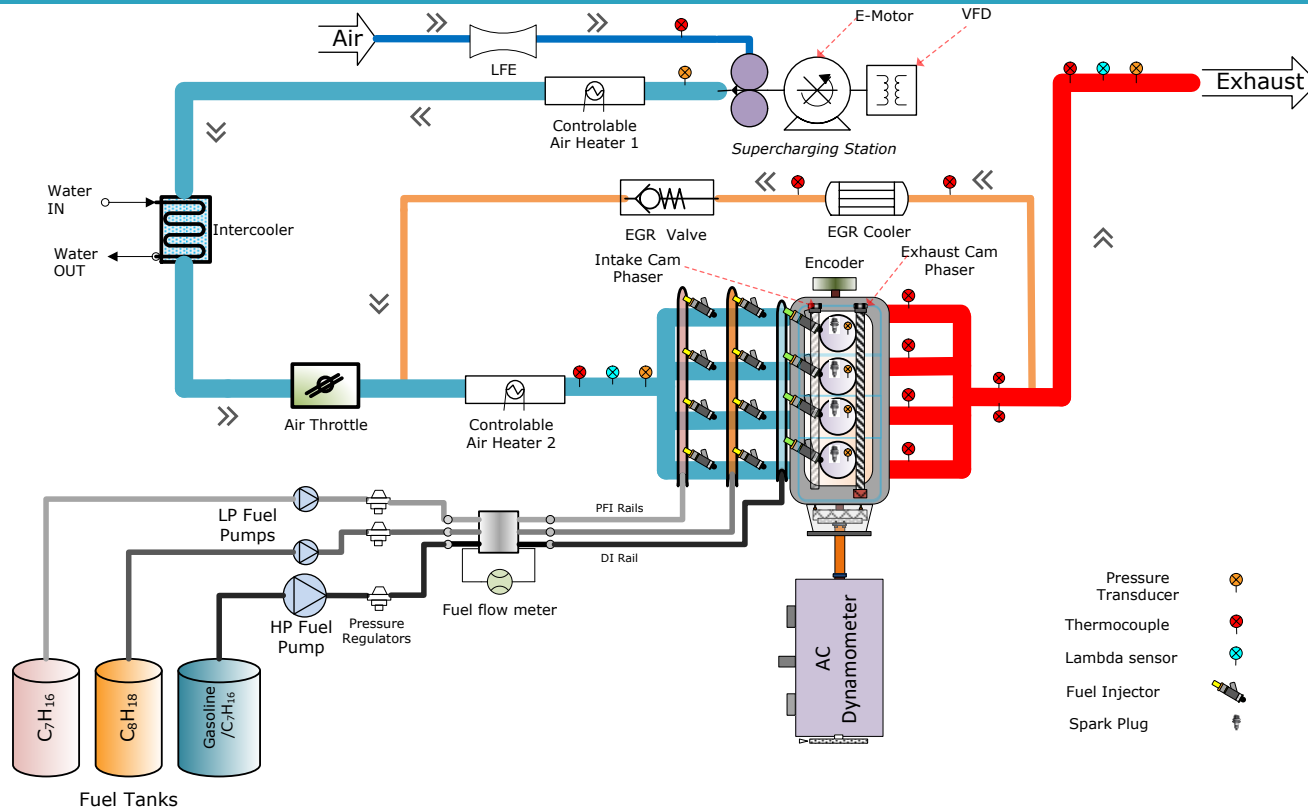
- **Model-based control of advanced IC engines**
- Predictive control of hybrid electric vehicles
- Control of connected and automated vehicles

# Introduction

RCCI offers peak indicated thermal efficiency of 53%, with ultra low NO<sub>x</sub> and PM emissions!



# Engine Experimental Setup





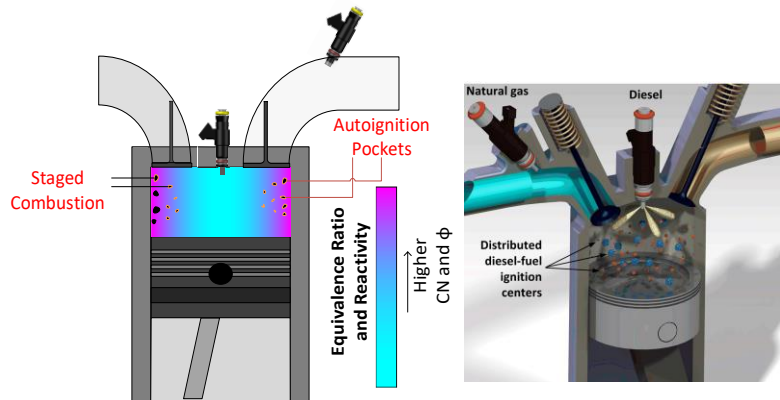
# Engine Experimental Setup



# Dynamic Model of RCCI Engines

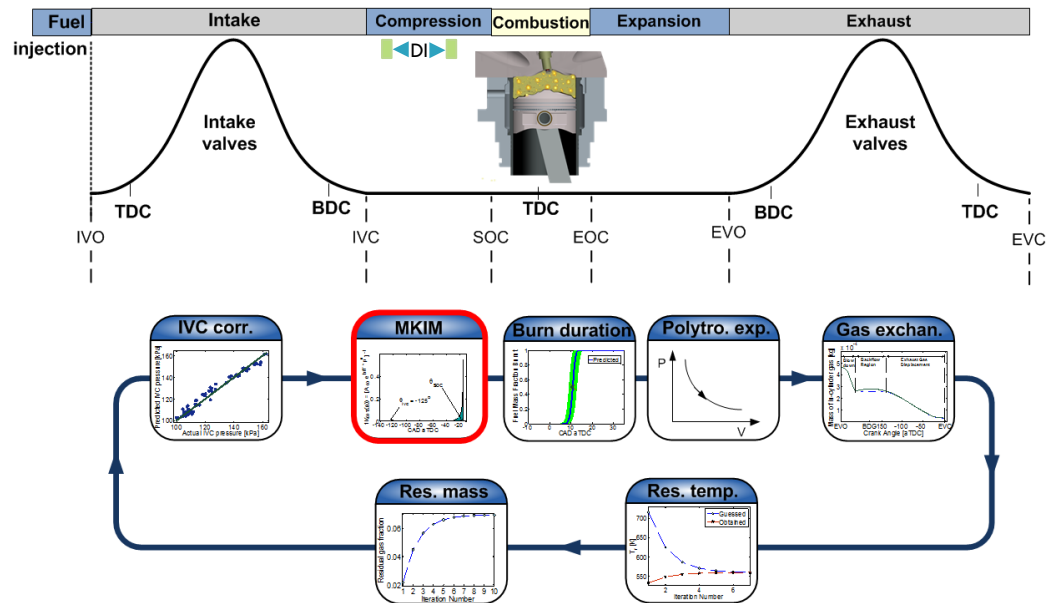
Predicts cycle-by-cycle combustion phasing and load

## Phenomenological Model



$$\int_{SOI}^{SOC} \frac{d\theta}{N A_2 (\varphi_{DI}^{B_2 DI} + \varphi_{PFI}^{B_2 PFI}) \exp\left(\frac{a}{(CN_{mix} + b)} \left(\frac{P_{IVC} v_c^{k_c}}{T_{IVC} v_c^{k_c-1}}\right)^{D_2}\right)} + \int_{IVC}^{SOI} \frac{d\theta}{A_1 N \varphi_{PFI}^{B_1} \exp\left(\frac{C_1}{T_{IVC} v_c^{k_c-1}} \left(\frac{P_{IVC} v_c^{k_c}}{T_{IVC} v_c^{k_c-1}}\right)^{D_1}\right)} = 1$$

## Dynamic Model



\* K. Sadabadi, M. Shahbakhti, A. Bharath, and R. Reitz. "Modelling of Combustion Phasing of an RCCI Engine for Control Applications." *Int. J. of Engine Research*, 2016.

\* K. Sadabadi, M. Shahbakhti, "Dynamic Modeling and Controller Design of Combustion Phasing of an RCCI Engine", ASME Dynamic Systems Control Conference, 2016.

# Natural gas-diesel RCCI Engine Controller

## State-Space Representation

$$X_{k+1} = f(X_k, u_k, d_k)$$

$$y_{k+1} = g(X_k, u_k, d_k)$$

### □ States

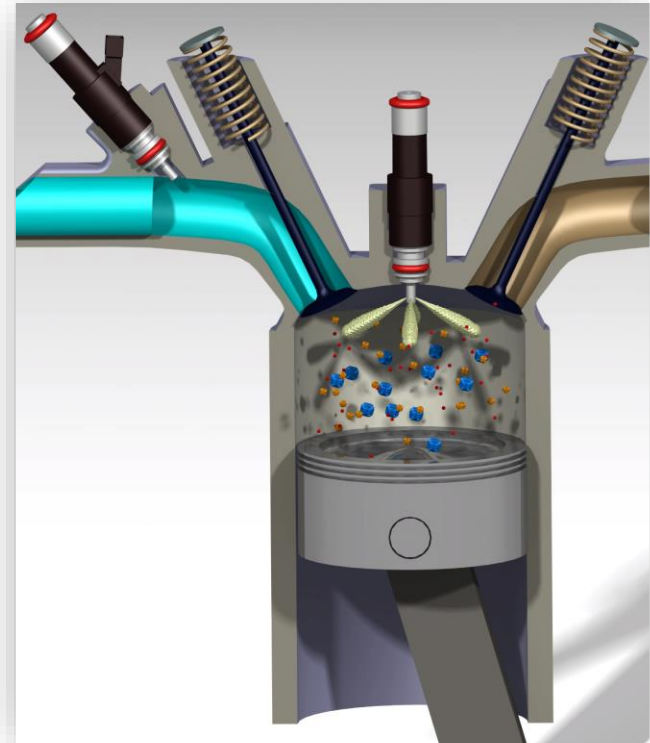
$$X = [CA50 \quad T_{soc} \quad P_{soc} \quad T_{rg} \quad m_{evc}]$$

### □ Control inputs

$$u = [PR, SOI, FQ]$$

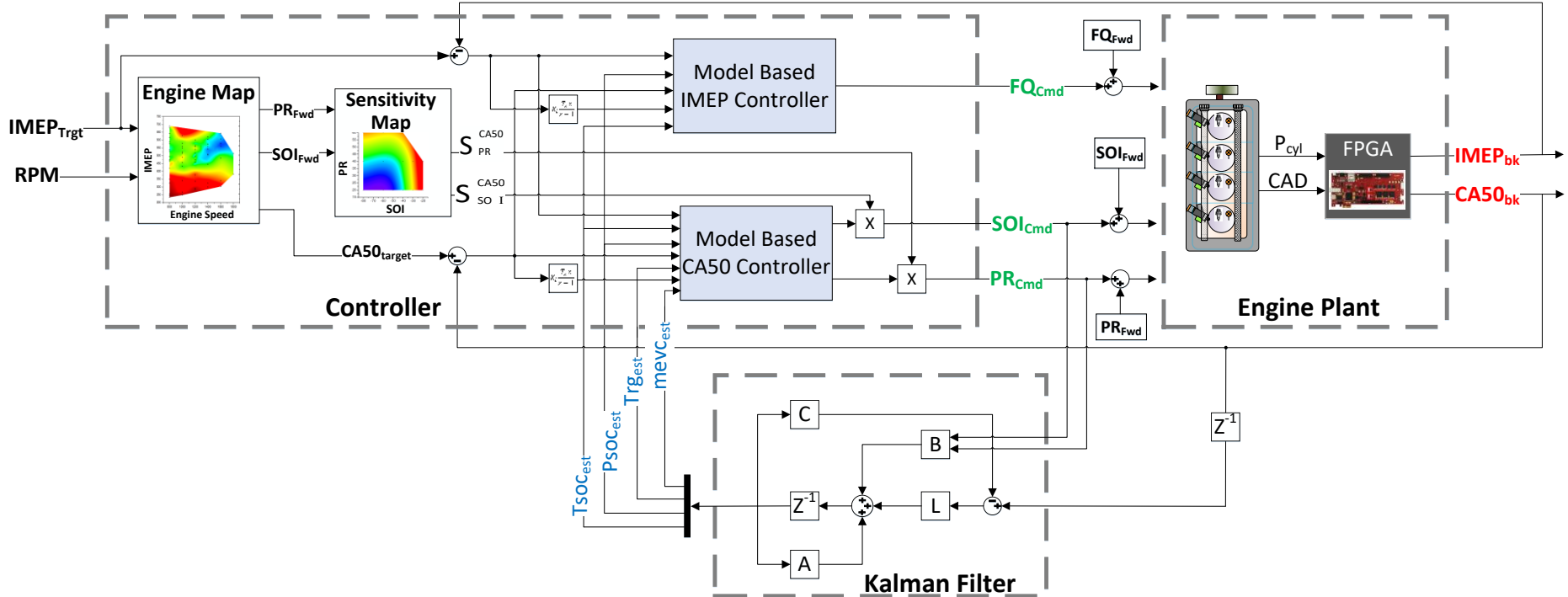
### □ Disturbance

$$d = [T_{man}]$$

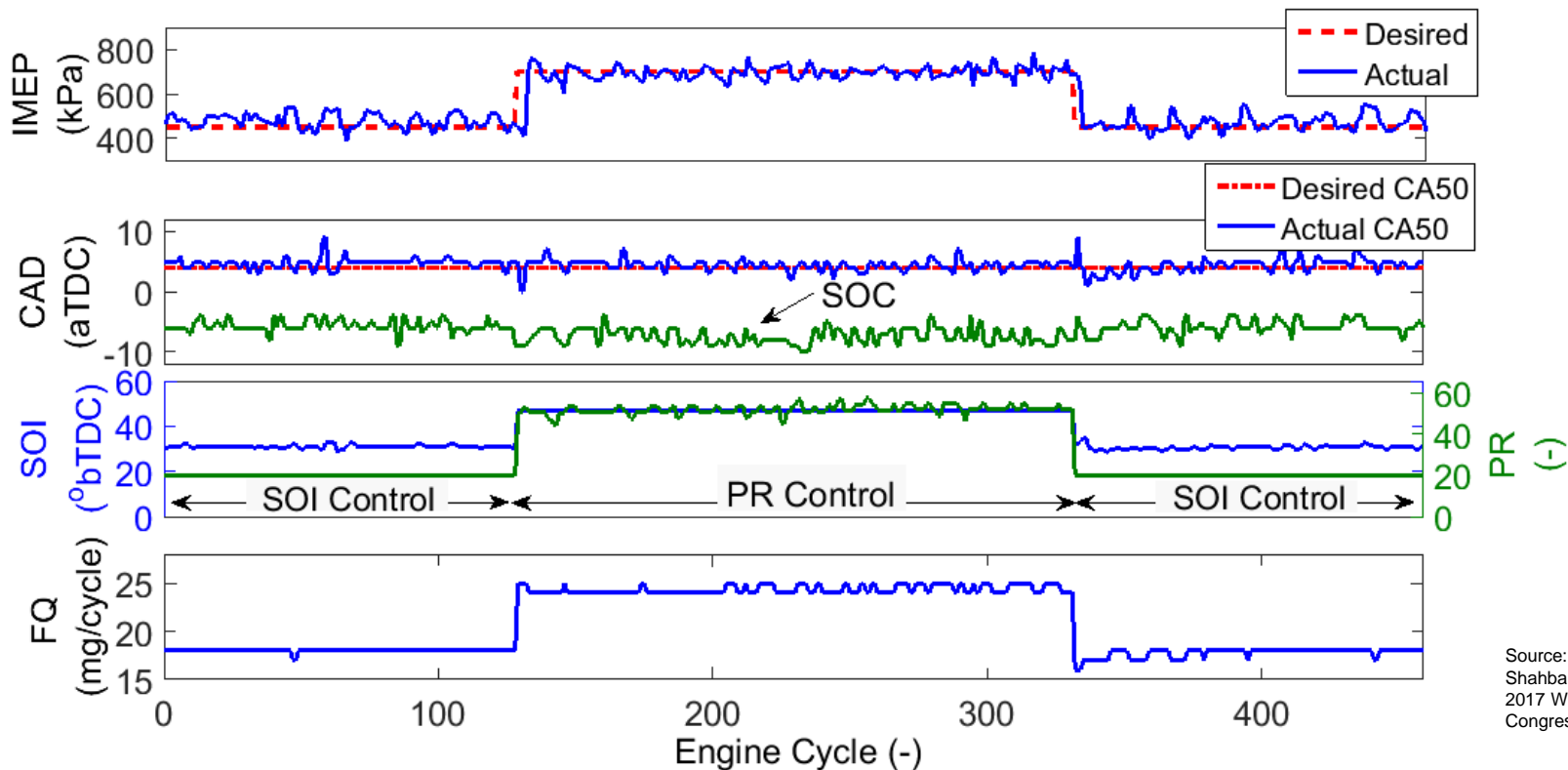


# RCCI Engine Controller

## Block Diagram

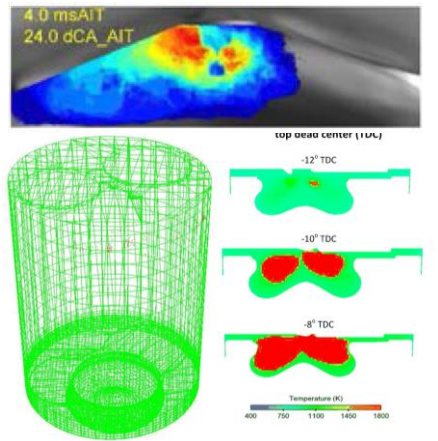


# Experimental Control Results

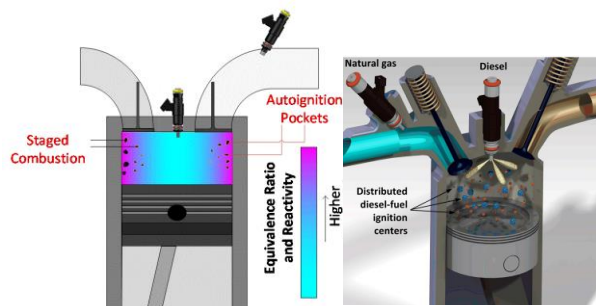


# Summary

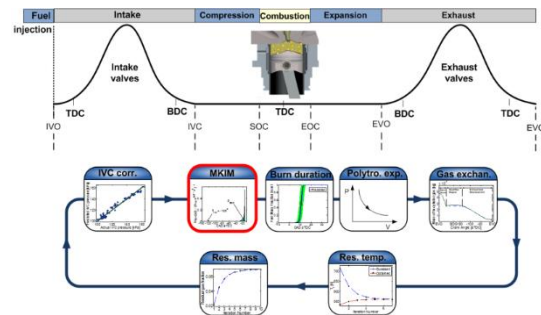
## I. Optical Engine Data/ Detailed Combustion Model



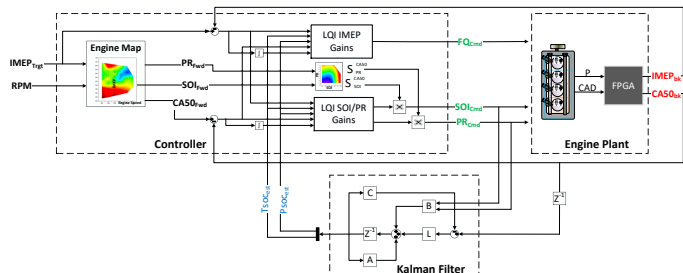
## II. Phenomenological Combustion Model



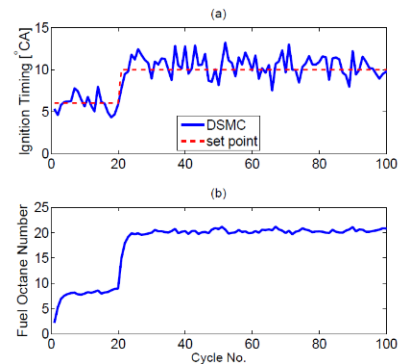
## III. Control Dynamic Model



## IV. Model-based Controller Design



## V. Combustion Control



# Part III: Control of automotive energy systems

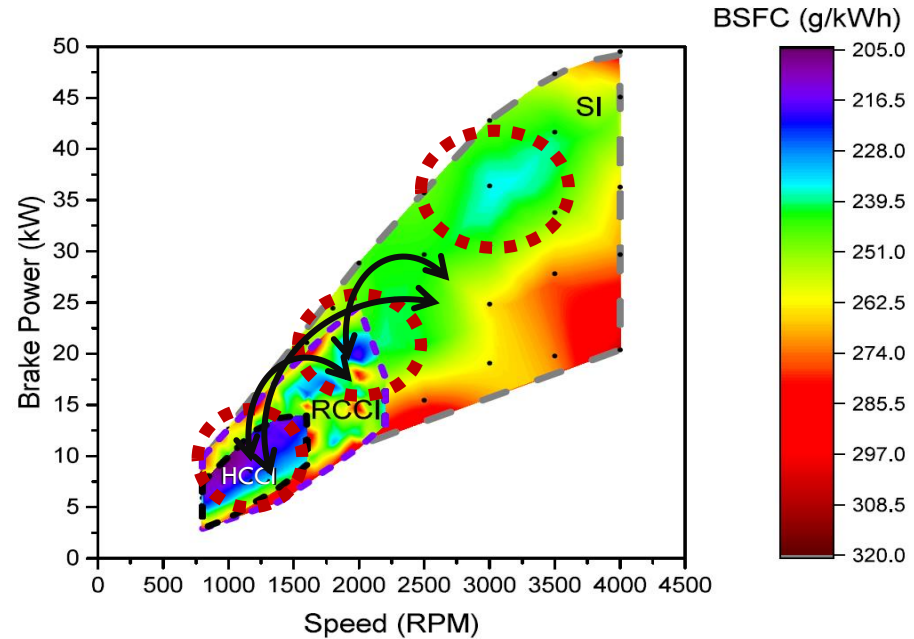
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- Model-based control of IC engines
- **Predictive control of hybrid electric vehicles**
- Control of connected and automated vehicles

# Motivation

## Electrified multi-mode powertrain for best fuel conversion efficiency

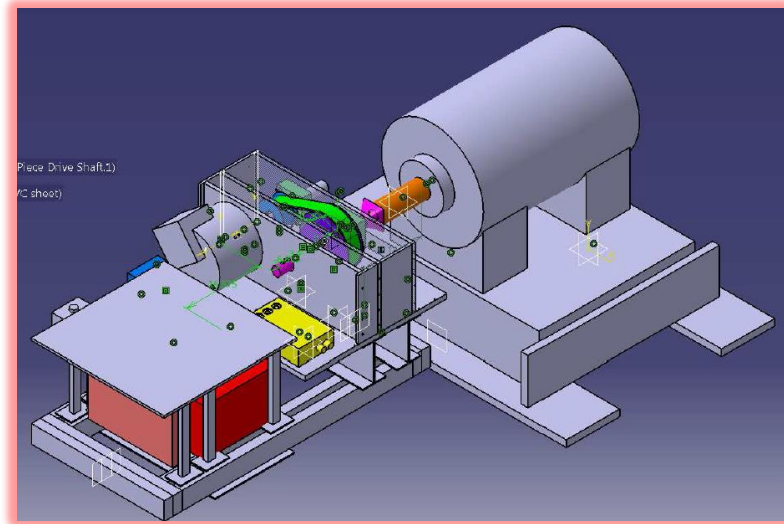
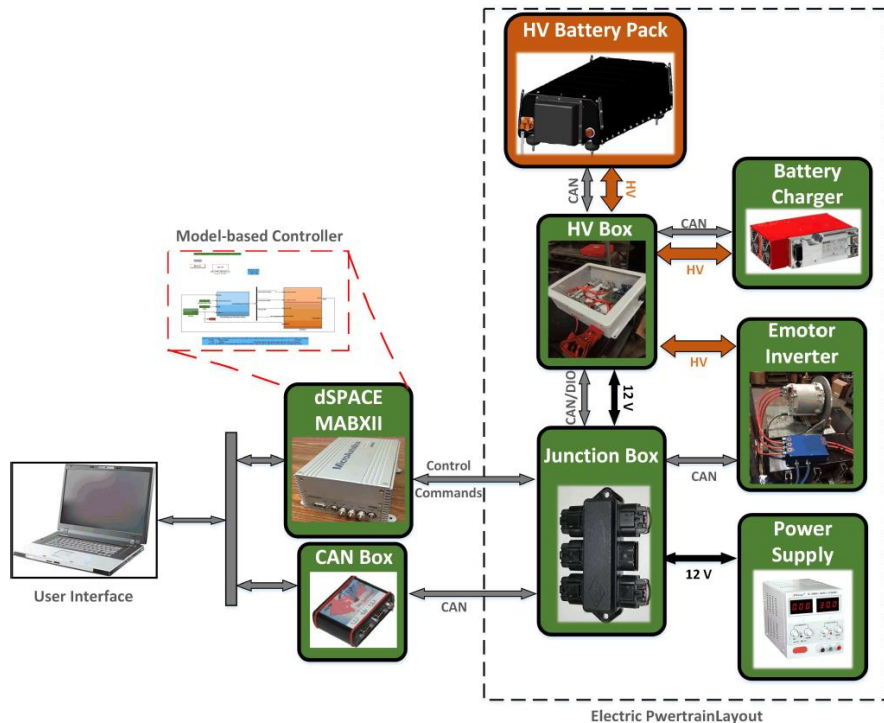
- SI mode is more efficient in the high power region.
- RCCI mode is more efficient in the medium power region.
- HCCI mode is more efficient in the low power region.



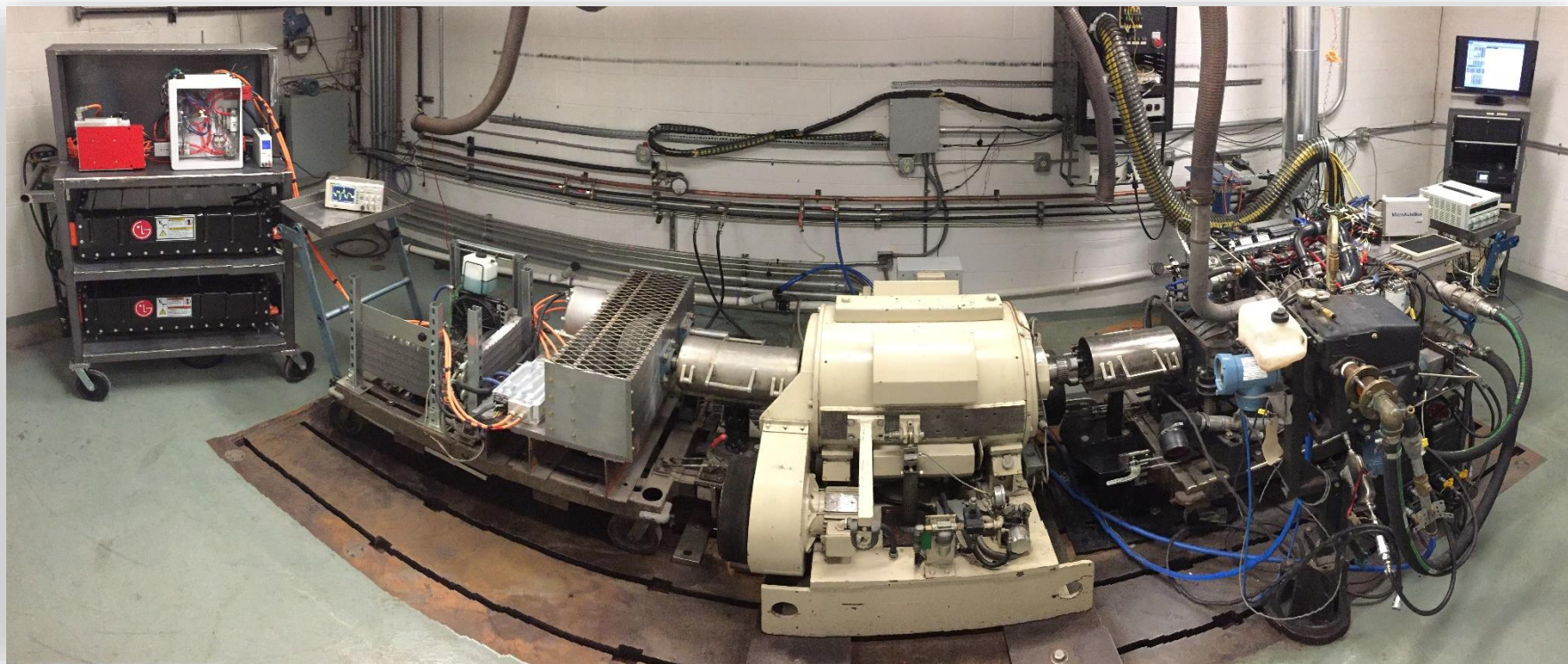
Electrification helps to utilize the best engine points and minimize engine transients!



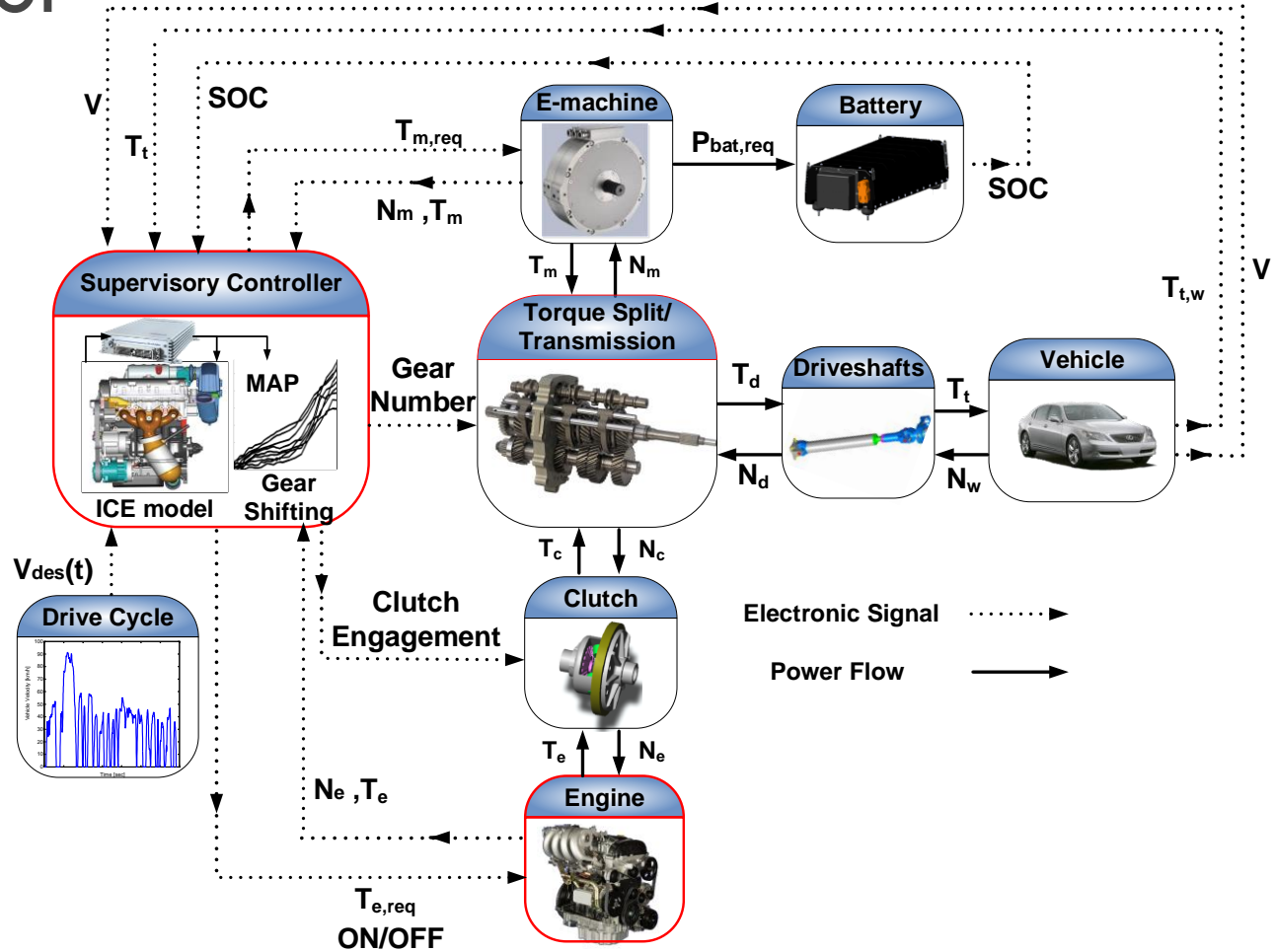
# Design of Hybrid Electric Powertrain Testbed



# Multi-Mode Electrified Experimental Setup



# HEV Models for Optimization



# Design of Optimal Control for Multi-Mode Hybrid Electric Vehicle

## Cost Function:

$$J(u(t)) = \int_0^T (\dot{m}_f(P_{bat}, t) + \Gamma \cdot F_{p1} + \Lambda \cdot m_{ij} + \Psi \cdot F_{p2}) dt$$

Engine ON/OFF  
Penalty

Mode-Switching  
Penalty

Gear-Shifting  
Penalty

## Hard Constraints:

$$|SOC_f - SOC_0| \leq 0.01$$

$$0.3 \leq SOC(t) \leq 0.7$$

$$P_{bat,min} \leq P_{bat}(t) \leq P_{bat,max}$$

$$P_{eng,min}(\omega_{eng}) \leq P_{eng}(t, \omega_{eng}) \leq P_{eng,max}(\omega_{eng})$$

$$\omega_{eng,min} \leq \omega_{eng}(t) \leq \omega_{eng,max}$$

$$0 \leq P_{motor}(t) \leq 100 \text{ kW}$$

$$0 \leq \omega_{motor}(t) \leq 8000 \text{ RPM}$$

$$Temp_{exh}(\omega_{eng,min}, T_{eng,min}) \geq 300 \text{ }^\circ\text{C}$$

$$\omega_{eng} \leq 1500 \text{ rpm}, \text{ if } V_{veh} \leq 40 \text{ km/h}$$

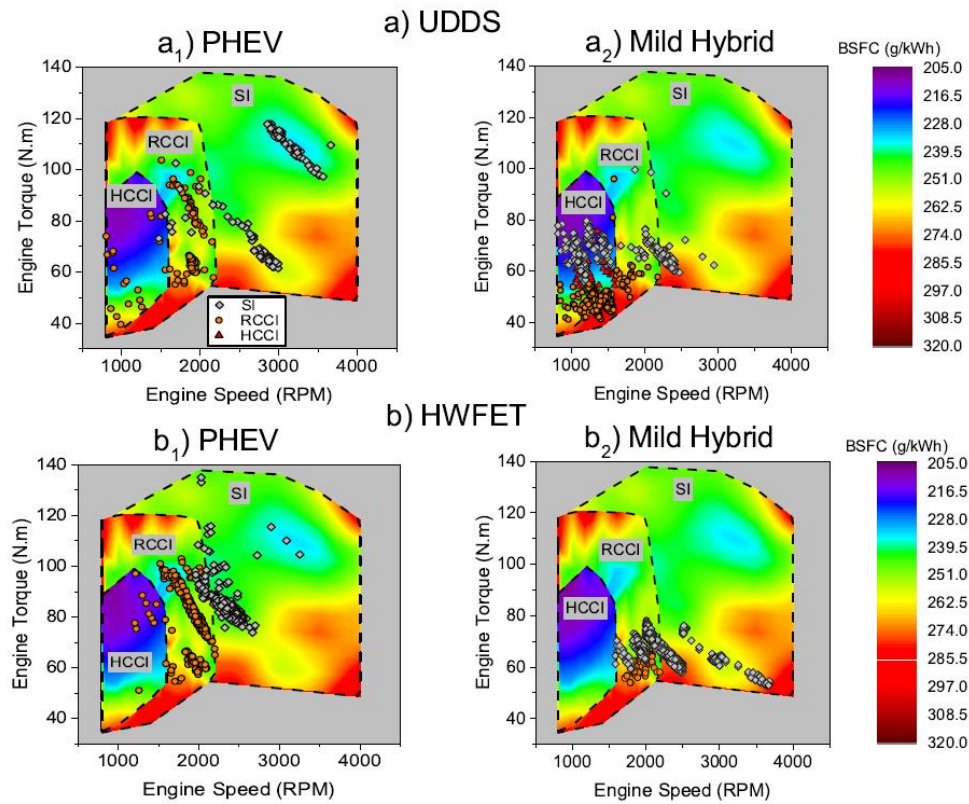
Catalyst light-off  
constraint

NVH constraint



# Analysis for Parallel Architecture

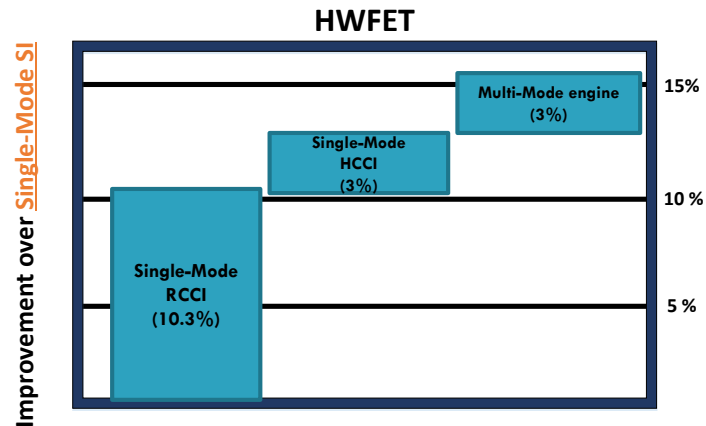
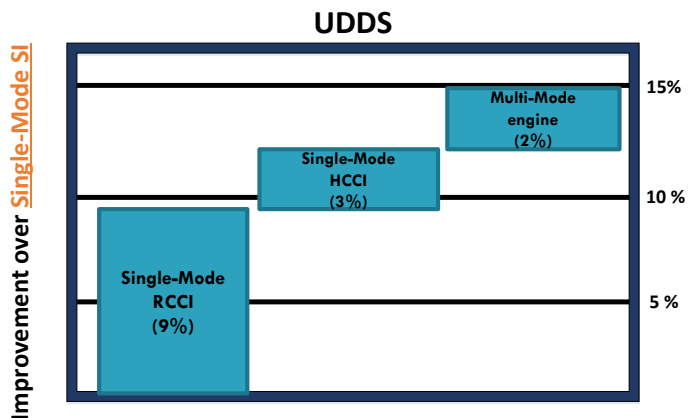
- In the PHEV, the multi-mode LTC-SI engine has less advantage compared to the mild HEV due to availability of higher electric power for locating the engine operating points in high power SI regions



Source: A. Solouk, M. Shahbakhti, et. al., *SAE Int. J. of Alternative Powertrains*, 2017.

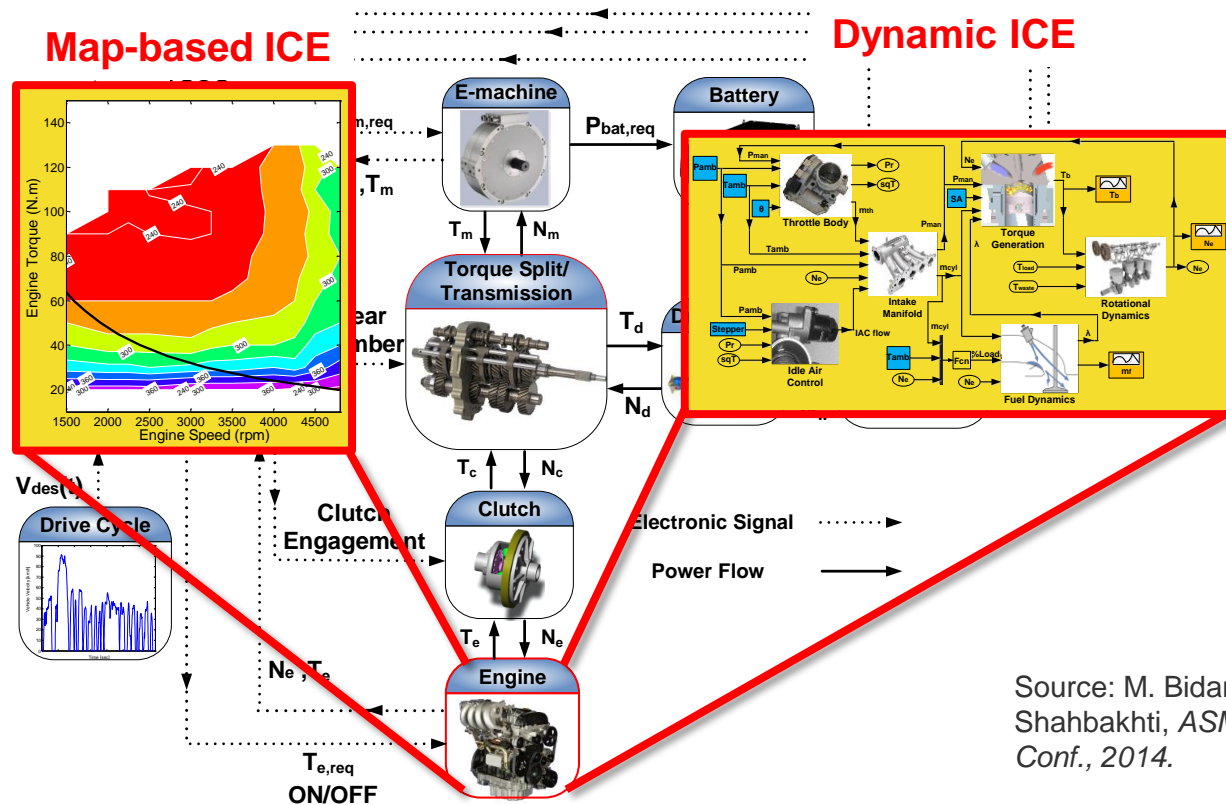
# LTC-HEV Results

- REx (Series) Architecture:**

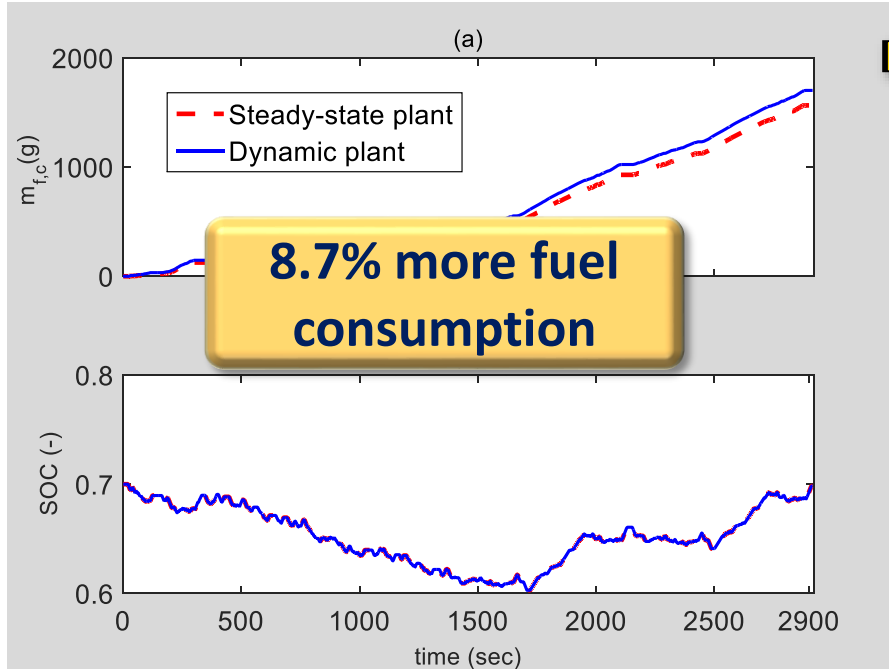


- The **REx** platform provides the higher fuel saving for the multi-mode LTC-SI, compared to the parallel hybrid electric platform.

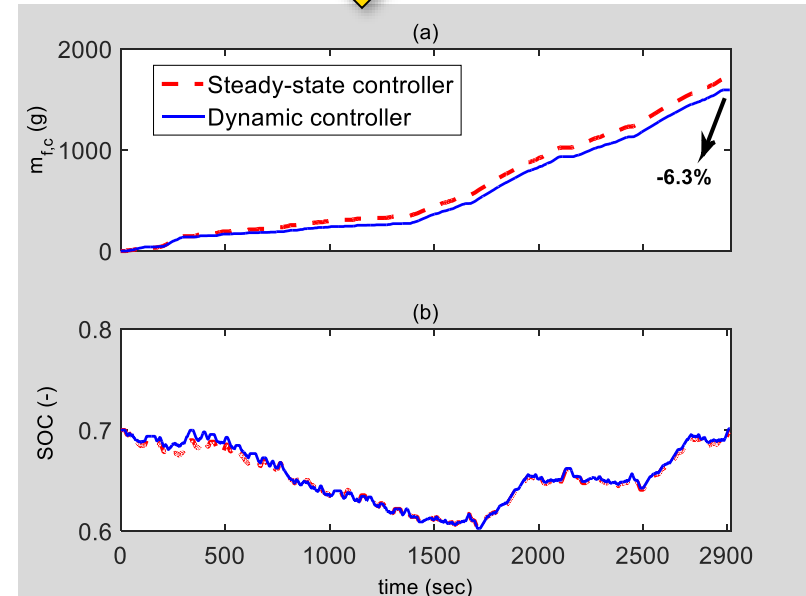
# Energy Management/Control of a Hybrid electric Vehicle by Incorporating Powertrain Dynamics



# Combined UDDS+HWFET Drive Cycle Results



$$\mathbb{J}_{dyn}(k) = \int_{t_k}^{t_k+t_p} [(\dot{m}_f(t) + \dot{m}_{f,pen}(\Delta N_e, T_e)) \cdot Q_{hv} + \alpha \cdot P_{bat,req}] dt$$



Source: M. Bidarvatan, M. Shahbakhti, *ASME Dyn Sys Ctrl Conf.*, 2015.



# Part III: Control of automotive energy systems

---

- Model-based control of IC engines
- Predictive control of hybrid electric vehicles
- **Control of connected and automated vehicles**

# Motivation: V2X data can tell us about future power demand for vehicle controls

By 2021, all the vehicles sold in US will be connected vehicles!

Traffic conditions



Traffic lights



Neighboring vehicles (V2V)



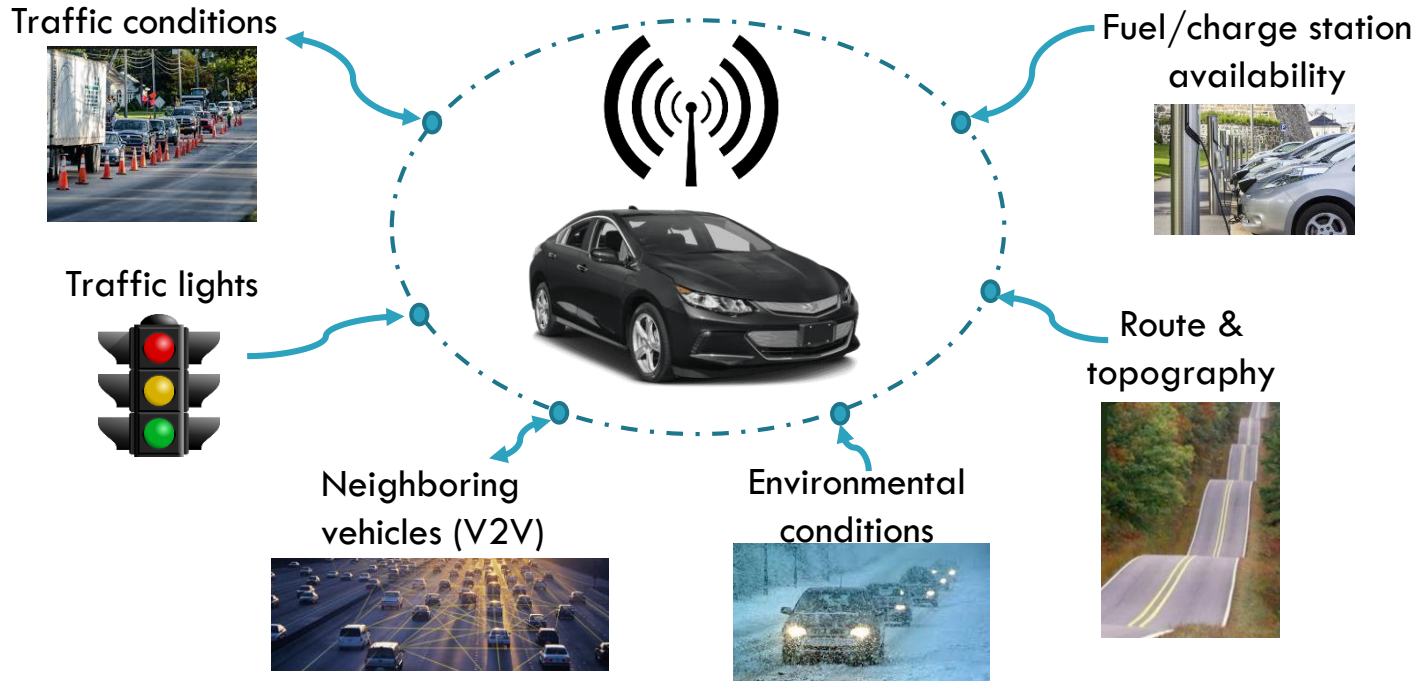
Environmental conditions



Fuel/charge station availability

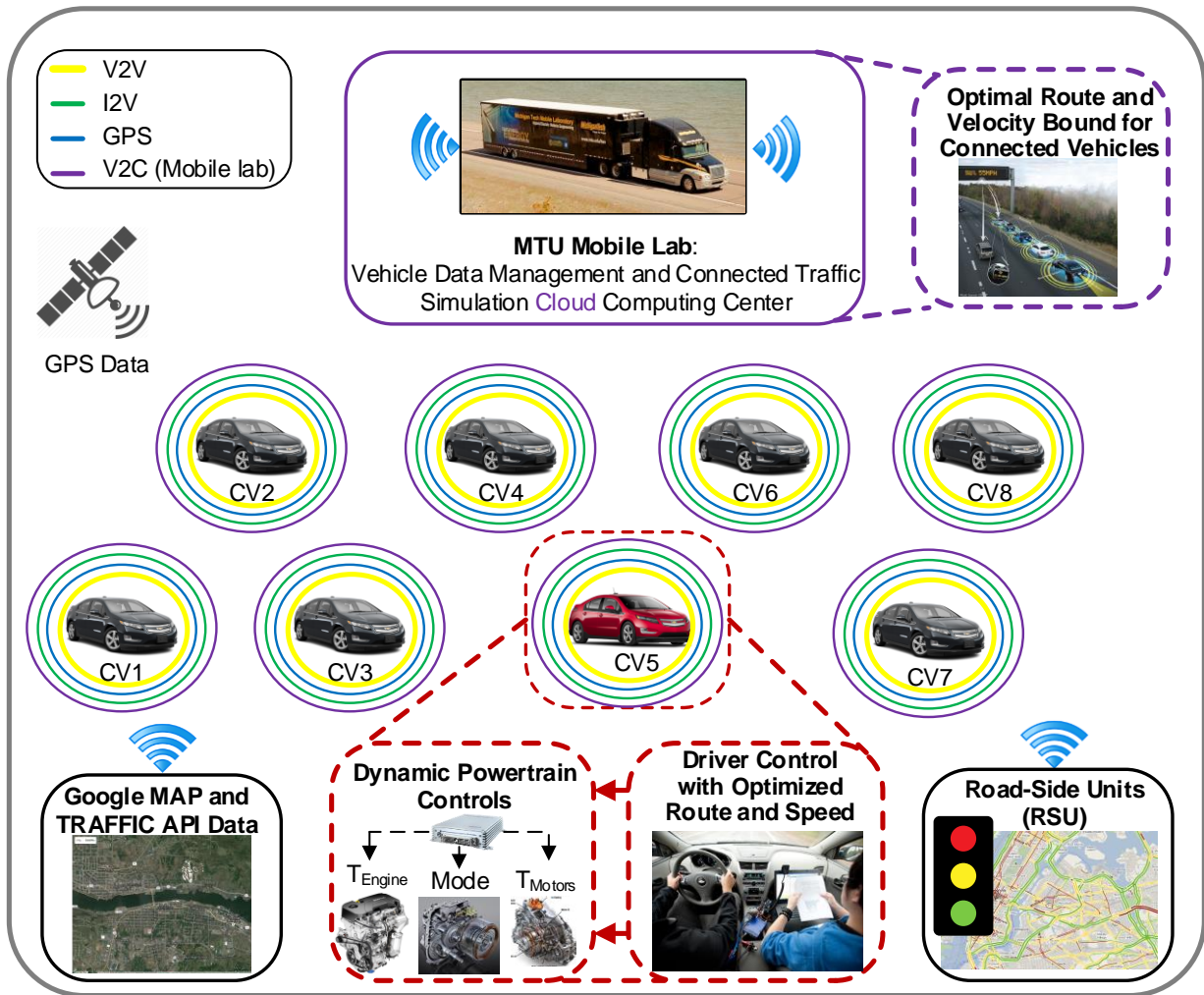


Route & topography



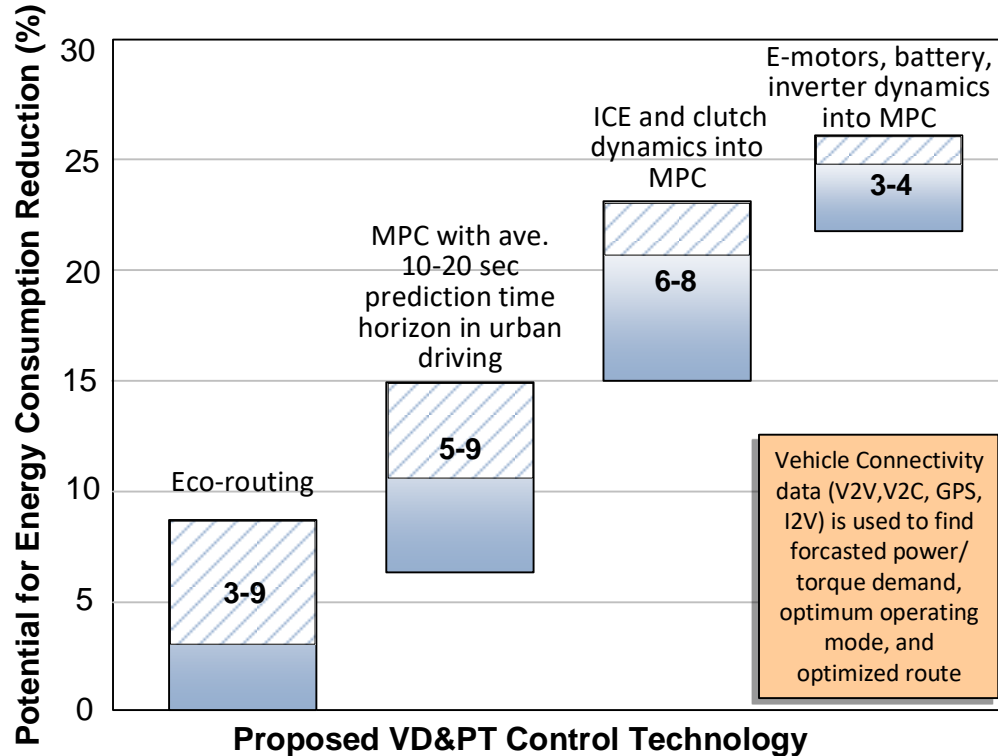
# Michigan Tech- GM NextCar Project

- Vehicle dynamic and powertrain control for connected and automated vehicles
- Targets:
  - 20% reduction in energy consumption in PHEV/HEV operation
  - 6% increase in EV range



# NextCar:

## Projection of energy consumption reduction



# NextCar: Real-time optimal (i) route selection, (ii) vehicle 5 modes selection, (iii) speed trajectory, (iv) ICE/motor torques/speeds

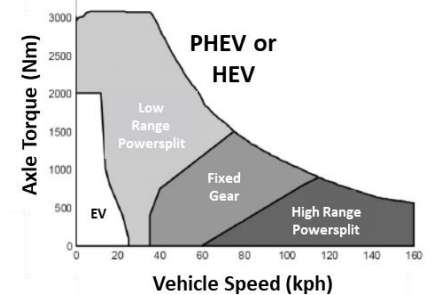
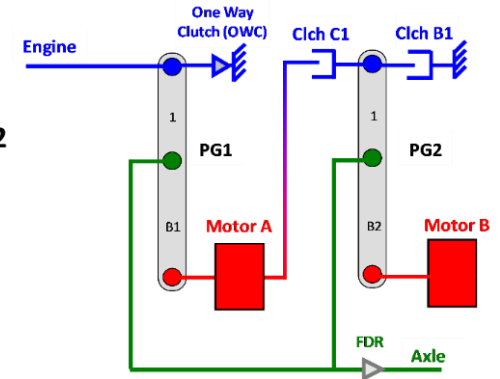
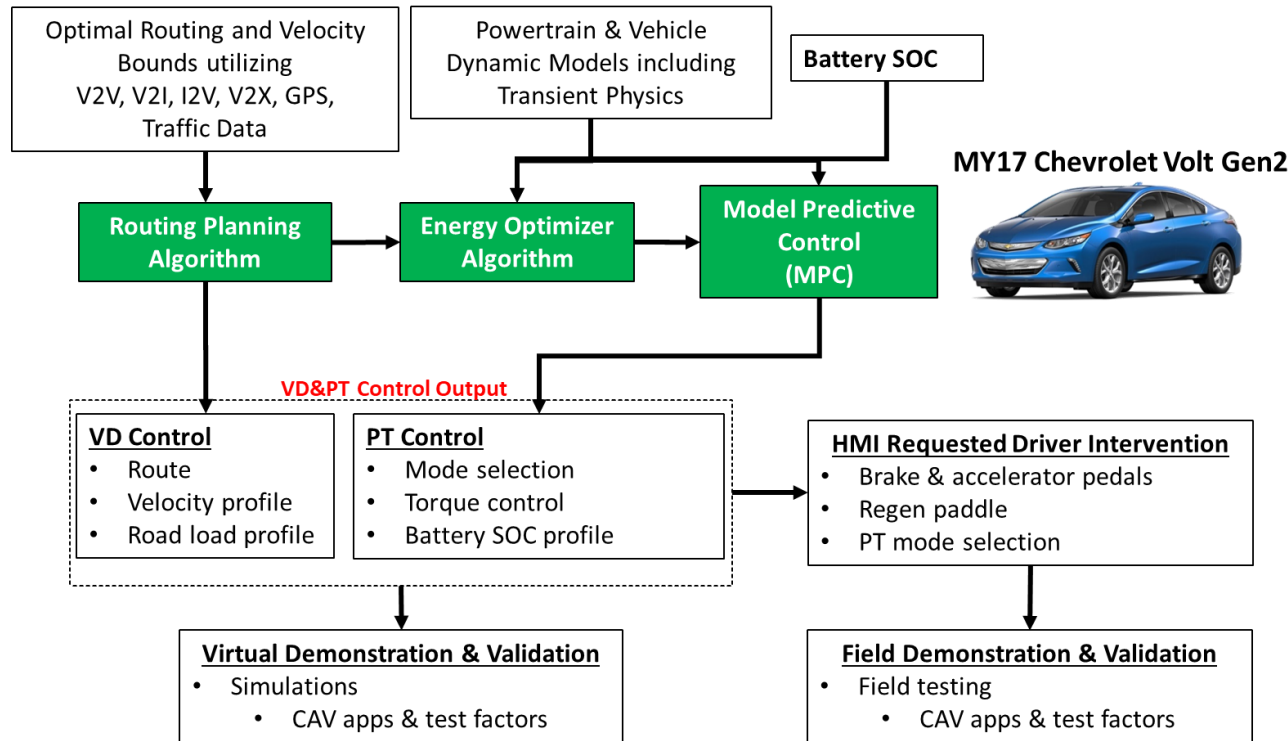
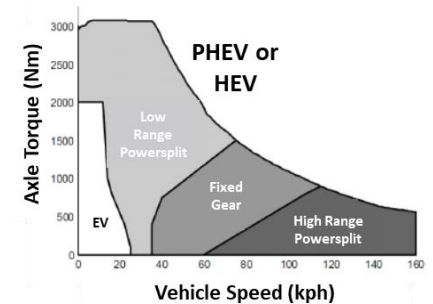
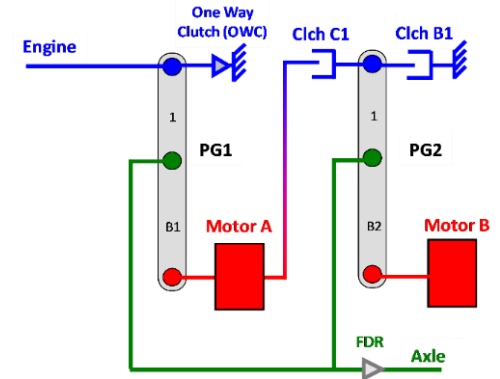
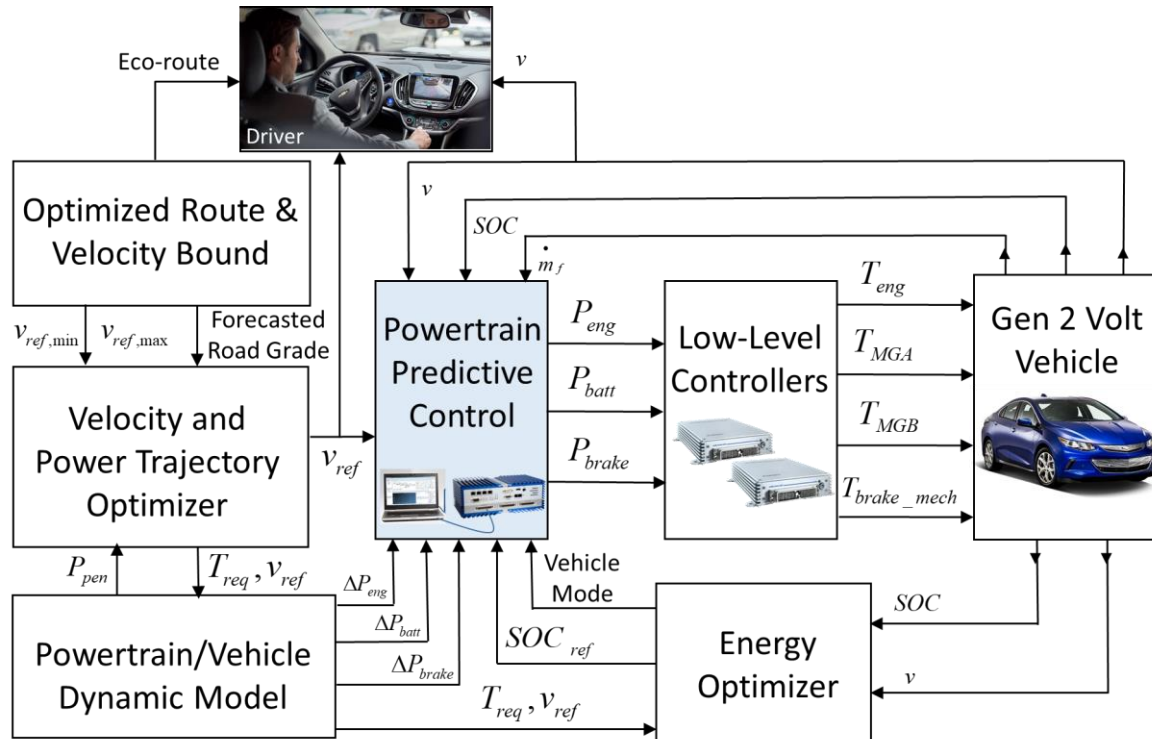


Image of modes: SAE 2015-01-1152

# NextCar: Real-time optimal (i) route selection, (ii) vehicle 5 modes selection, (iii) speed trajectory, (iv) ICE/motor torques/speeds





# NextCar Platform



Mobile Lab traffic center

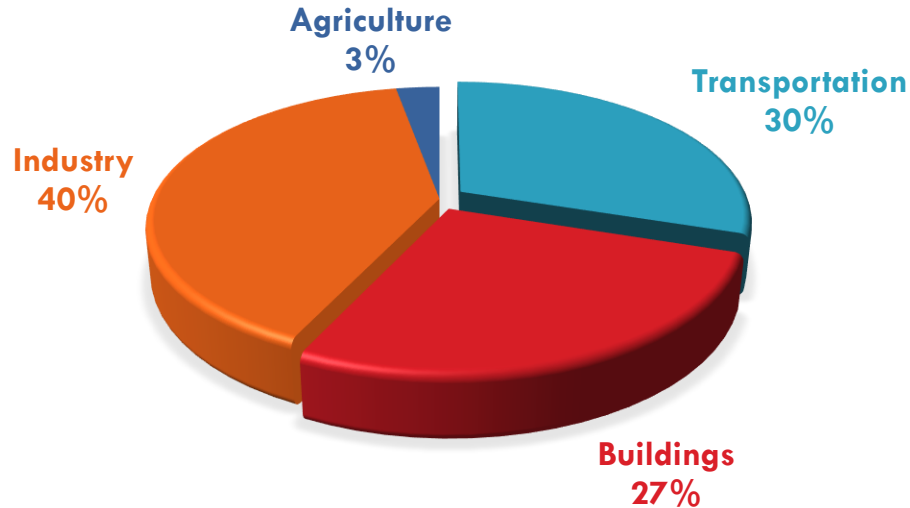


Mode selection and velocity optimization

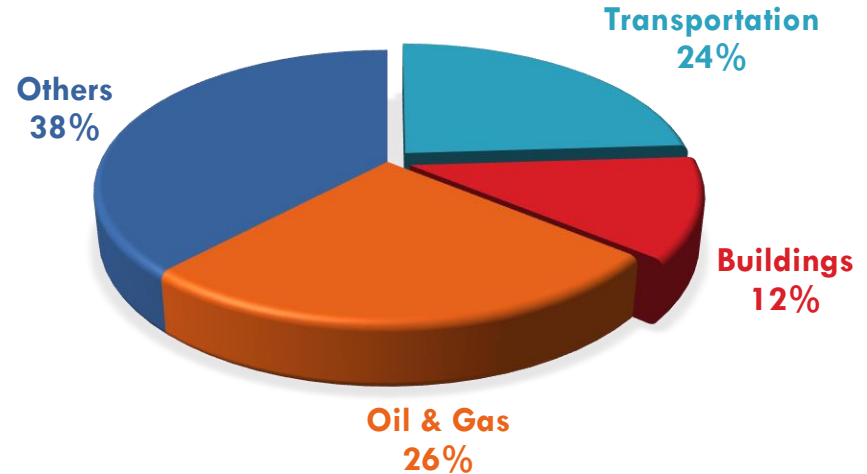


# Concluding remarks (I)

## Canada Energy Consumption by End Users



## Greenhouse Gas Emissions



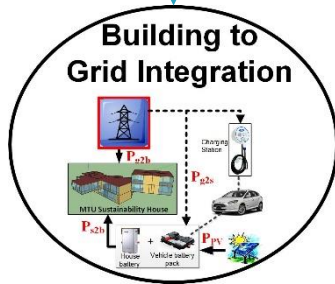


# Concluding remarks (II)

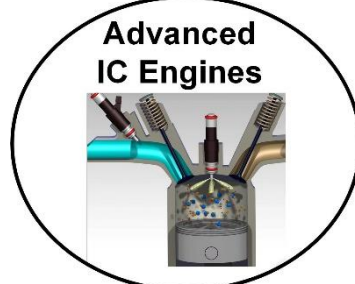
## Model-based Control of Building and Automotive Energy Systems



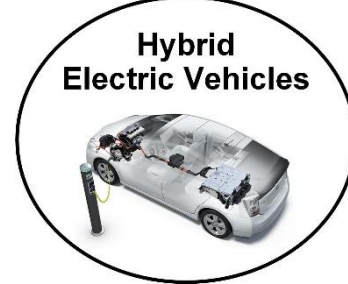
24-36%  
Energy  
Saving



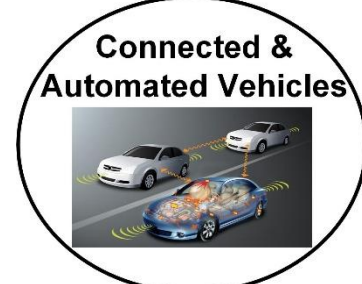
5-42%  
Elec. Cost  
Saving



upto 15%  
Energy  
Saving



6-17%  
Energy  
Saving

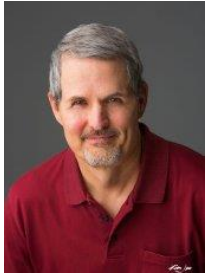


6-20%  
Energy  
Saving

# Acknowledgments (I)

## Current/past collaborators for materials presented

70



Prof. Rush Robinett  
Michigan Tech.



Prof. Sumit Paudyal  
Michigan Tech.



Prof. Rolf Reitz  
U. Wisconsin Madison



Dr. Ali Borhan  
Cummins



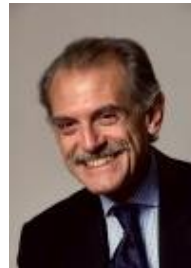
Prof. Javad Mohammadpour  
U. of Georgia



Prof. Jeff Naber  
Michigan Tech.



Dr. Mehdi Maasoumy  
C3 IoT, California



Prof. Alberto S. Vincentelli  
UC Berkeley



Dr. Ali Shakiba  
Ford Motor Company

# Acknowledgments (II)

## Collaborators in NextCar Project

71



# Acknowledgments (III)

## EML Sponsors



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**TOYOTA**





# THANK YOU!

## Questions?

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